

Programming Languages and Compilers (CS 421)

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LR Parsing Tables

- Build a pair of tables, Action and Goto, from the grammar
 - This is the hardest part, we omit here
 - Rows labeled by states
 - For Action, columns labeled by terminals and “end-of-tokens” marker
 - (more generally strings of terminals of fixed length)
 - For Goto, columns labeled by non-terminals

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Action and Goto Tables

- Given a state and the next input, Action table says either
 - **shift** and go to state n , or
 - **reduce** by production k (explained in a bit)
 - **accept** or **error**
- Given a state and a non-terminal, Goto table says
 - go to state m

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LR(i) Parsing Algorithm

- Based on push-down automata
- Uses states and transitions (as recorded in Action and Goto tables)
- Uses a stack containing states, terminals and non-terminals

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LR(i) Parsing Algorithm

0. Insure token stream ends in special “end-of-tokens” symbol
1. Start in state 1 with an empty stack
2. Push **state**(1) onto stack
- 3. Look at next i tokens from token stream ($toks$) (don't remove yet)
4. If top symbol on stack is **state**(n), look up action in Action table at (n , $toks$)

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LR(i) Parsing Algorithm

5. If action = **shift** m ,
 - a) Remove the top token from token stream and push it onto the stack
 - b) Push **state**(m) onto stack
 - c) Go to step 3

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LR(i) Parsing Algorithm

6. If action = **reduce** k where production k is $E ::= u$
- Remove $2 * \text{length}(u)$ symbols from stack (u and all the interleaved states)
 - If new top symbol on stack is **state**(m), look up new state p in $\text{Goto}(m,E)$
 - Push E onto the stack, then push **state**(p) onto the stack
 - Go to step 3

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LR(i) Parsing Algorithm

7. If action = **accept**
- Stop parsing, return success
8. If action = **error**,
- Stop parsing, return failure

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Adding Synthesized Attributes

- Add to each **reduce** a rule for calculating the new synthesized attribute from the component attributes
- Add to each non-terminal pushed onto the stack, the attribute calculated for it
- When performing a **reduce**,
 - gather the recorded attributes from each non-terminal popped from stack
 - Compute new attribute for non-terminal pushed onto stack

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Shift-Reduce Conflicts

- Problem:** can't decide whether the action for a state and input character should be **shift** or **reduce**
- Caused by ambiguity in grammar
- Usually caused by lack of associativity or precedence information in grammar

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Example: $\langle \text{Sum} \rangle = 0 \mid 1 \mid (\langle \text{Sum} \rangle)$
 $\mid \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$

$\bullet 0 + 1 + 0$ shift
 $\rightarrow 0 \bullet + 1 + 0$ reduce
 $\rightarrow \langle \text{Sum} \rangle \bullet + 1 + 0$ shift
 $\rightarrow \langle \text{Sum} \rangle + \bullet 1 + 0$ shift
 $\rightarrow \langle \text{Sum} \rangle + 1 \bullet + 0$ reduce
 $\rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle \bullet + 0$

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Example - cont

- Problem:** shift or reduce?
- You can shift-shift-reduce-reduce or reduce-shift-shift-reduce
- Shift first - right associative
- Reduce first- left associative

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Reduce - Reduce Conflicts

- **Problem:** can't decide between two different rules to reduce by
- Again caused by ambiguity in grammar
- **Symptom:** RHS of one production suffix of another
- Requires examining grammar and rewriting it
- Harder to solve than shift-reduce errors

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Example

■ $S ::= A \mid aB$ $A ::= abc$ $B ::= bc$

● abc shift
a ● bc shift
ab ● c shift
abc ●

- Problem: reduce by $B ::= bc$ then by $S ::= aB$, or by $A ::= abc$ then $S ::= A$?

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Semantics

- Expresses the meaning of syntax
- Static semantics
 - Meaning based only on the form of the expression without executing it
 - Usually restricted to type checking / type inference

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Dynamic semantics

- Method of describing meaning of executing a program
- Several different types:
 - Operational Semantics
 - Axiomatic Semantics
 - Denotational Semantics

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Dynamic Semantics

- Different languages better suited to different types of semantics
- Different types of semantics serve different purposes

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Operational Semantics

- Start with a simple notion of machine
- Describe how to execute (implement) programs of language on virtual machine, by describing how to execute each program statement (ie, following the *structure* of the program)
- Meaning of program is how its execution changes the state of the machine
- Useful as basis for implementations

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Axiomatic Semantics

- Also called Floyd-Hoare Logic
- Based on formal logic (first order predicate calculus)
- Axiomatic Semantics is a logical system built from *axioms* and *inference rules*
- Mainly suited to simple imperative programming languages

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Axiomatic Semantics

- Used to formally prove a property (*post-condition*) of the *state* (the values of the program variables) after the execution of program, assuming another property (*pre-condition*) of the state before execution
- Written :
 {Precondition} Program {Postcondition}
- Source of idea of *loop invariant*

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Denotational Semantics

- Construct a function \mathcal{M} assigning a mathematical meaning to each program construct
- Lambda calculus often used as the range of the meaning function
- Meaning function is compositional: meaning of construct built from meaning of parts
- Useful for proving properties of programs

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Natural Semantics

- Aka Structural Operational Semantics, aka “Big Step Semantics”
- Provide value for a program by rules and derivations, similar to type derivations
- Rule conclusions look like
$$(C, m) \Downarrow m'$$
or
$$(E, m) \Downarrow v$$

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Simple Imperative Programming Language

- $I \in \text{Identifiers}$
- $N \in \text{Numerals}$
- $B ::= \text{true} \mid \text{false} \mid B \ \& \ B \mid B \ \text{or} \ B \mid \text{not} \ B \mid E < E \mid E = E$
- $E ::= N \mid I \mid E + E \mid E * E \mid E - E \mid - E$
- $C ::= \text{skip} \mid C; C \mid I ::= E \mid \text{if } B \text{ then } C \text{ else } C \text{ fi} \mid \text{while } B \text{ do } C \text{ od}$

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Natural Semantics of Atomic Expressions

- Identifiers: $(I, m) \Downarrow m(I)$
- Numerals are values: $(N, m) \Downarrow N$
- Booleans: $(\text{true}, m) \Downarrow \text{true}$
 $(\text{false}, m) \Downarrow \text{false}$

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Booleans:

$$\frac{(B, m) \Downarrow \text{false}}{(B \& B', m) \Downarrow \text{false}} \quad \frac{(B, m) \Downarrow \text{true} \quad (B', m) \Downarrow b}{(B \& B', m) \Downarrow b}$$

$$\frac{(B, m) \Downarrow \text{true}}{(B \text{ or } B', m) \Downarrow \text{true}} \quad \frac{(B, m) \Downarrow \text{false} \quad (B', m) \Downarrow b}{(B \text{ or } B', m) \Downarrow b}$$

$$\frac{(B, m) \Downarrow \text{true}}{(\text{not } B, m) \Downarrow \text{false}} \quad \frac{(B, m) \Downarrow \text{false}}{(\text{not } B, m) \Downarrow \text{true}}$$

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Relations

$$\frac{(E, m) \Downarrow U \quad (E', m) \Downarrow V \quad U \sim V = b}{(E \sim E', m) \Downarrow b}$$

- By $U \sim V = b$, we mean does (the meaning of) the relation \sim hold on the meaning of U and V
- May be specified by a mathematical expression/equation or rules matching U and V

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Arithmetic Expressions

$$\frac{(E, m) \Downarrow U \quad (E', m) \Downarrow V \quad U \text{ op } V = N}{(E \text{ op } E', m) \Downarrow N}$$

where N is the specified value for $U \text{ op } V$

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Commands

Skip: $(\text{skip}, m) \Downarrow m$

Assignment: $\frac{(E, m) \Downarrow V}{(I ::= E, m) \Downarrow m[I \leftarrow V]}$

Sequencing: $\frac{(C, m) \Downarrow m' \quad (C', m') \Downarrow m''}{(C; C', m) \Downarrow m''}$

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If Then Else Command

$$\frac{(B, m) \Downarrow \text{true} \quad (C, m) \Downarrow m'}{(\text{if } B \text{ then } C \text{ else } C' \text{ fi}, m) \Downarrow m'}$$

$$\frac{(B, m) \Downarrow \text{false} \quad (C', m) \Downarrow m'}{(\text{if } B \text{ then } C \text{ else } C' \text{ fi}, m) \Downarrow m'}$$

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While Command

$$\frac{(B, m) \Downarrow \text{false}}{(\text{while } B \text{ do } C \text{ od}, m) \Downarrow m}$$

$$\frac{(B, m) \Downarrow \text{true} \quad (C, m) \Downarrow m' \quad (\text{while } B \text{ do } C \text{ od}, m') \Downarrow m''}{(\text{while } B \text{ do } C \text{ od}, m) \Downarrow m''}$$

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Example: If Then Else Rule

$(\text{if } x > 5 \text{ then } y := 2 + 3 \text{ else } y := 3 + 4 \text{ fi, } \{x \rightarrow 7\}) \Downarrow ?$

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Example: If Then Else Rule

$\frac{(x > 5, \{x \rightarrow 7\}) \Downarrow ?}{(\text{if } x > 5 \text{ then } y := 2 + 3 \text{ else } y := 3 + 4 \text{ fi, } \{x \rightarrow 7\}) \Downarrow ?}$

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Example: Arith Relation

$? > ? = ?$

$\frac{(x, \{x \rightarrow 7\}) \Downarrow ? \quad (5, \{x \rightarrow 7\}) \Downarrow ?}{(x > 5, \{x \rightarrow 7\}) \Downarrow ?}$
 $\frac{\quad}{(\text{if } x > 5 \text{ then } y := 2 + 3 \text{ else } y := 3 + 4 \text{ fi, } \{x \rightarrow 7\}) \Downarrow ?}$

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Example: Identifier(s)

$7 > 5 = \text{true}$

$\frac{(x, \{x \rightarrow 7\}) \Downarrow 7 \quad (5, \{x \rightarrow 7\}) \Downarrow 5}{(x > 5, \{x \rightarrow 7\}) \Downarrow ?}$
 $\frac{\quad}{(\text{if } x > 5 \text{ then } y := 2 + 3 \text{ else } y := 3 + 4 \text{ fi, } \{x \rightarrow 7\}) \Downarrow ?}$

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Example: Arith Relation

$7 > 5 = \text{true}$

$\frac{(x, \{x \rightarrow 7\}) \Downarrow 7 \quad (5, \{x \rightarrow 7\}) \Downarrow 5}{(x > 5, \{x \rightarrow 7\}) \Downarrow \text{true}}$
 $\frac{\quad}{(\text{if } x > 5 \text{ then } y := 2 + 3 \text{ else } y := 3 + 4 \text{ fi, } \{x \rightarrow 7\}) \Downarrow ?}$

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Example: If Then Else Rule

$7 > 5 = \text{true}$

$\frac{(x, \{x \rightarrow 7\}) \Downarrow 7 \quad (5, \{x \rightarrow 7\}) \Downarrow 5}{(x > 5, \{x \rightarrow 7\}) \Downarrow \text{true}}$ $\frac{(y := 2 + 3, \{x \rightarrow 7\})}{\Downarrow ?}$
 $\frac{\quad}{(\text{if } x > 5 \text{ then } y := 2 + 3 \text{ else } y := 3 + 4 \text{ fi, } \{x \rightarrow 7\}) \Downarrow ?}$

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Example: Assignment

$$\begin{array}{c}
 7 > 5 = \text{true} \\
 \frac{(x, \{x > 7\}) \Downarrow 7 \quad (5, \{x > 7\}) \Downarrow 5}{(x > 5, \{x > 7\}) \Downarrow \text{true}} \quad \frac{(2+3, \{x > 7\}) \Downarrow ?}{(y := 2 + 3, \{x > 7\})} \\
 \frac{\quad}{(\text{if } x > 5 \text{ then } y := 2 + 3 \text{ else } y := 3 + 4 \text{ fi}, \{x > 7\}) \Downarrow ?}
 \end{array}$$

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Example: Arith Op

$$\begin{array}{c}
 ? + ? = ? \\
 \frac{(2, \{x > 7\}) \Downarrow ? \quad (3, \{x > 7\}) \Downarrow ?}{(2+3, \{x > 7\}) \Downarrow ?} \\
 7 > 5 = \text{true} \\
 \frac{(x, \{x > 7\}) \Downarrow 7 \quad (5, \{x > 7\}) \Downarrow 5}{(x > 5, \{x > 7\}) \Downarrow \text{true}} \quad \frac{(y := 2 + 3, \{x > 7\})}{(y := 2 + 3, \{x > 7\})} \\
 \frac{\quad}{(\text{if } x > 5 \text{ then } y := 2 + 3 \text{ else } y := 3 + 4 \text{ fi}, \{x > 7\}) \Downarrow ?}
 \end{array}$$

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Example: Numerals

$$\begin{array}{c}
 2 + 3 = 5 \\
 \frac{(2, \{x > 7\}) \Downarrow 2 \quad (3, \{x > 7\}) \Downarrow 3}{(2+3, \{x > 7\}) \Downarrow ?} \\
 7 > 5 = \text{true} \\
 \frac{(x, \{x > 7\}) \Downarrow 7 \quad (5, \{x > 7\}) \Downarrow 5}{(x > 5, \{x > 7\}) \Downarrow \text{true}} \quad \frac{(y := 2 + 3, \{x > 7\})}{(y := 2 + 3, \{x > 7\})} \\
 \frac{\quad}{(\text{if } x > 5 \text{ then } y := 2 + 3 \text{ else } y := 3 + 4 \text{ fi}, \{x > 7\}) \Downarrow ?}
 \end{array}$$

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Example: Arith Op

$$\begin{array}{c}
 2 + 3 = 5 \\
 \frac{(2, \{x > 7\}) \Downarrow 2 \quad (3, \{x > 7\}) \Downarrow 3}{(2+3, \{x > 7\}) \Downarrow 5} \\
 7 > 5 = \text{true} \\
 \frac{(x, \{x > 7\}) \Downarrow 7 \quad (5, \{x > 7\}) \Downarrow 5}{(x > 5, \{x > 7\}) \Downarrow \text{true}} \quad \frac{(y := 2 + 3, \{x > 7\})}{(y := 2 + 3, \{x > 7\})} \\
 \frac{\quad}{(\text{if } x > 5 \text{ then } y := 2 + 3 \text{ else } y := 3 + 4 \text{ fi}, \{x > 7\}) \Downarrow ?}
 \end{array}$$

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Example: Assignment

$$\begin{array}{c}
 2 + 3 = 5 \\
 \frac{(2, \{x > 7\}) \Downarrow 2 \quad (3, \{x > 7\}) \Downarrow 3}{(2+3, \{x > 7\}) \Downarrow 5} \\
 7 > 5 = \text{true} \\
 \frac{(x, \{x > 7\}) \Downarrow 7 \quad (5, \{x > 7\}) \Downarrow 5}{(x > 5, \{x > 7\}) \Downarrow \text{true}} \quad \frac{(y := 2 + 3, \{x > 7\})}{(y := 2 + 3, \{x > 7\})} \\
 \frac{\quad}{(\text{if } x > 5 \text{ then } y := 2 + 3 \text{ else } y := 3 + 4 \text{ fi}, \{x > 7\}) \Downarrow ?}
 \end{array}$$

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Example: If Then Else Rule

$$\begin{array}{c}
 2 + 3 = 5 \\
 \frac{(2, \{x > 7\}) \Downarrow 2 \quad (3, \{x > 7\}) \Downarrow 3}{(2+3, \{x > 7\}) \Downarrow 5} \\
 7 > 5 = \text{true} \\
 \frac{(x, \{x > 7\}) \Downarrow 7 \quad (5, \{x > 7\}) \Downarrow 5}{(x > 5, \{x > 7\}) \Downarrow \text{true}} \quad \frac{(y := 2 + 3, \{x > 7\})}{(y := 2 + 3, \{x > 7\})} \\
 \frac{\quad}{(\text{if } x > 5 \text{ then } y := 2 + 3 \text{ else } y := 3 + 4 \text{ fi}, \{x > 7\}) \Downarrow \{x > 7, y > 5\}}
 \end{array}$$

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Let in Command

$$\frac{(E, m) \Downarrow v \quad (C, m[I \leftarrow v]) \Downarrow m'}{(\text{let } I = E \text{ in } C, m) \Downarrow m'}$$

Where $m''(y) = m'(y)$ for $y \neq I$ and $m''(I) = m(I)$ if $m(I)$ is defined, and $m''(I)$ is undefined otherwise

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Example

$$\frac{\frac{(x, \{x \rightarrow 5\}) \Downarrow 5 \quad (3, \{x \rightarrow 5\}) \Downarrow 3}{(x+3, \{x \rightarrow 5\}) \Downarrow 8}}{(5, \{x \rightarrow 17\}) \Downarrow 5 \quad (x := x+3, \{x \rightarrow 5\}) \Downarrow \{x \rightarrow 8\}}}{(\text{let } x = 5 \text{ in } (x := x+3), \{x \rightarrow 17\}) \Downarrow ?}$$

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Example

$$\frac{\frac{(x, \{x \rightarrow 5\}) \Downarrow 5 \quad (3, \{x \rightarrow 5\}) \Downarrow 3}{(x+3, \{x \rightarrow 5\}) \Downarrow 8}}{(5, \{x \rightarrow 17\}) \Downarrow 5 \quad (x := x+3, \{x \rightarrow 5\}) \Downarrow \{x \rightarrow 8\}}}{(\text{let } x = 5 \text{ in } (x := x+3), \{x \rightarrow 17\}) \Downarrow \{x \rightarrow 17\}}$$

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Comment

- Simple Imperative Programming Language introduces variables *implicitly* through assignment
- The let-in command introduces scoped variables *explicitly*
- Clash of constructs apparent in awkward semantics

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Interpretation Versus Compilation

- A **compiler** from language L1 to language L2 is a program that takes an L1 program and for each piece of code in L1 generates a piece of code in L2 of same meaning
- An **interpreter** of L1 in L2 is an L2 program that executes the meaning of a given L1 program
- Compiler would examine the body of a loop once; an interpreter would examine it every time the loop was executed

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Interpreter

- An *Interpreter* represents the operational semantics of a language L1 (source language) in the language of implementation L2 (target language)
- Built incrementally
 - Start with literals
 - Variables
 - Primitive operations
 - Evaluation of expressions
 - Evaluation of commands/declarations

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Interpreter

- Takes abstract syntax trees as input
 - In simple cases could be just strings
- One procedure for each syntactic category (nonterminal)
 - eg one for expressions, another for commands
- If Natural semantics used, tells how to compute final value from code
- If Transition semantics used, tells how to compute next “state”
 - To get final value, put in a loop

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Natural Semantics Example

- $\text{compute_exp}(\text{Var}(v), m) = \text{look_up } v \text{ } m$
- $\text{compute_exp}(\text{Int}(n), _) = \text{Num}(n)$
- ...
- $\text{compute_com}(\text{IfExp}(b, c1, c2), m) =$
if $\text{compute_exp}(b, m) = \text{Bool}(\text{true})$
then $\text{compute_com}(c1, m)$
else $\text{compute_com}(c2, m)$

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Natural Semantics Example

- $\text{compute_com}(\text{While}(b, c), m) =$
if $\text{compute_exp}(b, m) = \text{Bool}(\text{false})$
then m
else compute_com
 $(\text{While}(b, c), \text{compute_com}(c, m))$
- May fail to terminate - exceed stack limits
- Returns no useful information then

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