

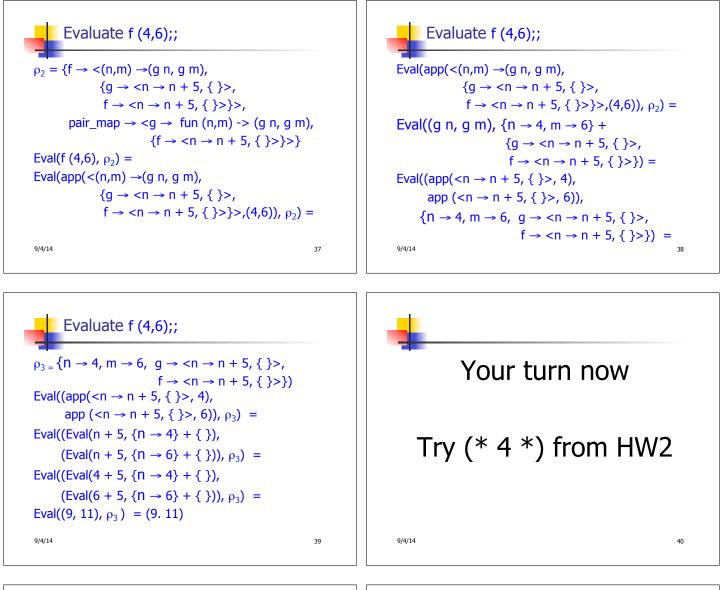


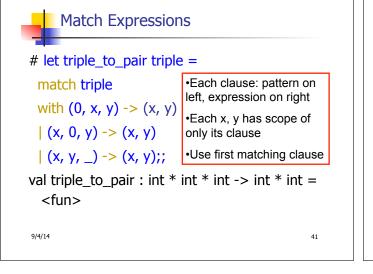


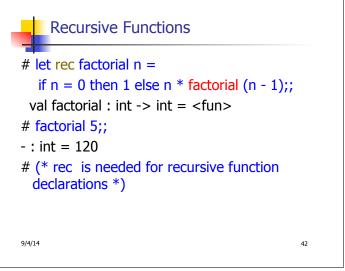
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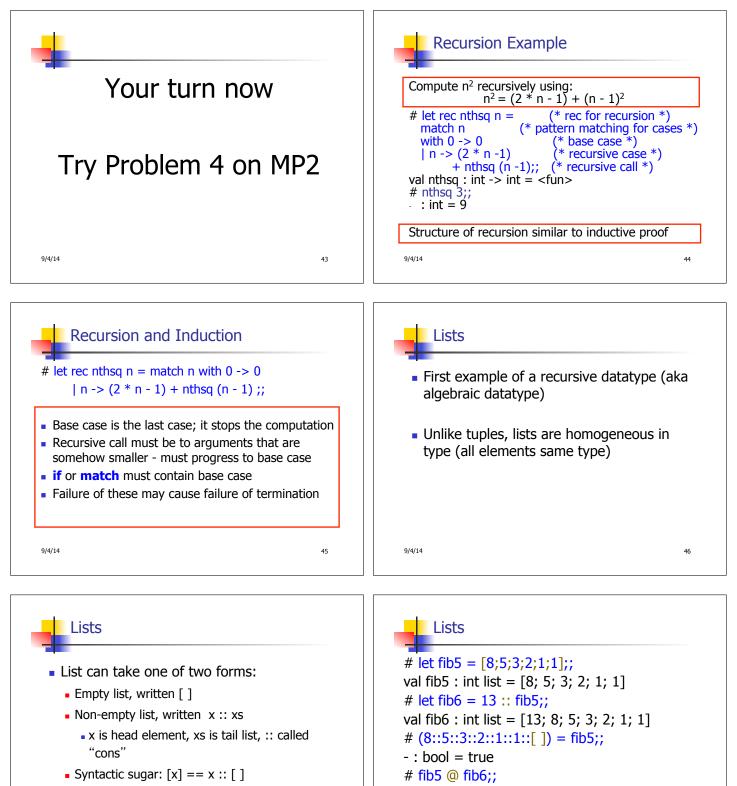
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[x1; x2; ...; xn] == x1 :: x2 :: ... :: xn :: []

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1]

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- : int list = [8; 5; 3; 2; 1; 1; 13; 8; 5; 3; 2; 1;



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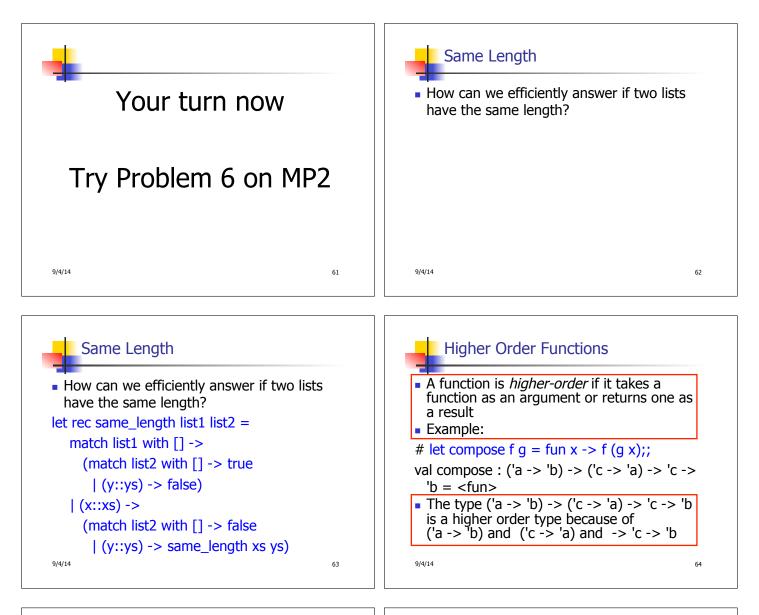
54

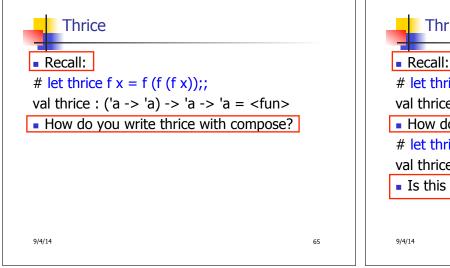
53

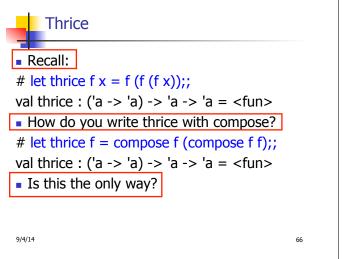
- : string list = ["there"; "there"; "hi"; "hi"]

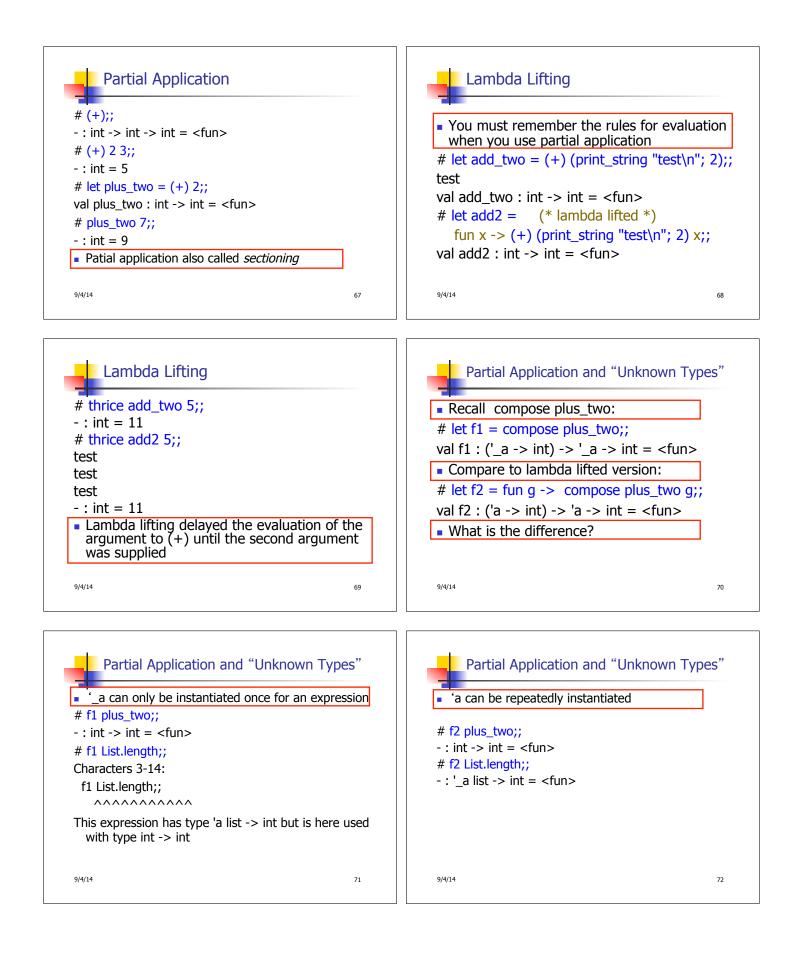
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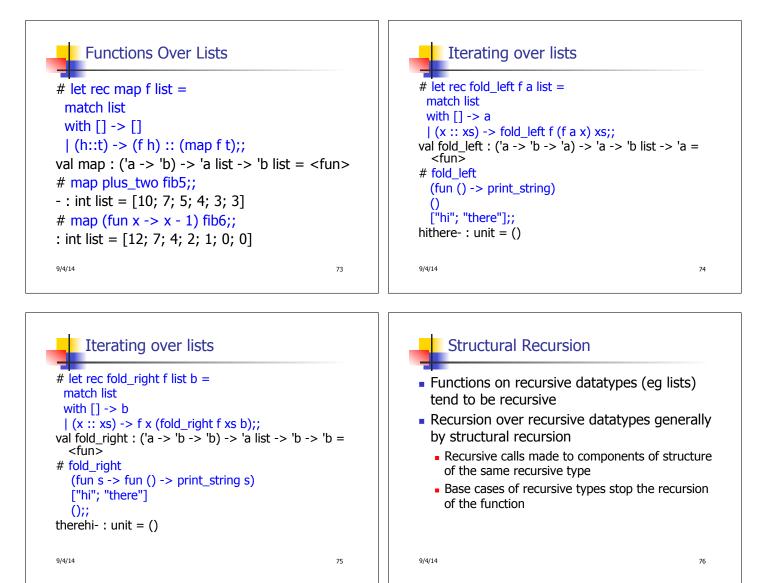


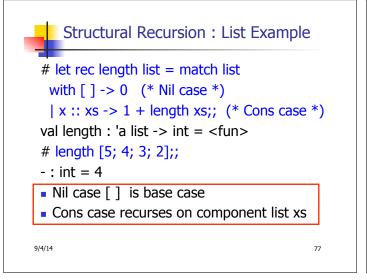












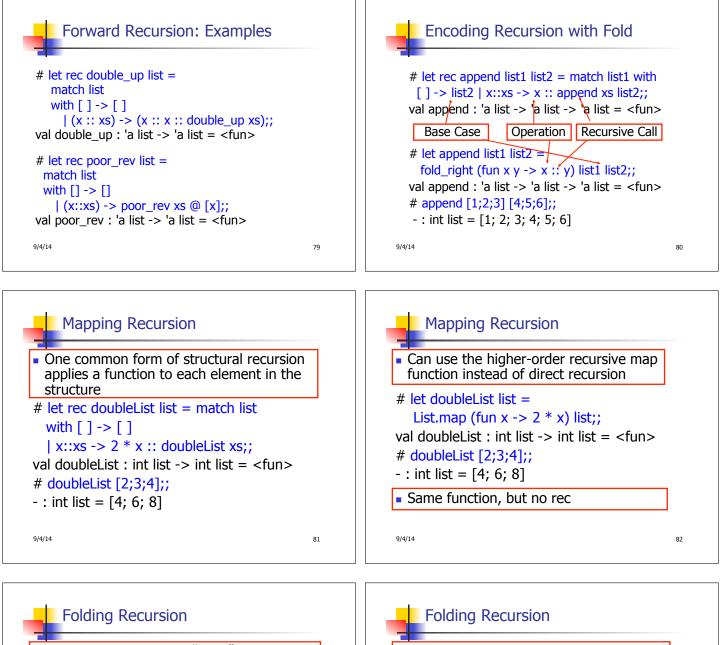
Forward Recursion

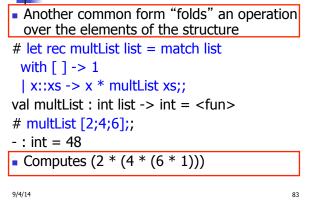
- In Structural Recursion, split input into components and (eventually) recurse
- Forward Recursion form of Structural Recursion
- In forward recursion, first call the function recursively on all recursive components, and then build final result from partial results

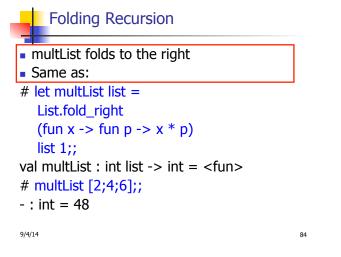
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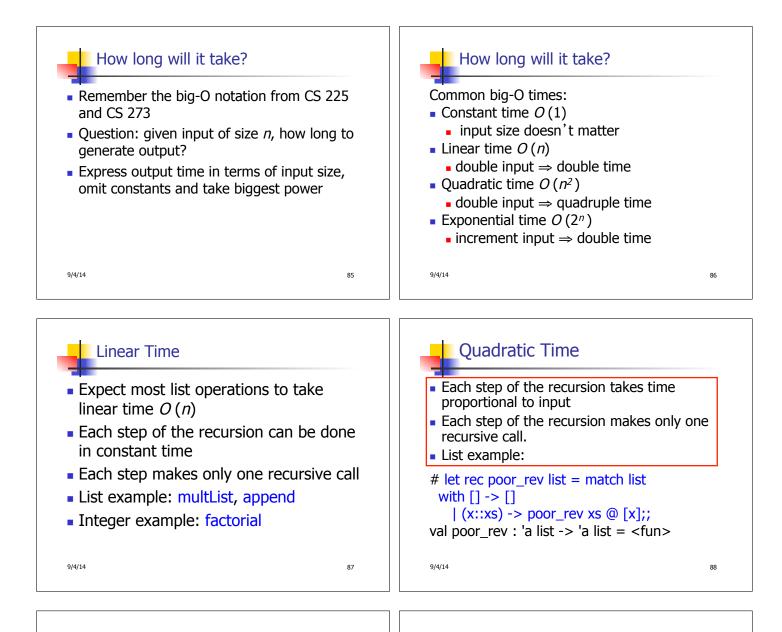
 Wait until whole structure has been traversed to start building answer

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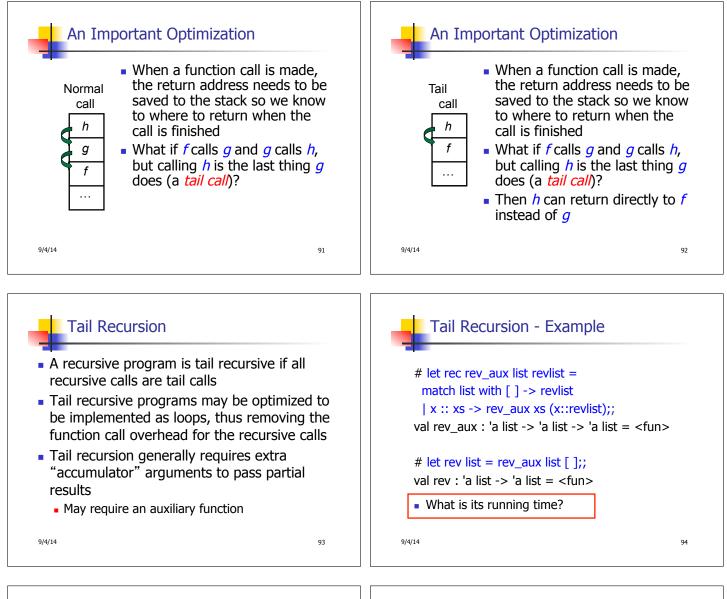


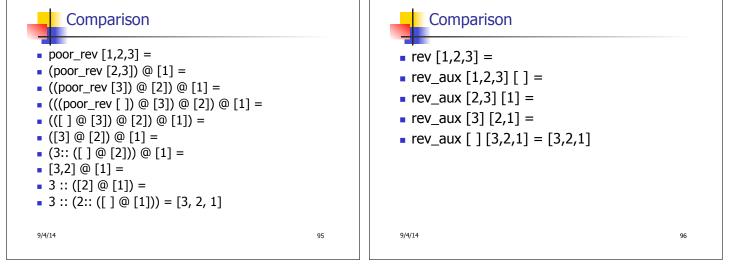
Exponential running time

- Hideous running times on input of any size
- Each step of recursion takes constant time
- Each recursion makes two recursive calls
- Easy to write naïve code that is exponential for functions that can be linear

```
# Exponential running time
# let rec naiveFib n = match n
with 0 -> 0
| 1 -> 1
|_-> naiveFib (n-1) + naiveFib (n-2);;
val naiveFib : int -> int = <fun>
```

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Folding

- Can replace recursion by fold_right in any forward primitive recursive definition
 - Primitive recursive means it only recurses on immediate subcomponents of recursive data structure
- Can replace recursion by fold_left in any tail primitive recursive definition

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