MP 10 – An Evaluator for MicroML

CS 421 – Fall 2012 Revision 1.1

Assigned November 13, 2012 **Due** November 29, 2012 23:59 **Extension** 48 hours (20% penalty)

1 Change Log

- **1.2** Changed the due date to Thursday, 29 November 2012.
- $\textbf{1.1 Corrected Problem 12 to require } (\texttt{val rec} \ f \ x = e \ , \ m) \Downarrow ([(\texttt{Some} \ f, RecVarVal(x, e, m))], \{f \rightarrow RecVarVal(x, e, m)\}).$
- 1.0 Initial Release.

2 Overview

Previously, you created a lexer, a parser, and a type inferencer for MicroML. Finally, your hard work will pay off – it is time to create an evaluator for MicroML programs. Lexing, parsing, and type inferencing will be taken care of automatically (you have already implemented these parts in previous MPs.) Your evaluator can assume that its input is correctly typed.

Your evaluator will be responsible for evaluating two kinds of things: declarations, and expressions. At top level, your evaluator will be called on a declaration or an expression with an empty memory. It will recurse on the parts, eventually returning the binding.

3 Types

For this assignment, one should note the difference between expressions and values. An expression is a syntax tree, like 2 + (4*3) or (3 < 4), whereas a value is a single object, like 14 or true. A value is the result of evaluating an expression. Note that closures are values representing functions.

Recall that we represent MicroML programs with the following OCaml types defined in Mp10common:

```
(* expressions for MicroML *)
type const =
     BoolConst of bool
                               (* for true and false *)
                               (* 0,1,2, ... *)
   | IntConst of int
   | RealConst of float
                              (* 2.1, 3.0, 5.975, ... *)
   | StringConst of string
                               (* "a", "hi there", ... *)
   | NilConst
                               (* [ ] *)
   | UnitConst
                               (* ( ) *)
type mon_op =
     IntNegOp
                   (* integer negation *)
   | HdOp
                   (* hd *)
   qOlT |
                   (* tl *)
                   (* fst *)
   | FstOp
   | SndOp
                   (* snd *)
```

```
| PrintStringOp (* print_string *)
type bin op =
    IntPlusOp
                      (* _ + _ *)
   | IntMinusOp
                      (* _ - _ *)
   | IntTimesOp
                     (* _ * _ *)
   | IntDivOp
                     (* _ / _ *)
   | RealPlusOp
                     (* _ +. _ *)
   | RealMinusOp
                     (* _ -. _ *)
   | RealTimesOp
                     (* _ *. _ *)
   | RealDivOp
                     (* _ /. _ *)
                     (* _ ^
   | ConcatOp
                     (* _ :: _ *)
  | ConsOp
   | CommaOp
                     (* _ , _ *)
                     (* _ = _ *)
   | EqOp
   | GreaterOp
type dec =
                                    (* val x = exp *)
    Val of string * exp
   | Rec of string * string * exp
                                  (* val rec f x = exp *)
   | Seq of dec * dec
                                    (* dec1 dec2 *)
   | Local of dec * dec
                                    (* local dec1 in dec2 end *)
and exp =
  | VarExp of string
                                        (* variables *)
   | ConstExp of const
                                        (* constants *)
   | MonOpAppExp of mon_op * exp
                                        (* % exp1
                   where % is a builtin monadic operator *)
   | BinOpAppExp of bin_op * exp * exp (* exp1 % exp2
                   where % is a builtin binary operator *)
   | IfExp of exp * exp * exp
                                       (* if exp1 then exp2 else exp3 *)
   | AppExp of exp * exp
                                        (* exp1 exp2 *)
   | FnExp of string * exp
                                        (* fn x => x *)
                                        (* let dec in exp end *)
   | LetExp of dec * exp
   | RaiseExp of exp
                                         (* raise e *)
   | HandleExp of (exp * int option * exp * (int option * exp) list)
                          (* e handle i => e0 | j => e1 | ... | k => en *)
```

With these, we form a MicroML abstract syntax tree. A MicroML AST will be the *input* to your evaluator. The *output* given by evaluating an AST expression is a value type. The value type is defined in Mp10common:

```
type value =
    UnitVal
| BoolVal of bool
| IntVal of int
| RealVal of float
| StringVal of string
| PairVal of value * value
| ListVal of value list
| ClosureVal of string * exp * value env
(* | RecVarVal of exp * exp env * value env
| RecVarVal of string * exp * value env
```

Values can also be stored in memory. Memory serves as both *input* to your evaluator in general, and *output* from your evaluator when evaluating declarations. For example, one evaluates a declaration starting from some initial

memory, and a list of bindings to be printed by the interpreter and an incremental memory are returned.

We will represent our memory using a value env. That is, we will use the env type from previous MPs to hold value types.

Recall from MP6 the use of the 'a env type defined in Mp10common:

```
(* environments *)
type 'a env = (string * 'a) list
```

You can interact with the env type by using functions defined in Mp10common:

```
val empty_env : 'a env = []
val make_env : string -> 'a -> 'a env = <fun>
val lookup_env : 'a env -> string -> 'a option = <fun>
val sum_env : 'a env -> 'a env -> 'a env = <fun>
val ins_env : 'a env -> string -> 'a -> 'a env = <fun>
```

4 Compiling, etc...

For this MP, you will only have to modify **mp10-skeleton.ml** (first convert it to **mp10.ml**), adding the functions requested. To test your code, type make and the three needed executables will be built: micromlint, micromlintSol and grader. The first two are explained below. grader checks your implementation against the solution for a fixed set of test cases as given in the tests file.

You may also work interactively with your code in OCaml. To facilitate your doing this, and because there are more files than usual to load than usual, we have included in mpl0grader a file .ocamlinit that is executed by ocaml every time it is started in the directory mpl0grader. The contents of the file are:

```
#load "mp10common.cmo";;
#load "micromlparse.cmo";;
#load "micromllex.cmo";;
#load "solution.cmo";;
open Mp10common;;
#use "mp10.ml";;
```

4.1 Running MicroML

The given Makefile builds executables called micromlint and micromlintSol. The first is an executable for an interactive loop for the evaluator built from your solution to the assignment and the second is built from the standard solution. If you run ./micromlint or ./micromlintSol, you will get an interactive screen, much like the OCaml interactive screen. You can type in MicroML declarations (followed by a semicolon), and they will be evaluated, and the resulting binding will be displayed.

At the command prompt, the programs will be evaluated (or fail evaluation) starting from the initial memory, which is empty. Each time, if evaluation is successful, the resulting memory will be displayed. Note that a program can fail at any of several stages: lexing, parsing, type inferencing, or evaluation itself. Evaluation itself will tend to fail until you have solved at least some of the problems to come.

Part 1

Problems in Part 1 of this MP are mandatory for all students. Part 2 is mandatory for only grad students. Undergrads may submit a solution for Part 2 for extra credit. Part 1 does not contain any exception handling. Part 2 will cover exceptions.

5 Problems

These problems ask you to create an evaluator for MicroML by writing the functions eval_dec, and eval_exp as specified. In addition, you will be asked to implement the functions const_to_val, monOpApply and binOpApply.

For each problem, you should refer to the list of rules given as part of the problem. The rules specify how evaluation should be carried out, using natural semantics. Natural semantics were covered in class; see the lecture notes for details.

Here are some guidelines:

- eval_dec takes a declaration and a memory, and returns a pair of a mapping from string options to values, and memory. Its type is dec * value env -> (string option * value) list * value env.
- eval_exp takes an expression and a memory, and returns a value. Its type is exp * value env -> value.

The problems are ordered such that simpler and more fundamental concepts come first. For this reason, it is recommended that you solve the problems in the order given. Doing so may make it easier for you to test your solution before it is completed.

Here is a key to interpreting the rules:

```
d= declaration m= memory stored as a value env e= expression v= value x= identifier/variable t= constant b= list of bound values to be printed by the interpreter rd= recursive definitions stored as an exp env tl= tail of a list
```

As mentioned, you should test your code in the executable MicroML environment. The problem statements that follow include some examples. However, the problem statements also contain test cases that can be used to test your implementation in the OCaml environment.

1. Constants (8 pts)

Extend eval_exp (exp, m) to handle constants (i.e. integers, bools, real numbers, strings, nil, and unit). For this question you will need to implement const_to_val: const -> value. This function takes a constant and returns the corresponding value.

$$(t,m) \downarrow const_to_val(t)$$

In the MicroML environment,

```
> 2;
result:
val it = 2
```

A sample test case for the OCaml environment:

```
# eval_exp (ConstExp(IntConst 2), []);;
- : Mp10common.value = IntVal 2
```

2. Val Declarations (6 pts)

Extend eval_dec (dec, m) to handle val-declarations. eval_dec takes a declaration and a memory, and returns a list of bindings introduced by the declaration, which will be printed by the interpreter, together with the memory containing only those bindings introduced by the declaration. If _ is encountered, we want to print out the evaluation, but not update the memory, We do this by binding the value to None in the list to be printed, but we do not include the binding in the memory. This is represented by the second rule.

$$\frac{(e,m) \Downarrow v}{(\mathsf{val}\; x = e\;,\; m) \Downarrow ([(\mathsf{Some}\; x,v)], \{x \to v\})} \qquad \frac{(e,m) \Downarrow v}{(\mathsf{val}\; _ = e\;,\; m) \Downarrow ([(\mathsf{None}\;,v)], \{\;\})}$$

In the MicroML environment,

```
> val x = 4;
result:
val x = 4
> val _ = 4;
result:
val _ = 4
```

A sample test case for the OCaml environment.

```
# eval_dec (Val ("x", ConstExp (IntConst 4)), []);;
- : (string option * Mp10common.value) list * Mp10common.value Mp10common.env
= ([(Some "x", IntVal 4)], [("x", IntVal 4)])
# eval_dec (Val ("", ConstExp (IntConst 4)), []);;
- : (string option * Mp10common.value) list * Mp10common.value Mp10common.env
= ([(None, IntVal 4)], [])
```

3. **Identifiers (no recursion)** (5 pts)

Extend eval_exp (exp, m) to handle identifiers (i.e. variables) that are not recursive. These are identifiers in m which are not equal to $RecVarVal\langle ... \rangle$, (recursive identifiers are handled later).

$$\frac{m(x) = v \quad \forall e \ rd \ m'. \ v \neq RecVarVal(e, rd, m')}{(x, m) \Downarrow v}$$

Here is a sample test case.

```
# eval_exp (VarExp "x", [("x", IntVal 2)]);;
- : Mp10common.value = IntVal 2
```

In the MicroML environment, if you have previously successfully done Problem 2, you can test this problem with:

```
> x;
result:
val it = 4
```

4. Functions (5 pts)

Extend eval_exp (exp, m) to handle functions. You will need to return a ClosureVal represented by $\langle x \to e, m \rangle$ in the rule below.

$$\frac{}{(\operatorname{fn} x => e, m) \Downarrow \langle x \to e, m \rangle}$$

A sample test case.

```
# eval_exp (FnExp ("x", VarExp "x"), []);;
- : Mp10common.value = ClosureVal ("x", VarExp "x", [])
```

In the MicroML environment.

```
> fn x => x;
result:
val it = <some closure>
```

5. Function application (6 pts)

Extend eval_exp (exp, m) to handle function application.

$$\frac{(e_1, m) \Downarrow \langle x \to e', m' \rangle \quad (e_2, m) \Downarrow v' \quad (e', \{x \to v'\} + m') \Downarrow v}{(e_1 e_2, m) \Downarrow v}$$

A sample test case.

```
# eval_exp (AppExp (FnExp ("x", VarExp "x"), ConstExp (IntConst 7)), []);;
- : Mp10common.value = IntVal 7
```

In the MicroML environment.

```
> (fn x => x) 7;
result:
val it = 7
```

6. Monadic Operator Application (8 pts)

Extend eval_exp (exp, m) to handle application of monadic operators ~, hd, tl, fst, snd and print_string. For this question, you need to implement the function monOpApply: mon_op -> value -> value following the table below.

(Hint: Check how we represent lists and pairs with the value type)

operator	argument	operation
hd	a list	return the head of the list
tl	a list	return the tail of the list
fst	a pair	return the first element of the pair
snd	a pair	return the second element of the pair
~	an integer	return the negated integer
print_string	a string	print the string to std_out, return unit

$$\frac{(e_2, m) \Downarrow v \quad monOpApply(mon, v) = v'}{(mon\ e, m) \Downarrow v'}$$

where mon is a monadic constant function value.

Note: For now, in monOpApply, you should raise an OCaml exception if hd or tl is applied to an empty list. This will change in Part 2.

A sample test case in the MicroML interpreter:

```
> ~2;
result:
val it = -2
```

A sample test case in the OCaml environment:

```
# monOpApply IntNegOp (IntVal 2);;
- : Mp10common.value = IntVal (-2)
# eval_exp (MonOpAppExp(IntNegOp, ConstExp (IntConst 2)), []);;
- : Mp10common.value = IntVal (-2)
```

7. **Binary Operators** (8 pts)

Extend eval_exp (exp, m) to handle the application of binary operators. For this question, you need to implement the binOpApply: $bin_op \rightarrow value \rightarrow value \rightarrow value$ function. The table below gives the outputs for given inputs to binOpApply.

operator	arguments	operation
"+"	Two integers	Addition
"-"	Two integers	Subtraction
" * "	Two integers	Multiplication
"/"	Two integers	Division
"+."	Two floating numbers	Addition
""	Two floating numbers	Subtraction
"*."	Two floating numbers	Multiplication
"/."	Two floating numbers	Division
п^п	Two strings	Concatenation
"::"	A value and a list	Cons
","	Two values	Pairing
"="	Two values	Equality comparison
">"	Two values	Greater than

$$\frac{(e_1,m) \Downarrow v_1 \quad (e_2,m) \Downarrow v_2 \quad binOpApply(\oplus, v_1, v_2) = v}{(e_1 \oplus e_2, m) \Downarrow v}$$

Note: For equality and other comparison operators, use the overloaded equality and comparison operators of OCaml directly on the objects of type value.

A sample test case.

In the MicroML environment, you can test this problem with:

```
> 3 + 4;
result:
val it = 7
```

8. **If constructs** (5 pts)

Extend eval_exp (exp, m) to handle if constructs.

A sample test case.

result: val it = 1

9. Let-in expression (6 pts)

Extend eval_exp (exp, m) to handle let-in expressions.

$$\frac{(d,m) \Downarrow (b,m') \quad (e,m'+m) \Downarrow v}{(\text{let } d \text{ in } e \text{ end }, m) \Downarrow v}$$

A sample test case.

```
# eval_exp (LetExp (Val ("y", ConstExp (IntConst 5)), VarExp "y"), []);;
- : Mp10common.value = IntVal 5
```

In the MicroML environment,

```
> let val y = 5 in y end;
result:
val it = 5
```

10. **Sequenced Declarations** (6 pts)

Extend eval_dec (dec, m) to handle sequenced declarations.

$$\frac{(d_1, m) \Downarrow (b1, m') \quad (d_2, m' + m) \Downarrow (b2, m'')}{(d_1 d_2, m) \Downarrow (b2 @ b1, m'' + m')}$$

A sample test case.

In the MicroML environment,

```
> val x = 4 val y = "hi";
result:
val x = 4
val y = "hi"
```

11. Local Declarations (5 pts)

Extend eval_dec (dec, m) to handle local declarations.

$$\frac{(d_1,m) \Downarrow (b1,m') \quad (d_2,m'+m) \Downarrow (b2,m'')}{(\texttt{local}\ d_1\ \texttt{in}\ d_2\ \texttt{end}\ ,m) \Downarrow (b2,m'')}$$

A sample test case.

In the MicroML environment,

```
> local val x = 3 in val y = (x, 3.14) end;
result:
val y = (3, 3.14)
```

12. **Recursive Declarations** (18 pts)

Extend eval_dec (dec, m) to handle recursive declarations. Recursive declarations are restricted defining functions. Within there bodies, they are allowed to be referenced. A non-recursive function declaration evaluates to a closure containing the environment that was in effect before the function declaration was made. Variables in the body aquire their meaning from the formal parameter or from this stored environment. In the case of a recursive function declaration, we have the problem that we also may have the variable naming this function used in its body. The environment in effect before the recursive declaration does not have this variable in it. We need to create an environment that has a value for the recursive variable, but that value needs to be a closure that contains the environment we are trying to create. We solve this problem by recording a "recursive variable value" for the variable in the environment in the closure for its value instead of its actual value. This "recursive variable value" basically is a prescription for how to build the needed value, *i.e.*, the needed closure, whenever we call the variable. Since this "recursive variable value" is a prescription for building a closure, not surprising it will have all the components of a closure, but since it is a prescription, it has a different constructor. RecVarVal(x, e, m) is the value we will associate with recursive function variable, keeps track of its formal parameter, its bound expression e, and a memory m in effect when the recursive declaration was made.

```
(val rec f(x) = e(x), m) \downarrow ([(Some f(x) = e(x)), \{f(x) = e(x)], \{f(x) = e(x)], \{f(x) = e(x)]
A sample test case.
# eval_dec (Rec ("even", "x",
IfExp (BinOpAppExp (EqOp, VarExp "x", ConstExp (IntConst 0)),
  ConstExp (BoolConst true),
  IfExp (BinOpAppExp (EqOp, VarExp "x", ConstExp (IntConst 1)),
   ConstExp (BoolConst false),
   AppExp (VarExp "even",
    BinOpAppExp (IntMinusOp, VarExp "x", ConstExp (IntConst 2)))))), []);;
- : (string option * Mp10common.value) list * Mp10common.value Mp10common.env =
([(Some "even",
   RecVarVal ("even", "x",
    IfExp (BinOpAppExp (EqOp, VarExp "x", ConstExp (IntConst 0)),
     ConstExp (BoolConst true),
     IfExp (BinOpAppExp (EqOp, VarExp "x", ConstExp (IntConst 1)),
      ConstExp (BoolConst false),
      AppExp (VarExp "even",
       BinOpAppExp (IntMinusOp, VarExp "x", ConstExp (IntConst 2))))),
    []))],
 [("even",
   RecVarVal ("even", "x",
    IfExp (BinOpAppExp (EqOp, VarExp "x", ConstExp (IntConst 0)),
     ConstExp (BoolConst true),
     IfExp (BinOpAppExp (EqOp, VarExp "x", ConstExp (IntConst 1)),
      ConstExp (BoolConst false),
      AppExp (VarExp "even",
       BinOpAppExp (IntMinusOp, VarExp "x", ConstExp (IntConst 2)))),
    []))])
In the MicroML environment.
> val rec even x = if x = 0 then true else if x = 1 then false else even (x - 2);
result:
val even = <some recvar>
```

13. **Recursive identifiers** (12 pts)

Extend eval_exp (exp, m) to handle recursive identifiers. These are identifiers that evaluate to RecVarVal(f, x, e, m') for some expression e, and a memory m'.

$$\frac{m(f) = RecVarVal(x, e, m')}{(f, m) \Downarrow \langle x \rightarrow e, \{f \rightarrow RecVarVal(x, e, m')\} + m' \rangle}$$

In the MicroML environment, once you have done Problem 12, you can try:

```
> val rec f x = if x = 0 then 1 else x * f (x - 1) val y = f 3 ; result: val f = <some recvar> val y = 6
```

Part 2

This part is mandatory for grad students. It is extra credit for undergrads.

Part 1 simply ignored exceptions. In this section we include them in our language. First of all, we use the value constructor Exp of int in our value type to represent the raising of an exception.

An exception propagates through the evaluates. That is, if a subexpression of an expression evaluates to an exception, then the main expression also evaluates to the exception without evaluating the remaining subexpressions. We need to update our evaluation rules to handle this situation:

Expression Rules

Constants

$$(t,m) \downarrow const_to_val(t)$$

Variables

$$\frac{m(x) = v \quad \forall x, \ e', \ m'. \ v \neq RecVarVal(y, e', m')}{(x, m) \Downarrow v}$$

If Expression

$$\underbrace{(e_1,m) \Downarrow true \quad (e_2,m) \Downarrow v}_{ \text{if } e_1 \text{ then } e_2 \text{ else } e_3 \Downarrow v} \qquad \underbrace{(e_1,m) \Downarrow false \quad (e_3,m) \Downarrow v}_{ \text{if } e_1 \text{ then } e_2 \text{ else } e_3 \Downarrow v}$$

$$(e_1,m) \Downarrow Exn(i)$$

if e_1 then e_2 else $e_3 \Downarrow Exn(i)$

Application

$$\frac{(e_1, m) \Downarrow \langle x \to e', m' \rangle \quad (e_2, m) \Downarrow v' \quad \forall i. \ v' \neq Exn(i) \quad (e', \{x \to v'\} + m') \Downarrow v}{(e_1 e_2, m) \Downarrow v}$$

$$\frac{(e_1, m) \Downarrow Exn(i)}{(e_1 e_2, m) \Downarrow Exn(i)} \quad \frac{(e_1, m) \Downarrow v \quad \forall j. \ v' \neq Exn(j) \quad (e_2, m) \Downarrow Exn(i)}{(e_1 e_2, m) \Downarrow Exn(i)}$$

Monadic Operator Application

$$\frac{(e,m) \Downarrow v \quad \forall i. \ v \neq Exn(i) \quad monOpApply(unc,v) = v'}{(mon_op \ e,m) \Downarrow v'} \qquad \frac{(e_1,m) \Downarrow Exn(i)}{(mon_op \ e_2,m) \Downarrow Exn(i)}$$

Binary Operator Application

$$\frac{(e_1,m) \Downarrow v_1 \quad (e_2,m) \Downarrow v_2 \quad \forall i. \ v_1 \neq Exn(i) \land v_2 \neq Exn(i) \quad binOpApply(\oplus, v_1, v_2) = v}{(e_1 \oplus e_2, m) \Downarrow v}$$

$$\frac{(e_1,m) \Downarrow Exn(i)}{(e_1 \oplus e_2, m) \Downarrow Exn(i)} \quad \frac{(e_1,m) \Downarrow v \quad \forall i. \ v \neq Exn(i) \quad (e_2,m) \Downarrow Exn(j)}{(e_1 \oplus e_2, m) \Downarrow Exn(j)}$$

Functions

$$\overline{(\operatorname{fn} x => e, m) \Downarrow \langle x \to e, m \rangle}$$

Let Expression

$$\frac{(d,m) \Downarrow (b,m') \quad \forall i \; tl. \; b_1 \neq (\text{None} \; , Exn(i)) :: tl \quad (e,m'+m) \Downarrow v}{(\text{let} \; d \; \text{in} \; e \; \text{end} \; , m) \Downarrow v}$$

$$\frac{(d,m) \Downarrow ((\text{None}, Exn(i) :: tl), m')}{(\text{let } d \text{ in } e \text{ end }, m) \Downarrow Exn(i)}$$

Recursive Identifiers

$$\frac{m(f) = RecVarVal(x, e, m')}{(f, m) \Downarrow \langle x \rightarrow e, \{f \rightarrow RecVarVal(x, e, m')\} + m' \rangle}$$

Declaration Rules

Val Declaration

$$\frac{(e,m) \Downarrow v \quad \forall i. \ v \neq Exn(i)}{(\text{val } x = e \ , \ m) \Downarrow ([(\text{Some } x,v)], \{x \rightarrow v\})} \qquad \frac{(e,m) \Downarrow v}{(\text{val } _ = e \ , \ m) \Downarrow ([(\text{None },v)], \{\ \})}$$

$$\frac{(e,m) \Downarrow Exn(i)}{(\mathsf{val}\; x = e\;,\; m) \Downarrow ([(\mathsf{None}\;, Exn(i))], \{\;\})}$$

Seq Declaration

$$\frac{(d_1,m) \Downarrow (((\operatorname{None}, Exn(i)) :: tl), m')}{(d_1d_2,m) \Downarrow ((\operatorname{None}, Exn(i)) :: tl, m')}$$

$$\frac{(d_1,m) \Downarrow (b1,m') \quad (d_2,m') \Downarrow (b2,m'') \quad \forall i.\ b1 \neq (\texttt{None}\ , Exn(i)) :: tl}{(d_1d_2,m) \Downarrow (b2 @ b1,m''+m')}$$

Recursive Declarations

$$\frac{m(f) = RecVarVal(x, e, m')}{(f, m) \Downarrow \langle x \rightarrow e, \{f \rightarrow RecVarVal(x, e, m')\} + m' \rangle}$$

Local Declaration

$$\frac{(d_1,m) \Downarrow (b1,m') \quad \forall i \ tl. \ b_1 \neq (\texttt{None} \ , Exn(i)) :: tl \quad (d_2,m'+m) \Downarrow (b2,m'')}{(\texttt{local} \ d_1 \ \texttt{in} \ d_2 \ \texttt{end} \ , m) \Downarrow (b2,m'')}$$

$$\frac{(d_1,m) \Downarrow ((\texttt{None} \ , Exn(i)) :: tl,m')}{(\texttt{local} \ d_1 \ \texttt{in} \ d_2 \ \texttt{end} \ , m) \Downarrow ([(\texttt{None} \ , Exn(i))], \{\ \})}$$

6 Problems

14. (20 pts)

Update your implementation to incorporate exceptions in the evaluator. Follow the rules given above.

15. Explicit exceptions (5 pts)

Extend eval_exp (exp, m) to handle explicit exception raising.

$$\frac{(e,m) \Downarrow n}{(\mathit{raise}\, e,m) \Downarrow Exn(n)} \qquad \frac{(e,m) \Downarrow Exn(i)}{(\mathit{raise}\, e,m) \Downarrow Exn(i)}$$

A sample test case.

result:

```
# eval_exp(RaiseExp (ConstExp (IntConst 1)),[]);;
- : Mp10common.value = Exn 1
In the MicroML environment,
> raise 1;
```

16. **Implicit exceptions** (4 pts)

val = (Exn 1)

Modify binOpApply and monOpApply to return an exception if an unexpected error occurs. In such case, Exn(0) should be returned. Below are the cases you need to cover:

- An attempt to divide by zero (Both integer and real division).
- An attempt to get the head of an empty list.
- An attempt to get the tail of an empty list.

A sample test case:

In the MicroML interpreter:

```
> 4/0;
result:
val _ = (Exn 0)
```

17. Handle expressions (10 pts)

Extend eval_exp (exp, m) to handle handle expressions.

$$\frac{(e,m) \Downarrow v \quad \forall j. \ v \neq Exn(j)}{((e \text{ handle } n_1 => e_1 \ | \ \dots \ | \ n_p => e_p), m) \Downarrow v}$$

$$\frac{(e,m) \Downarrow Exn(j) \qquad \forall k \leq p. \; (n_k \neq j \; \text{and} \; n_k \neq _)}{((e \; \text{handle} \; n_1 => e_1 \; | \; \ldots \; | \; n_p => e_p), m) \Downarrow Exn(j)}$$

$$\frac{(e,m) \Downarrow Exn(j) \quad (n_i = j \; \text{or} \; n_i = _) \quad \forall k < i. \; (n_k \neq j \; \text{and} \; n_k \neq _) \quad (e_i,m) \Downarrow v}{((e \; \text{handle} \; n_1 => e_1 \; | \; \ldots \; | \; n_p => e_p), m) \Downarrow v}$$

Sample code in OCaml would be:

Final Remark: Please add numerous test cases to the test suite. Try to cover obscure cases.