Orthographic Projection

CS 418: Interactive Computer Graphics

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Projections

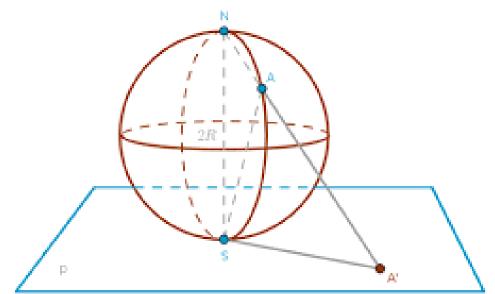
In computer graphics, eventually we need to move from 3D space to 2D space

More accurately: from 4D homogeneous coordinates to 3D homogeneous coordinates

A projection

is a transformation that maps from a high-dimensional space into a lower-dimensional space.

We will look at some common projections...and then we will discuss projection within WebGL



Planar Geometric Projections

Standard projections project onto a plane

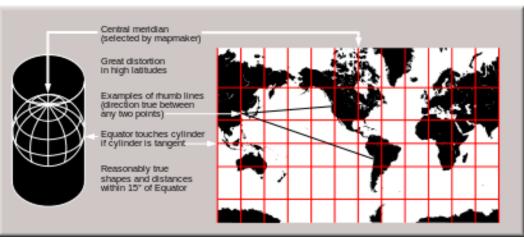
Projectors are lines that either

- converge at a center of projection
- are parallel

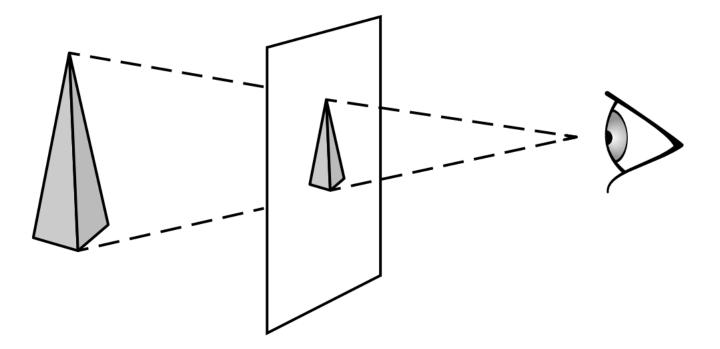
Such projections preserve lines

• but not necessarily angles

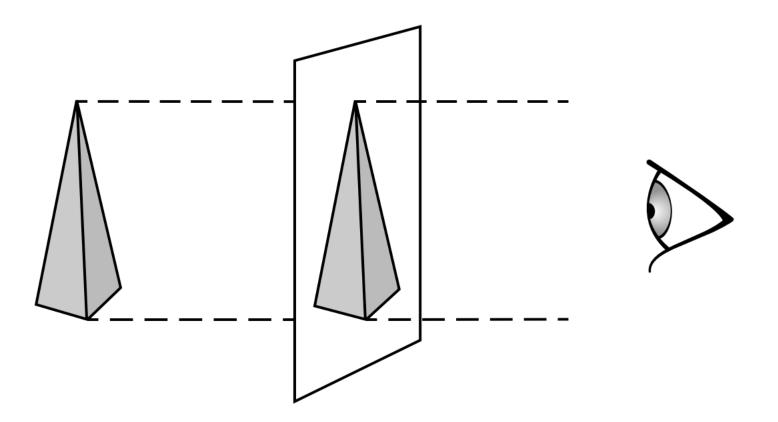
Non-planar projections are often used in map construction



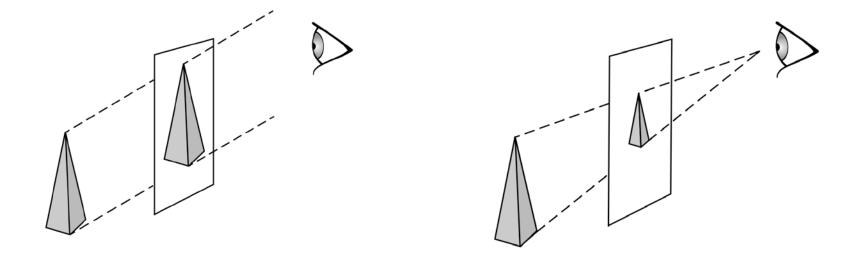
Perspective Projection



Orthographic Projection



Oblique Projections



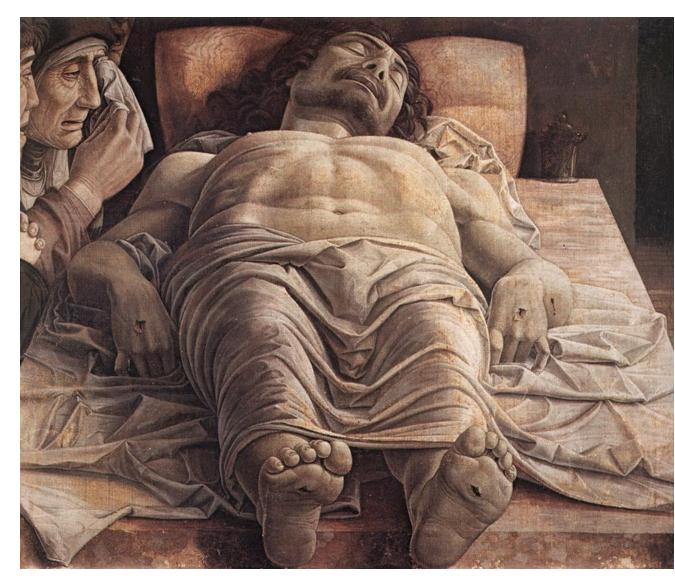
Oblique parallel projection Oblique perspective projection

Linear projections can be categorized

- By whether the projectors are parallel
- By whether the projectors are orthogonal to the view plane

We will not use these.....

Definition to Know: Foreshortening



Foreshortening is the visual effect or optical illusion that causes an object or distance to appear shorter than it actually is because it is angled toward the viewer.

i.e. projections squash receding surfaces

Can foreshortening happen in orthographic projection?

Andrea Mantegna The Lamentation over the Dead Christ

Clip Space View Volume

Before looking at projections in more detail...

...let's experimentally determine what the default view and view volume are.

So, if we don't do any transformations...where are we and what direction are we looking?

Take a look at

https://developer.mozilla.org/en-US/docs/Web/API/WebGL_API/WebGL_model_view_projection

http://jsfiddle.net/2x03hdc8/

It is a simple WebGL program that lets you draw rectangles

No transformations

By altering the rectangle coordinates, you can figure out the view....

Clip Space View Volume

• Something new – the code enables hidden surface removal

| 38 | // Tell WebGL to test the depth when drawing, so if a square is behind |
|----|--|
| 39 | // another square it won't be drawn |
| 40 | gl.enable(gl.DEPTH_TEST); |

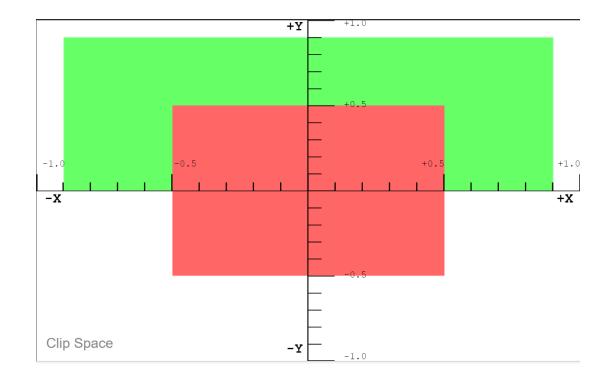
Side note - the overall code uses different conventions than used in our course (e.g. no glmatrix library)

So, probably don't base your assignments on this code

Clip Space View

- Red rectangle has z=0
- Green has z=0.5

What direction are we looking?

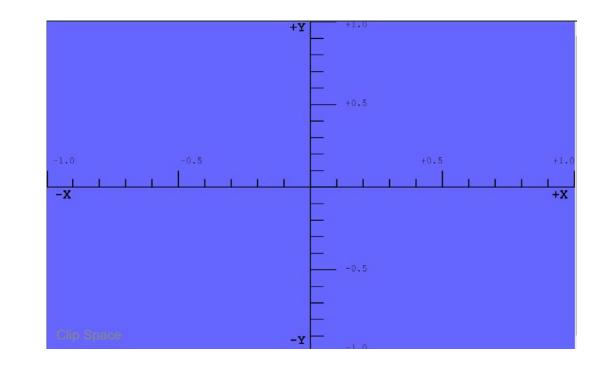


Clip Space View

We add a blue rectangle

It's at z=-1

Where is the near clipping plane?

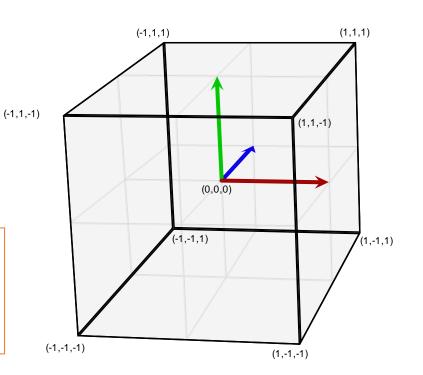


Clip Space View and View Volume

View is looking down Z+ Eyepoint is effectively at (0,0,-1) This is a left-handed coordinate system

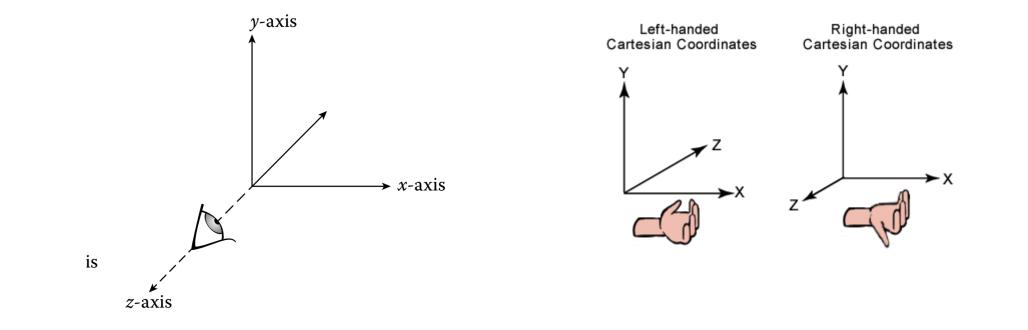
This is a little-known fact.... People often learn to use WebGL without ever learning this.

We'll see why in a few slides



Clipspace

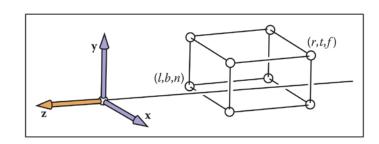
WebGL Style View

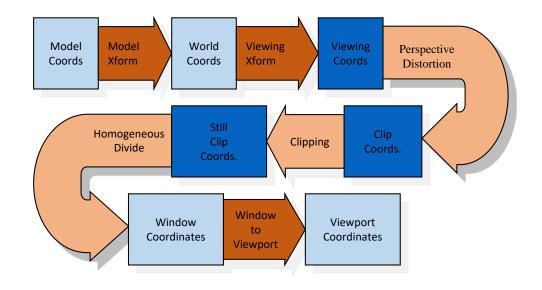


WebGL/OpenGL convention is to assume a right-handed world coordinate system

The *ortho* matrix is used to flip this coordinate system by scaling Z by -1 It then matches WebGL clip space

More WebGL Secrets





WebGL only performs an orthogonal projection

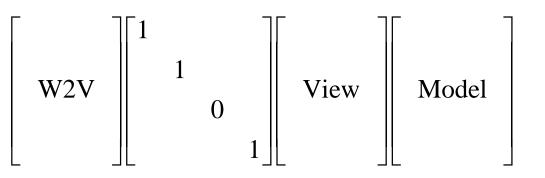
- Everything is projected to the z=0 plane in the normalized view volume
- But you can distort your geometry to achieve a perspective projection

The projection occurs when the geometry is in clip space (NDC)

- Even then, depth information is kept around to do hidden surface removal
- Depth information means transformed z coordinates

Orthographic Projection

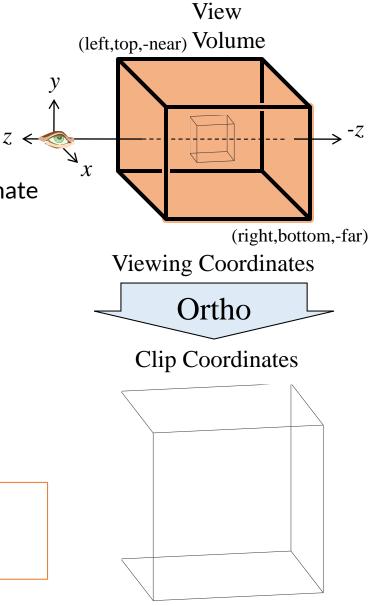
- Foreshortens
- No change in size by depth
- Classic Orthographic Projection matrix simply zeros the z- coordinate



mat4.ortho(out,left,right,bottom,top,near,far)

$$\begin{bmatrix} \frac{2}{r-l} & 0 & 0 & -\frac{r+l}{r-l} \\ 0 & \frac{2}{t-b} & 0 & -\frac{t+b}{t-b} \\ 0 & 0 & \frac{-2}{f-n} & -\frac{f+n}{f-n} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

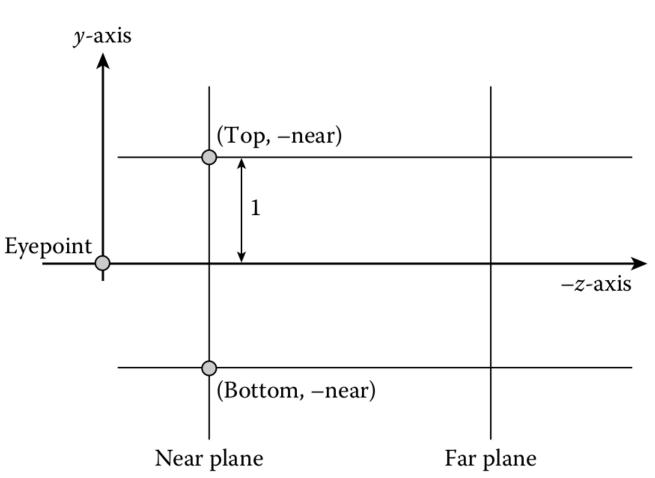
Does the ortho matrix perform a projection?



GLMatrix ortho matrix

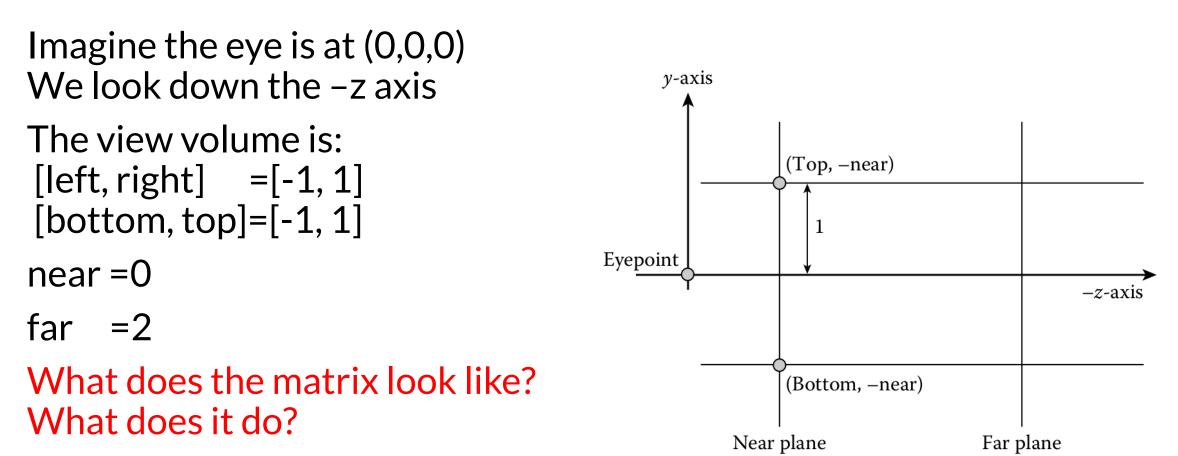
ortho(left,right,bottom,top,near,far)

- near and far are distances down the -z axis from origin
- l,r,b,t are coordinates of the bounding planes
- what does the matrix do?



GLMatrix ortho matrix

ortho(left,right,bottom,top,near,far)



GLMatrix ortho matrix

ortho(left,right,bottom,top,near,far)

Imagine the eye is at (0,0,0)We look down the -z axis

The view volume is: [left, right] =[-1, 1] [bottom, top]=[-1, 1]

near =0

far =2

Where does (0,0,0) get moved to? What else happens?

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & -1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$