

CS/ECE 374 A ✧ Spring 2026
☞ Midterm 1 Practice 1 ☞
February 19, 2026

Name:	
NetID:	

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- ***Don't panic!***
 - You have 120 minutes to answer five questions. The questions are described in more detail in a separate handout.
 - If you brought anything except your writing implements, your **hand-written** double-sided 8½" × 11" cheat sheet, and your university ID, please put it away for the duration of the exam. In particular, please turn off and put away *all* medically unnecessary electronic devices.
 - Please clearly print your name and your NetID in the boxes above.
 - Please also print your name at the top of every page of the answer booklet, except this cover page. We want to make sure that if a staple falls out, we can reassemble your answer booklet. (It doesn't happen often, but it does happen.)
 - Proofs or other justifications are required for full credit if and only if we explicitly ask for them, using the word ***prove*** or ***justify*** in bold italics.
 - **Do not write outside the black boxes on each page.** These indicate the area of the page that our scanners will actually scan. If the scanner can't see your work, we can't grade it.
 - If you run out of space for an answer, please use the overflow/scratch pages at the back of the answer booklet, but **please clearly indicate where we should look.** If we can't find your work, we can't grade it.
 - **Only work that is written into the stapled answer booklet will be graded.** In particular, you are welcome to detach scratch pages from the answer booklet, but any work on those detached pages will not be graded. Please let us know if you detach a page accidentally. We will provide additional scratch paper on request.
 - Please return ***all*** paper with your answer booklet: your question sheet, your cheat sheet, and all scratch paper. **Please put all loose paper *inside* your answer booklet.**
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Is between
between is and between
or between between and is
or between and and or
or between or and between
or between between and and
or between or and and
or between or and or?

For each statement below, check “Yes” if the statement is always true and check “No” otherwise, and give a brief (one short sentence) explanation of your answer. Read these statements very carefully—small details matter!

(a) Every integer in the empty set is prime.

Yes No _____

(b) The language $\{0^m 1^n \mid m + n \leq 374\}$ is regular.

Yes No _____

(c) The language $\{0^m 1^n \mid m - n \leq 374\}$ is regular.

Yes No _____

(d) For all languages L , the language L^* is regular.

Yes No _____

(e) For all languages L , the language L^* is infinite.

Yes No _____

(f) For all languages $L \subseteq \Sigma^*$, if L can be represented by a regular expression, then $\Sigma^* \setminus L$ is recognized by a DFA.

Yes No _____

(g) For all languages L and L' , if $L \cap L' = \emptyset$ and L' is not regular, then L is regular.

Yes No _____

(h) Every regular language is recognized by a DFA with at least 374 accepting states.

Yes No _____

(i) Every regular language is recognized by an NFA with at most 374 accepting states.

Yes No _____

(j) Every context-free language has an infinite fooling set.

Yes No _____

The *parity* of a bit-string w is 0 if w has an even number of 1 s, and 1 if w has an odd number of 1 s.

- (a) Give a *self-contained*, formal, recursive definition of the *parity* function. (In particular, do **not** refer to $\#$ or other functions defined in class.)
 - (b) **Prove** that for every regular language L , the language $\text{ODDPARITY}(L) := \{w \in L \mid \text{parity}(w) = 1\}$ is also regular.
 - (c) **Prove** that for every regular language L , the language $\text{ADDPARITY}(L) := \{\text{parity}(w) \cdot w \mid w \in L\}$ is also regular.
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For each of the following languages over the alphabet $\Sigma = \{0, 1\}$, either **prove** that the language is regular or **prove** that the language is not regular. Both of these languages contain the string 00110100000110100 .

(a) $\{0^n w 0^n \mid w \in \Sigma^+ \text{ and } n > 0\}$

(b) $\{w 0^n w \mid w \in \Sigma^+ \text{ and } n > 0\}$

For any string $w \in \{0, 1\}^*$, let $\text{take2skip2}(w)$ denote the subsequence of w containing symbols at positions $1, 2, 5, 6, 9, 10, \dots, 4i + 1, 4i + 2, \dots$. In other words, $\text{take2skip2}(w)$ takes the first two symbols of w , skips the next two, takes the next two, skips the next two, and so on. Let L be an arbitrary regular language over $\{0, 1\}$.

- (a) **Prove** that the language $\{w \in \Sigma^* \mid \text{take2skip2}(w) \in L\}$ is regular.
- (b) **Prove** that the language $\{\text{take2skip2}(w) \mid w \in L\}$ is regular.
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For each of the following languages L over the alphabet $\Sigma = \{0, 1\}$, describe a DFA that accepts L **and** give a regular expression that represents L . You do *not* need to prove that your answers are correct.

- (a) All strings in which every run of 1s has even length and every run of 0s has odd length.
 - (b) All strings in 0^*10^* whose length is a multiple of 3.
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(scratch paper)

(scratch paper)

(scratch paper)