## CS/ECE 374 A (Spring 2024) Homework 4 (due Feb 15 Thursday at 10am)

**Instructions:** As in previous homeworks.

- **Problem 4.1:** For each of the following languages, determine whether it is regular or not, and give a proof. To prove that a language is not regular, you should use the fooling set method. (To prove that a language is regular, you are allowed to use known facts about regular languages, e.g., closure properties, all finite languages are regular, ...)
  - (a)  $\{0^{i}1^{j}0^{k} : j \text{ is divisible by } i+k, \text{ and } i+j+k \text{ is divisible by } 4, \text{ and } i, j, k \ge 5\}.$
  - (b)  $\{xx^R 0x : x \in \{0,1\}^*\}$  (where  $x^R$  denotes the reverse of x).
  - (c) All strings  $x \in \{0, 1\}^*$  such that x ends in a palindrome of length between 4 and 374.
  - (d) All strings  $x \in \{0, 1\}^*$  such that x ends in a palindrome of length at least 374.
- **Problem 4.2:** Give a context-free grammar (CFG) for each of the following languages. You must provide explanation for how your grammar works, by describing in English what is generated by each non-terminal. (Formal proofs of correctness are not required.)
  - (a) All strings  $x \in \{0, 1\}^*$  such that x ends in a palindrome of length at least 4.
  - (b) All strings  $w = x0^i y$  where  $x, y \in \{0, 1\}^*$  and  $i \ge \frac{2|w|}{3}$ .
  - (c)  $\{0^i 1^j 0^k : k \ge 2i \text{ and } i+j+k \text{ is divisible by } 4\}.$