

CS/ECE 374 A ✧ Fall 2025  
🌀 Midterm 1 Practice 3 🌀  
September 28, 2025

Name:	
NetID:	

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- ***Don't panic!***
  - You have 120 minutes to answer five questions. The questions are described in more detail in a separate handout.
  - If you brought anything except your writing implements, your **hand-written** double-sided  $8\frac{1}{2}'' \times 11''$  cheat sheet, and your university ID, please put it away for the duration of the exam. In particular, please turn off and put away *all* medically unnecessary electronic devices.
  - Please clearly print your name and your NetID in the boxes above.
  - Please also print your name at the top of every page of the answer booklet, except this cover page. We want to make sure that if a staple falls out, we can reassemble your answer booklet. (It doesn't happen often, but it does happen.)
  - Proofs or other justifications are required for full credit if and only if we explicitly ask for them, using the word ***prove*** or ***justify*** in bold italics.
  - **Do not write outside the black boxes on each page.** These indicate the area of the page that our scanners will actually scan. If the scanner can't see your work, we can't grade it.
  - If you run out of space for an answer, please use the overflow/scratch pages at the back of the answer booklet, but **please clearly indicate where we should look**. If we can't find your work, we can't grade it.
  - **Only work that is written into the stapled answer booklet will be graded.** In particular, you are welcome to detach scratch pages from the answer booklet, but any work on those detached pages will not be graded. Please let us know if you detach a page accidentally. We will provide additional scratch paper on request.
  - Please return ***all*** paper with your answer booklet: your question sheet, your cheat sheet, and all scratch paper. **Please put all loose paper *inside* your answer booklet.**
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Is between  
between is and between  
or between between and is  
or between and and or  
or between or and between  
or between between and and  
or between or and and  
or between or and or?

**CS/ECE 374 A ♦ Fall 2025**  
**Midterm 1 Practice 2 Problem 1**

Name: \_\_\_\_\_

For each statement below, check “Yes” if the statement is always true and check “No” otherwise, and give a brief (one short sentence) explanation of your answer. Read these statements very carefully—small details matter!

- (a) Every integer in the empty set is prime.

Yes	No
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- (b) The language  $\{0^m 1^n \mid m + n \leq 374\}$  is regular.

Yes	No
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\_\_\_\_\_

- (c) The language  $\{0^m 1^n \mid m - n \leq 374\}$  is regular.

Yes	No
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\_\_\_\_\_

- (d) For all languages  $L$ , the language  $L^*$  is regular.

Yes	No
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\_\_\_\_\_

- (e) For all languages  $L$ , the language  $L^*$  is infinite.

Yes	No
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\_\_\_\_\_

- (f) For all languages  $L \subseteq \Sigma^*$ , if  $L$  can be represented by a regular expression, then  $\Sigma^* \setminus L$  is recognized by a DFA.

Yes	No
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\_\_\_\_\_

- (g) For all languages  $L$  and  $L'$ , if  $L \cap L' = \emptyset$  and  $L'$  is not regular, then  $L$  is regular.

Yes	No
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\_\_\_\_\_

- (h) Every regular language is recognized by a DFA with at least 374 accepting states.

Yes	No
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\_\_\_\_\_

- (i) Every regular language is recognized by an NFA with at most 374 accepting states.

Yes	No
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\_\_\_\_\_

- (j) Every context-free language has an infinite fooling set.

Yes	No
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\_\_\_\_\_

The *parity* of a bit-string  $w$  is 0 if  $w$  has an even number of 1s, and 1 if  $w$  has an odd number of 1s.

- (a) Give a *self-contained*, formal, recursive definition of the *parity* function. (In particular, do **not** refer to # or other functions defined in class.)
  - (b) **Prove** that for every regular language  $L$ , the language  $\text{ODDPARITY}(L) := \{w \in L \mid \text{parity}(w) = 1\}$  is also regular.
  - (c) **Prove** that for every regular language  $L$ , the language  $\text{ADDPARITY}(L) := \{\text{parity}(w) \cdot w \mid w \in L\}$  is also regular.
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<b>CS/ECE 374 A ✧ Fall 2025</b> <b>Midterm 1 Practice 2 Problem 3</b>	Name: _____
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For each of the following languages over the alphabet  $\Sigma = \{0, 1\}$ , either **prove** that the language is regular or **prove** that the language is not regular. Both of these languages contain the string **00110100000110100**.

(a)  $\{0^n w 0^n \mid w \in \Sigma^+ \text{ and } n > 0\}$

(b)  $\{w 0^n w \mid w \in \Sigma^+ \text{ and } n > 0\}$

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For any string  $w \in \{0, 1\}^*$ , let  $\text{take2skip2}(w)$  denote the subsequence of  $w$  containing symbols at positions  $1, 2, 5, 6, 9, 10, \dots, 4i + 1, 4i + 2, \dots$ . In other words,  $\text{take2skip2}(w)$  takes the first two symbols of  $w$ , skips the next two, takes the next two, skips the next two, and so on. Let  $L$  be an arbitrary regular language over  $\{0, 1\}$ .

- (a) **Prove** that the language  $\{w \in \Sigma^* \mid \text{take2skip2}(w) \in L\}$  is regular.
- (b) **Prove** that the language  $\{\text{take2skip2}(w) \mid w \in L\}$  is regular.
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<b>CS/ECE 374 A ✧ Fall 2025</b> <b>Midterm 1 Practice 2 Problem 5</b>	Name:
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For each of the following languages  $L$  over the alphabet  $\Sigma = \{0, 1\}$ , describe a DFA that accepts  $L$  **and** give a regular expression that represents  $L$ . You do **not** need to prove that your answers are correct.

- (a) All strings in which every run of 1s has even length and every run of 0s has odd length.
  - (b) All strings in  $0^*10^*$  whose length is a multiple of 3.
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(scratch paper)



(scratch paper)

(scratch paper)