

CS/ECE 374 A ✧ Fall 2025
☞ Midterm 1 Practice 2 ☞
September 26, 2025

Name:	
NetID:	

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- ***Don't panic!***
 - You have 120 minutes to answer five questions. The questions are described in more detail in a separate handout.
 - If you brought anything except your writing implements, your **hand-written** double-sided $8\frac{1}{2}'' \times 11''$ cheat sheet, and your university ID, please put it away for the duration of the exam. In particular, please turn off and put away *all* medically unnecessary electronic devices.
 - Please clearly print your name and your NetID in the boxes above.
 - Please also print your name at the top of every page of the answer booklet, except this cover page. We want to make sure that if a staple falls out, we can reassemble your answer booklet. (It doesn't happen often, but it does happen.)
 - Proofs or other justifications are required for full credit if and only if we explicitly ask for them, using the word ***prove*** or ***justify*** in bold italics.
 - **Do not write outside the black boxes on each page.** These indicate the area of the page that our scanners will actually scan. If the scanner can't see your work, we can't grade it.
 - If you run out of space for an answer, please use the overflow/scratch pages at the back of the answer booklet, but **please clearly indicate where we should look**. If we can't find your work, we can't grade it.
 - **Only work that is written into the stapled answer booklet will be graded.** In particular, you are welcome to detach scratch pages from the answer booklet, but any work on those detached pages will not be graded. Please let us know if you detach a page accidentally. We will provide additional scratch paper on request.
 - Please return ***all*** paper with your answer booklet: your question sheet, your cheat sheet, and all scratch paper. **Please put all loose paper *inside* your answer booklet.**
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CS/ECE 374 A ♦ Fall 2025
Midterm 1 Practice 2 Problem 1

Name: _____

For each statement below, check “Yes” if the statement is always true and check “No” otherwise, and give a brief (one short sentence) explanation of your answer. Read these statements very carefully—small details matter!

(a) Every infinite language is regular.

Yes	No	_____
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(b) The language $(0 + 1(01^*0)^*1)^*$ is not context-free.

Yes	No	_____
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(c) Every subset of an irregular language is irregular.

Yes	No	_____
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(d) The language $\{0^a 1^b \mid a - b \text{ is divisible by } 374\}$ is regular.

Yes	No	_____
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(e) If language L is not regular, then L has a finite fooling set.

Yes	No	_____
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(f) If there is a DFA that rejects every string in language L , then L is regular.

Yes	No	_____
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(g) If language L is accepted by an DFA with n states, then its complement $\Sigma^* \setminus L$ is also accepted by a DFA with n states.

Yes	No	_____
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(h) 1^*0^* is a fooling set for the language $\{1^i 0^{i+j} 1^j \mid i, j \geq 0\}$.

Yes	No	_____
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(i) Every regular language is accepted by a DFA with an odd number of accepting states.

Yes	No	_____
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(j) The context-free grammar $S \rightarrow \varepsilon \mid 0S1S \mid 1S0S$ generates all strings in which the number of 0s equals the number of 1s.

Yes	No	_____
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CS/ECE 374 A ✧ Fall 2025 Midterm 1 Practice 2 Problem 2	Name:
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For any string w , let $\text{cycleleft}(w)$ denote the string obtained by moving the first symbol of w (if any) to the end. (See the question handout for a formal recursive definition.) Let L be an arbitrary regular language over the alphabet $\{0, 1\}$.

- (a) Prove that $\text{CYCLELEFT}(L) = \{\text{cycleleft}(w) \mid w \in L\}$ is a regular language.
- (b) Prove that $\text{CYCLERIGHT}(L) = \{w \in \Sigma^* \mid \text{cycleleft}(w) \in L\}$ is a regular language.
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CS/ECE 374 A ✧ Fall 2025 Midterm 1 Practice 2 Problem 3	Name:
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For any string $w \in \{0, 1\}^*$, let $\text{squish}(w)$ denote the string obtained by dividing w into pairs of symbols, replacing each pair with 0 if the symbols are equal and 1 otherwise, and keeping the last symbol if w has odd length. (See the question handout for a formal recursive definition.)

- (a) **Prove** that $\#(1, \text{squish}(w)) \leq \#(1, w)$ for every string w .
- (b) **Prove** that $\#(1, \text{squish}(w))$ is even if and only if $\#(1, w)$ is even, for every string w .
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CS/ECE 374 A ✧ Fall 2025 Midterm 1 Practice 2 Problem 4	Name:
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Let L be the set of all strings in $\{0, 1\}^*$ in which every run of 0s is followed immediately by a *shorter* run of 1s.

- (a) **Prove** that L is *not* a regular language.
 - (b) Describe a context-free grammar for L .
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CS/ECE 374 A ✧ Fall 2025 Midterm 1 Practice 2 Problem 5	Name:
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For each of the following languages L over the alphabet $\Sigma = \{0, 1\}$, describe a DFA that accepts L **and** give a regular expression that represents L . You do not need to justify your answers.

- (a) Strings that do not contain the subsequence 01110 .
- (b) Strings that contain at least two even-length runs of 1 s.

(scratch paper)

(scratch paper)

(scratch paper)