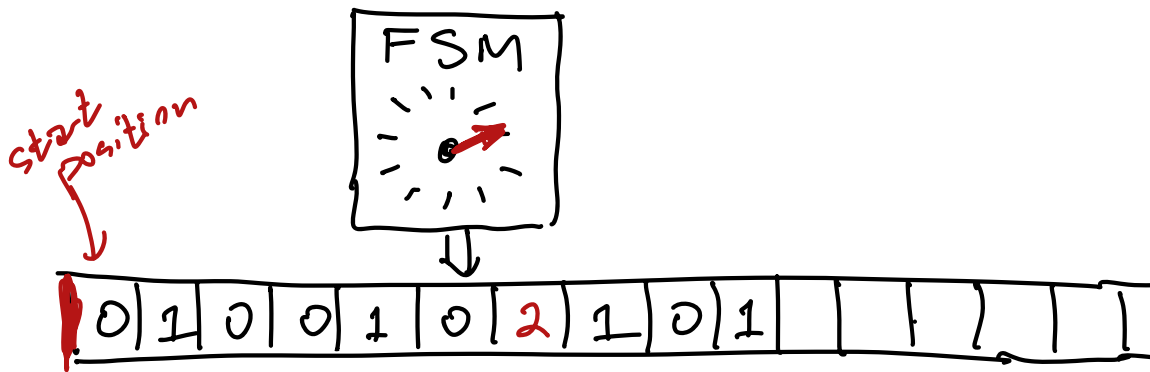


Sequencing	Languages	Machine
Branching	Regular	DFA / NFA
Repetition		
Recursion	Context-free	Pushdown automaton
		Recursive NFA
<u>Memory</u>	Recursive decidable	Turing machine
		Python
		ISC
		"Arbitrary computation"



At each step:

- Read symbol at curr pos on tape
- State
  - Write symbol at curr pos on tape
  - Change state
  - Move 1 step  $\rightarrow$  or  $\leftarrow$

Entscheidungsproblem "Decision problem"

Gödel	Nope	Incompleteness
Church	Nope	$\lambda$ -calculus
Turing	Nope	TM halting problem

There is no TM that can decide if an arbitrary TM halts.

There is no Python program that can decide, given source code for any Python program, whether that program halts.

CODE is DATA

Suppose this is false



```
I Hate Myself (M):  
  if Haltomatic(M) = True  
    hang  
  else  
    return False
```

I Hate Myself (I Hate Myself)

# Turing Machine $(\Sigma, \Gamma, \square, Q, \text{start}, \text{accept}, \text{reject}, \delta)$

$\Sigma$  - input alphabet  $\leftarrow$  finite

$\Gamma \supseteq \Sigma$  - tape alphabet  $\leftarrow$  finite

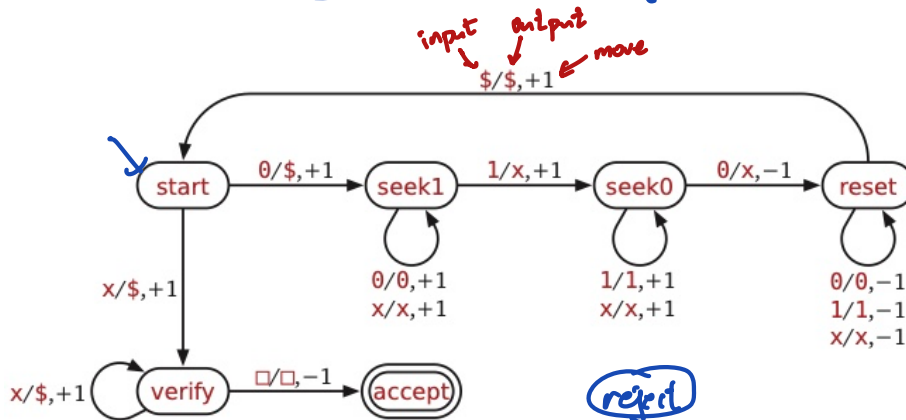
blank  $\square \in \Gamma \setminus \Sigma$

$Q$  - states  $\leftarrow$  finite

$\text{start}, \text{accept}, \text{reject} \in Q$

transition  $\delta: Q \times \Gamma \rightarrow Q \times \Gamma \times \{-1, +1\}$

$\{0^n 1^n 0^n \mid n \geq 0\}$



$\delta(p, a) = (q, b, \Delta)$	explanation
$\delta(\text{start}, 0) = (\text{seek1}, \$, +1)$	mark first 0 and scan right
$\delta(\text{start}, x) = (\text{verify}, \$, +1)$	looks like we're done, but let's make sure
$\delta(\text{seek1}, 0) = (\text{seek1}, 0, +1)$	scan rightward for 1
$\delta(\text{seek1}, x) = (\text{seek1}, x, +1)$	
$\delta(\text{seek1}, 1) = (\text{seek0}, x, +1)$	mark 1 and continue right
$\delta(\text{seek0}, 1) = (\text{seek0}, 1, +1)$	scan rightward for 0
$\delta(\text{seek0}, x) = (\text{seek0}, x, +1)$	.
$\delta(\text{seek0}, 0) = (\text{reset}, x, +1)$	mark 0 and scan left
$\delta(\text{reset}, 0) = (\text{reset}, 0, -1)$	scan leftward for \$
$\delta(\text{reset}, 1) = (\text{reset}, 1, -1)$	
$\delta(\text{reset}, x) = (\text{reset}, x, -1)$	
$\delta(\text{reset}, \$) = (\text{start}, \$, +1)$	step right and start over
$\delta(\text{verify}, x) = (\text{verify}, \$, +1)$	scan right for any unmarked symbol
$\delta(\text{verify}, \square) = (\text{accept}, \square, -1)$	success!

The transition function for a Turing machine that decides the language  $\{0^n 1^n 0^n \mid n \geq 0\}$ .

$$\delta(p, a) = (q, b, \Delta)$$

$$\delta(\text{start}, 0) = (\text{seek1}, \$, +1)$$

$$\delta(\text{start}, x) = (\text{verify}, \$, +1)$$

$$\delta(\text{seek1}, 0) = (\text{seek1}, 0, +1)$$

$$\delta(\text{seek1}, x) = (\text{seek1}, x, +1)$$

$$\delta(\text{seek1}, 1) = (\text{seek0}, x, +1)$$

$$\delta(\text{seek0}, 1) = (\text{seek0}, 1, +1)$$

$$\delta(\text{seek0}, x) = (\text{seek0}, x, +1)$$

$$\delta(\text{seek0}, 0) = (\text{reset}, x, +1)$$

$$\delta(\text{reset}, 0) = (\text{reset}, 0, -1)$$

$$\delta(\text{reset}, 1) = (\text{reset}, 1, -1)$$

$$\delta(\text{reset}, x) = (\text{reset}, x, -1)$$

$$\delta(\text{reset}, \$) = (\text{start}, \$, +1)$$

$$\delta(\text{verify}, x) = (\text{verify}, \$, +1)$$

$$\delta(\text{verify}, \square) = (\text{accept}, \square, -1)$$

$$(\text{start}, 001100)$$

$$\Rightarrow (\text{seek1}, \$01100)$$

$$\Rightarrow (\text{seek1}, \$01100)$$

$$\Rightarrow (\text{seek0}, \$0x100)$$

$$\Rightarrow (\text{seek0}, \$0x100)$$

$$\Rightarrow (\text{reset}, \$0x1x0)$$

$$\Rightarrow (\text{reset}, \$0x1x0)$$

$$\Rightarrow (\text{reset}, \$0x1x0)$$

$$\Rightarrow (\text{reset}, \$0x1x0)$$

$$\Rightarrow (\text{reset}, \$0x1x0)$$

$$\Rightarrow (\text{start}, \$0x1x0)$$

$$\Rightarrow (\text{seek1}, \$x1x0)$$

$$\Rightarrow (\text{seek1}, \$x1x0)$$

$$\Rightarrow (\text{seek0}, \$xxx0)$$

$$\Rightarrow (\text{seek0}, \$xxx0)$$

$$\Rightarrow (\text{reset}, \$xxxx)$$

$$\Rightarrow (\text{reset}, \$xxxx)$$

$$\Rightarrow (\text{reset}, \$xxxx)$$

$$\Rightarrow (\text{reset}, \$xxxx)$$

$$\Rightarrow (\text{start}, \$xxxx)$$

$$\Rightarrow (\text{verify}, \$\$xxx)$$

$$\Rightarrow (\text{verify}, \$\$xx)$$

$$\Rightarrow (\text{verify}, \$\$\$x)$$

$$\Rightarrow (\text{verify}, \$\$\$\square)$$

$$\Rightarrow (\text{accept}, \$\$\$\$\$) \Rightarrow \text{accept!}$$

$$(\text{start}, 00100)$$

$$\Rightarrow (\text{seek1}, \$0100)$$

$$\Rightarrow (\text{seek1}, \$0100)$$

$$\Rightarrow (\text{seek0}, \$0x00)$$

$$\Rightarrow (\text{seek0}, \$0x00)$$

$$\Rightarrow (\text{reset}, \$0xx0)$$

$$\Rightarrow (\text{reset}, \$0xx0)$$

$$\Rightarrow (\text{reset}, \$0xx0)$$

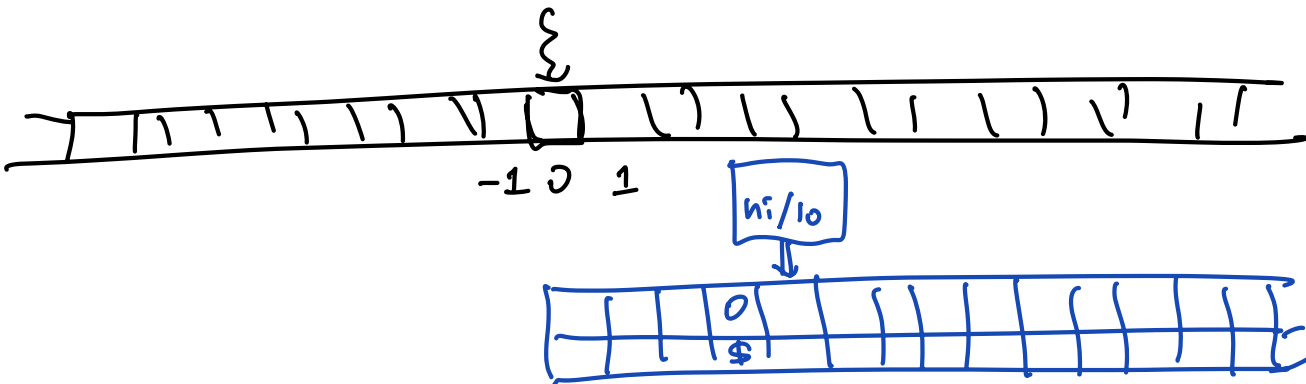
$$\Rightarrow (\text{start}, \$0xx0)$$

$$\Rightarrow (\text{seek1}, \$\$xx0)$$

$$\Rightarrow (\text{seek1}, \$\$xx0)$$

$$\Rightarrow (\text{seek1}, \$\$xx0) \Rightarrow \text{reject!}$$

Simulate bi-infinite tape using 2 tracks

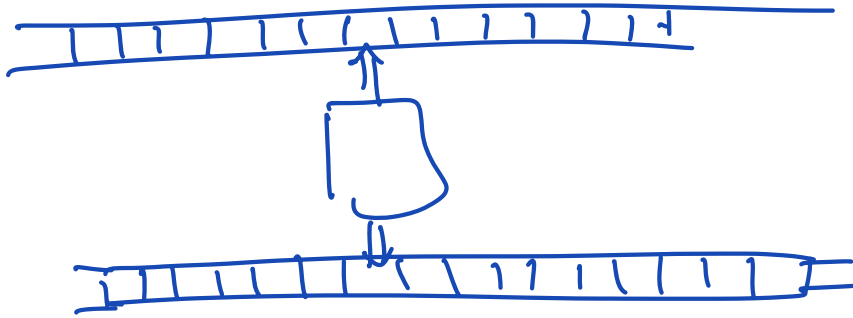


$$Q' = Q \times Q$$

$$Q' = Q \times \{h_i, 10\}$$

+  
-

Simulate multiple tapes



tape 1	0	1	2	0				
tape 2		B	X		0	1	2	
pos 1				*				
pos 2							*	

2d tape

