CS/ECE 374 A **♦** Fall 2019

September 30, 2019

Real name:	
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• Don't panic!

- If you brought anything except your writing implements, your **hand-written** double-sided 8½" × 11" cheat sheet, and your university ID, please put it away for the duration of the exam. In particular, please turn off and put away *all* medically unnecessary electronic devices.
- Please clearly print your real name, your university NetID, your Gradescope name, and your Gradescope email address in the boxes above. However, if you are using your real name and your university email address on Gradescope, you do *not* need to write everything twice. We will not scan this page into Gradescope.
- Please also print **only the name you are using on Gradescope** at the top of every page of the answer booklet, except this cover page. These are the pages we will scan into Gradescope.
- Please do not write outside the black boxes on each page; these indicate the area of the page that the scanner can actually see.
- If you run out of space for an answer, feel free to use the scratch pages at the back of the answer booklet, but **please clearly indicate where we should look**.
- Proofs are required for full credit if and only if we explicitly ask for them, using the word *prove* in bold italics.
- Please return *all* paper with your answer booklet: your question sheet, your cheat sheet, and all scratch paper.

CS/ECE 374 A ♦ Fall 2019 Fake Midterm 1 Problem 1 Gradescope name:

For each statement below, check "True" if the statement is *always* true and "False" otherwise. Each correct answer is worth $-\frac{1}{2}$ point; checking "I don't know" is worth $+\frac{1}{4}$ point; and flipping a coin is (on average) worth $+\frac{1}{4}$ point.

Yes No IDK

Every integer in the empty set is prime.

Yes No IDK

The language $\{0^m 1^n \mid m+n \le 374\}$ is regular.

Yes No IDK

The language $\{0^m 1^n \mid m-n \le 374\}$ is regular.

Yes No IDK

For all languages L, the language L^* is regular.

Yes No IDK

For all languages L, the language L^* is infinite.

Yes No IDK

For all languages $L \subset \Sigma^*$, if L can be represented by a regular expression, then $\Sigma^* \setminus L$ is recognized by a DFA.

Yes No

IDK

IDK

IDK

For all languages L and L', if $L \cap L' = \emptyset$ and L' is not regular, then L is regular.

Yes

No

Let $M = (\Sigma, Q, s, A, \delta)$ and $M' = (\Sigma, Q, s, Q \setminus A, \delta)$ be arbitrary **DFA**s with identical alphabets, states, starting states, and transition functions, but with complementary accepting states. Then $L(M) \cap L(M') = \emptyset$.

Yes

No

Let $M = (\Sigma, Q, s, A, \delta)$ and $M' = (\Sigma, Q, s, Q \setminus A, \delta)$ be arbitrary **NFA**s with identical alphabets, states, starting states, and transition functions, but with complementary accepting states. Then $L(M) \cap L(M') = \emptyset$.

Yes

No

IDK

For all context-free language L, the language L^{\ast} is also context-free.

CS/ECE 374 A ♦ Fall 2019 Fake Midterm 1 Problem 2

Gradescope name:

For each of the following languages over the alphabet $\Sigma = \{0,1\}$, either *prove* that the language is regular or *prove* that the language is not regular. *Exactly one of these two languages is regular.* Both of these languages contain the string 00110100000110100.

1.
$$\left\{ \mathbf{0}^n w \mathbf{0}^n \mid w \in \Sigma^+ \text{ and } n > 0 \right\}$$

2.
$$\{wo^n w \mid w \in \Sigma^+ \text{ and } n > 0\}$$

CS/ECE 374 A ♦ Fall 2019 Fake Midterm 1 Problem 3

Gradescope name:

The *parity* of a bit-string w is 0 if w has an even number of 1s, and 1 if w has an odd number of 1s. For example:

 $parity(\varepsilon) = 0$ parity(0010100) = 0 parity(00101110100) = 1

(a) Give a *self-contained*, formal, recursive definition of the *parity* function. (In particular, do *not* refer to # or other functions defined in class.)

(b) Let *L* be an arbitrary regular language. Prove that the language $OddParity(L) := \{w \in L \mid parity(w) = 1\}$ is also regular.

(c) Let *L* be an arbitrary regular language. Prove that the language $AddParity(L) := \{parity(w) \cdot w \mid w \in L\}$ is also regular.

[Hint: Yes, you have enough room.]

CS/ECE 374 A & Fall 2019	Gradescope name:
Fake Midterm 1 Problem 4	

For each of the following languages L, give a regular expression that represents L and describe a DFA that recognizes L. You do **not** need to prove that your answers are correct.

(a) All strings in $(0 + 1)^*$ that do not contain the substring 0110.

(b) All strings in 0*10* whose length is a multiple of 3.

CS/ECE 374 A ♦ Fall 2019	Gradescope name:
Fake Midterm 1 Problem 5	

Consider the language L of all strings in $\{0,1\}^*$ in which the number of 0s is even, the number of 1s is divisible by 3, and the total number of symbols is divisible by 5. For example, the strings 01011 and 00000000000 are in L, but the strings 01001 and 10101010 are not.

Formally describe a DFA $M = (Q, s, A, \delta)$ over the alphabet $\Sigma = \{0, 1\}$ that recognizes L. **Do not attempt to** <u>draw</u> the DFA. Do not use the phrase "product construction". Instead, formally and explicitly specify each of the the components Q, s, A, and δ .