$\frac{\text{Quiz 1}}{\text{CS 373: Theory of Computation}}$

Date: September 9, 2010. Lecture Section AL1. Time limit: 15 minutes.

Name					
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Discussion	Tu 2-2:50	Tu 3-3:50	Tu 4-4:50	W 4-4:50	W 5-5:50

Pick the correct alternative from among the choices (A), (B), and (C) provided for each question below. Each question is worth 1 point.

- 1. Consider the set X defined inductively as follows: (1) $(3,5) \in X$, (2) if $(x,y) \in X$ then $(x+2,y) \in X$, and (3) if $(x,y) \in X$ then $(y,x) \in X$. Which of the following pairs is a member of X?
 - (A) (222, 402)
 - (B) (1,7)
 - (C) (151, 1171)
- 2. Let $L = \{010, 101, 001, 011\}$, and $K = \{w \mid 0w \in L\}$. Which of the following strings is a member of K?
 - (A) 0101
 - (B) 01
 - (C) 011
- 3. Let M be a DFA such that M accepts the empty string ϵ .
 - (A) The initial state of M must be an accepting state.
 - (B) There is a DFA N that recognizes the same language as M and has exactly one final state.
 - (C) The initial state of M is not an accepting state.
- 4. Let $M = (Q, \Sigma, \delta, q_0, F)$ be a NFA. Recall that we had defined a function $\hat{\Delta}: Q \times \Sigma^* \to 2^Q$ that given a state q and string w returns the states of all the active threads after reading w from q. Using $\hat{\Delta}$ we can define acceptance as w is accepted by M iff
 - (A) $\hat{\Delta}(q_0, w) \in F$
 - (B) $\hat{\Delta}(q_0, w) = F$
 - (C) $\hat{\Delta}(q_0, w) \cap F \neq \emptyset$

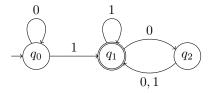


Figure 1: DFA M for question 5

- 5. Recall that 0 is an even number. The language recognized by DFA M in Figure $\ref{eq:model}$ is
 - (A) $\{w \mid w \text{ has even length}\}$
 - (B) $\{w \mid w \text{ has at least one 1 and has an even number of 0s after the last 1}\}$
 - (C) $\{w \mid w \text{ has at least one 1 and has an even number of 0s}\}$

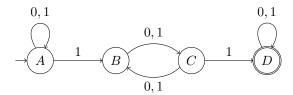


Figure 2: NFA N for question 6

- 6. The language recognized by NFA N in Figure ?? is
 - (A) $\{w \mid w \text{ is a string of 0s and 1s}\}$
 - (B) $\{w \mid w \text{ is a binary number that is a multiple of } 4\}$
 - (C) $\{w \mid w \text{ has a pair of 1s separated by an odd number of symbols}\}$