

Algorithms and Data Structures for Data Science

lab_recursion

CS 277

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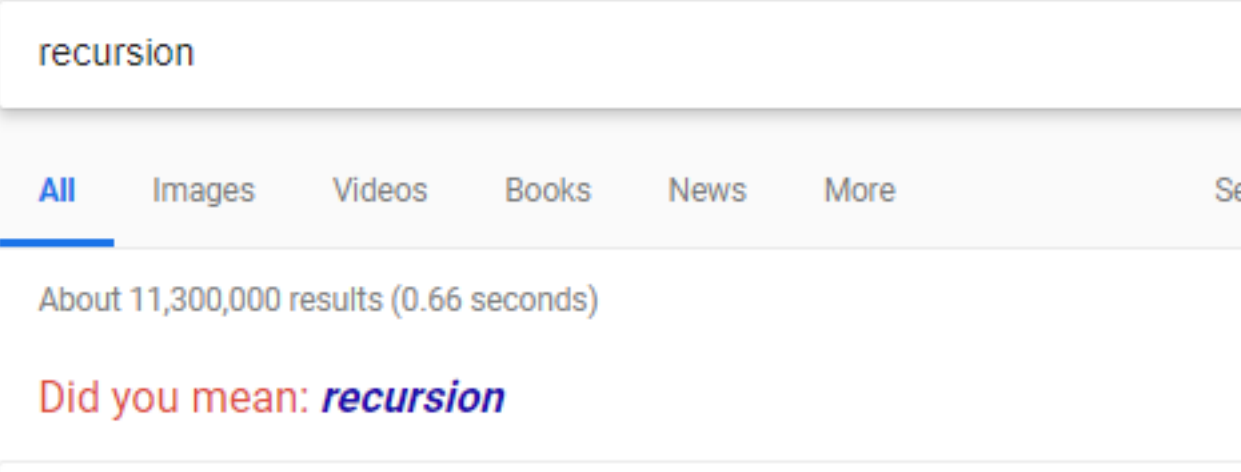
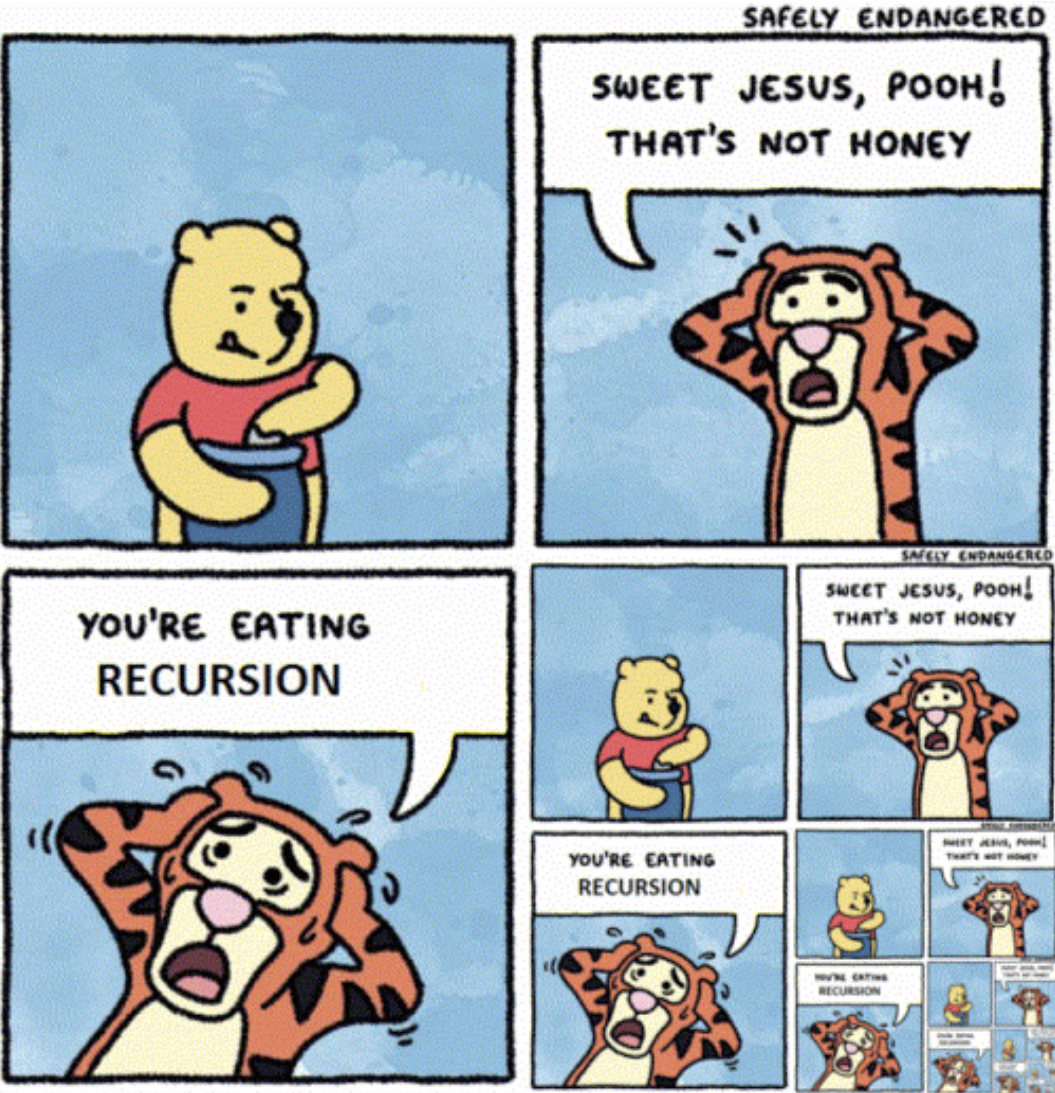
Department of Computer Science

Learning Objectives

Review fundamentals of recursion

Implement recursive functions to handle a variety of tasks

Recursion



WHO WOULD WIN?

WHO WOULD WIN?	
<p>Highly complex recursive calls</p>	<p>Simple and basic loops</p>
Highly complex recursive calls	Simple and basic loops

Recursion

The success or failure of this lab (and the time it takes you) depends on your ability to answer the following:

Base Case: What is the smallest sub-problem? What is the trivial solution?

Recursive Step: How can I reduce my problem to an easier one?

Combining: How can I build my solution from recursive pieces?

Lets work together to brainstorm some of the following functions!



Each exercise a fun new twist!

Sum of Digits:

Triangle:

Palindrome:

Fibonacci:

Bonus List Partitiong:

Recursion Practice: Sum of Digits

Given a number, return the numerical value of summing each digit.

277

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Recursion Practice: Sum of Digits

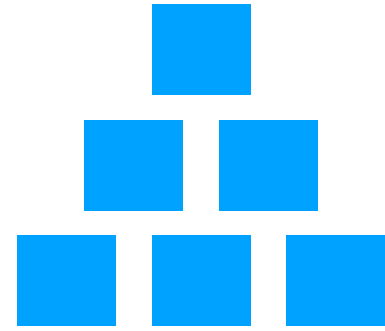
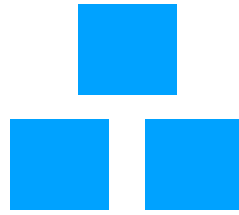
Given a number, return the numerical value of summing each digit.

Base Case:

Recursive Step:

Combining:

Recursion Practice: Triangle



Given the height of a triangle, how many total blocks were used to make it?

Base Case:

Recursive Step:

Combination Step:

Recursion Practice: String Palindrome

Given a string, return whether it is a palindrome or not (True or False)

AAA

racecar

racetrack

Recursion Practice: String Palindrome

Given a string, return whether it is a palindrome or not (True or False)

Base Case:

Recursive Step:

Combining:

Recursion Practice: Recursive Fibonacci

Given a number n , return the n th Fibonacci number:

$$Fib(n) = Fib(n - 1) + Fib(n - 2), \quad n > 1$$

Base Case:

Recursive Step:

Combining:

Using all elements in a list, can we make two lists which have equal sums?

Input

[4, 3, 1] ([], [])

[3, 1] ([4], []) ([], [4])

[1] ([3, 4], []) ([4], [3]) ([3], [4]) ([], [3, 4])

[]

([1, 3, 4], []) ([1, 4], [3]) ([1, 3], [4]) ([1], [3, 4])

([3, 4], [1]) ([4], [1, 3]) ([3], [1, 4]) ([], [1, 3, 4])

Recursive List Partitioning

Base Case: When my input list is empty, I have tried every permutation

Recursive Step: Given list L, pop() L[0] to left *and* right and recurse on both

Combination Step: If either partition recursion is True, return True