

# Algorithms and Data Structures for Data Science

## Trees

CS 277

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March 20, 2023



UNIVERSITY OF  
**ILLINOIS**  
URBANA - CHAMPAIGN

Department of Computer Science



# Assignment Extensions

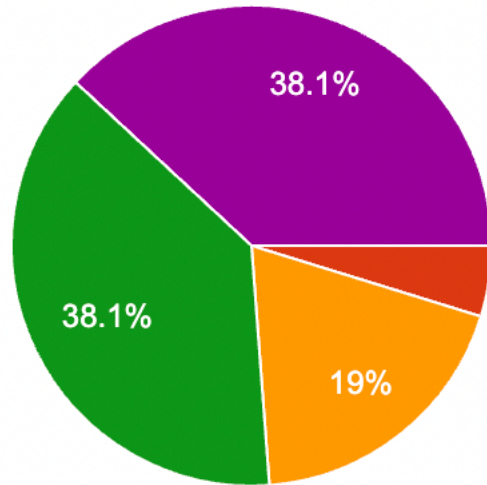
Everyone will have until Wednesday (3/22) to complete lab\_search

Everyone will have until Friday (3/24) to complete mp\_hash

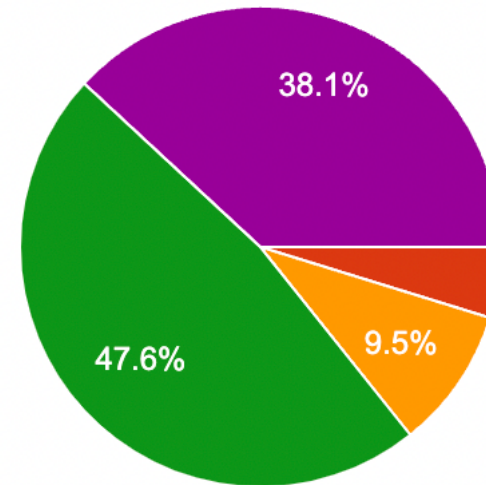
# Informal Early Feedback

I feel that I can actively participate...

in lecture:



in class in general:



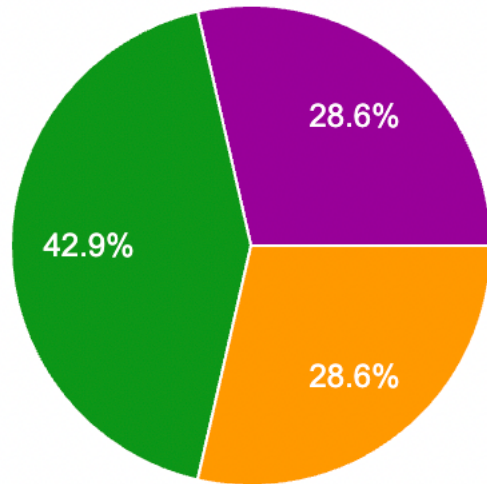
- Strongly disagree
- Disagree
- Neutral
- Agree
- Strongly agree

90.5% / 81% of class receive helpful and complete answers in / out of class

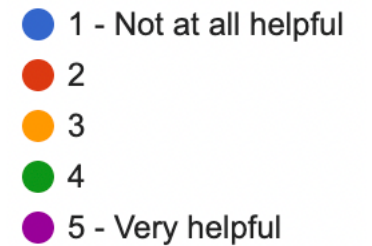
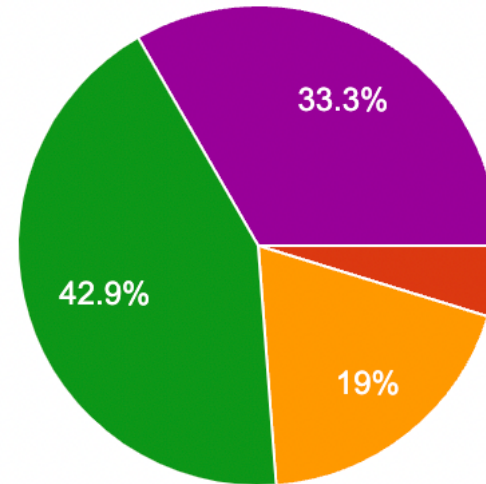
# Informal Early Feedback

Helpful for learning material...

Lectures:

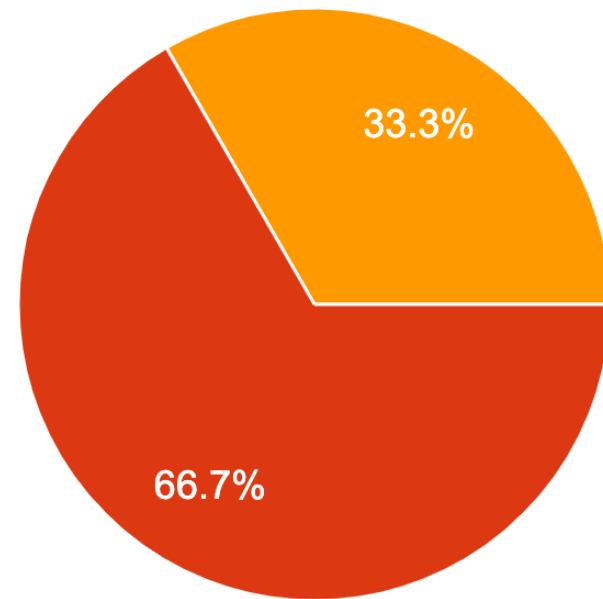


Assignments:



# Informal Early Feedback

Pacing of the course:



- Too slow
- Just right
- Too Fast

# Informal Early Feedback



Labs and lectures are 'most helpful' to most students; MPs not listed at all

## **Requests / Suggestions (in no particular order):**

Extending deadline for labs (or opening labs earlier in week)

Providing annotated lecture slides after each lecture

Include more live coding demonstrations in the class

Giving optional coding questions for practice exercises

Providing practice exams / example exam questions

A final project instead of a final

# Learning Objectives

Formally define the tree data structure

Explore properties of trees and the specifics of binary trees

Implement and understand traversals and search on trees

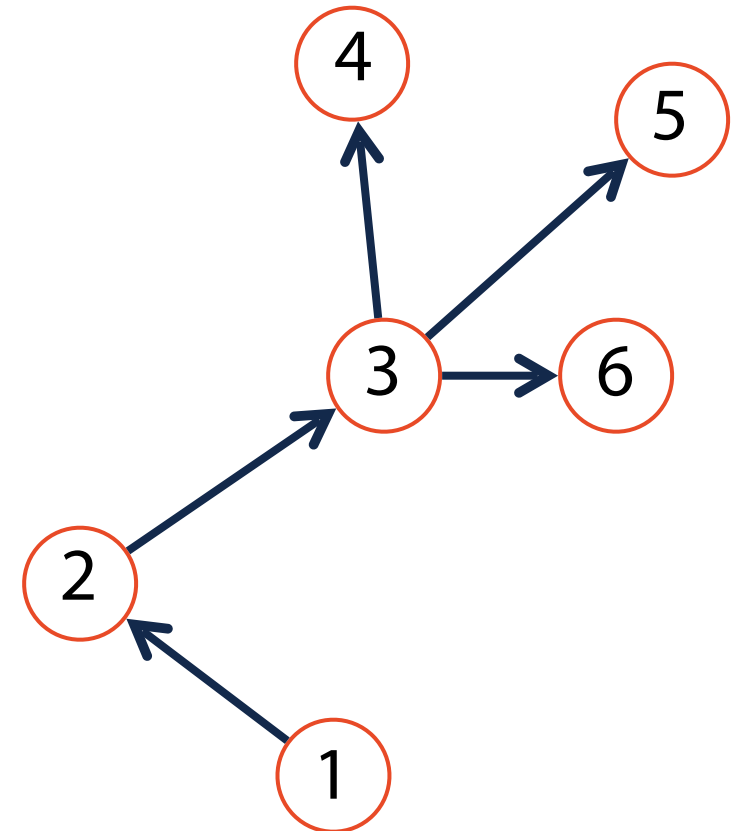


# Trees

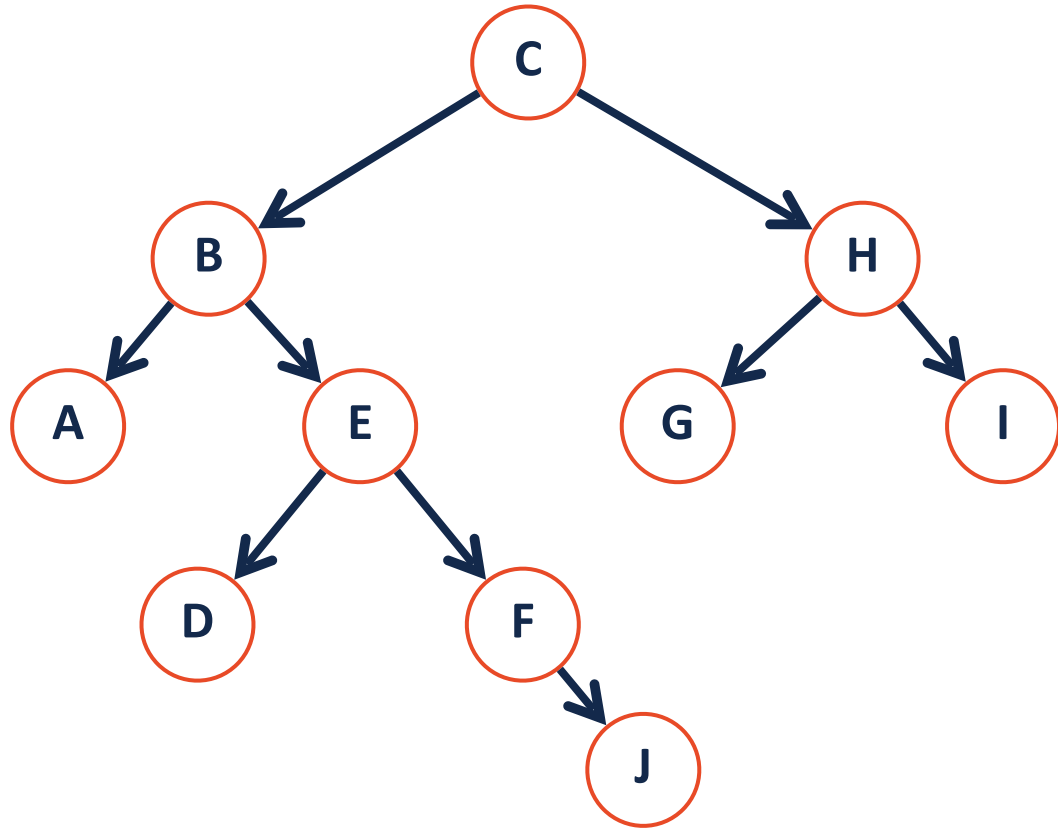
A non-linear data structure defined recursively as a collection of nodes where each node contains a value and zero or more connected nodes.

(In CS 277) a tree is also:

- 1) Acyclic
- 2) Rooted



# Tree Terminology

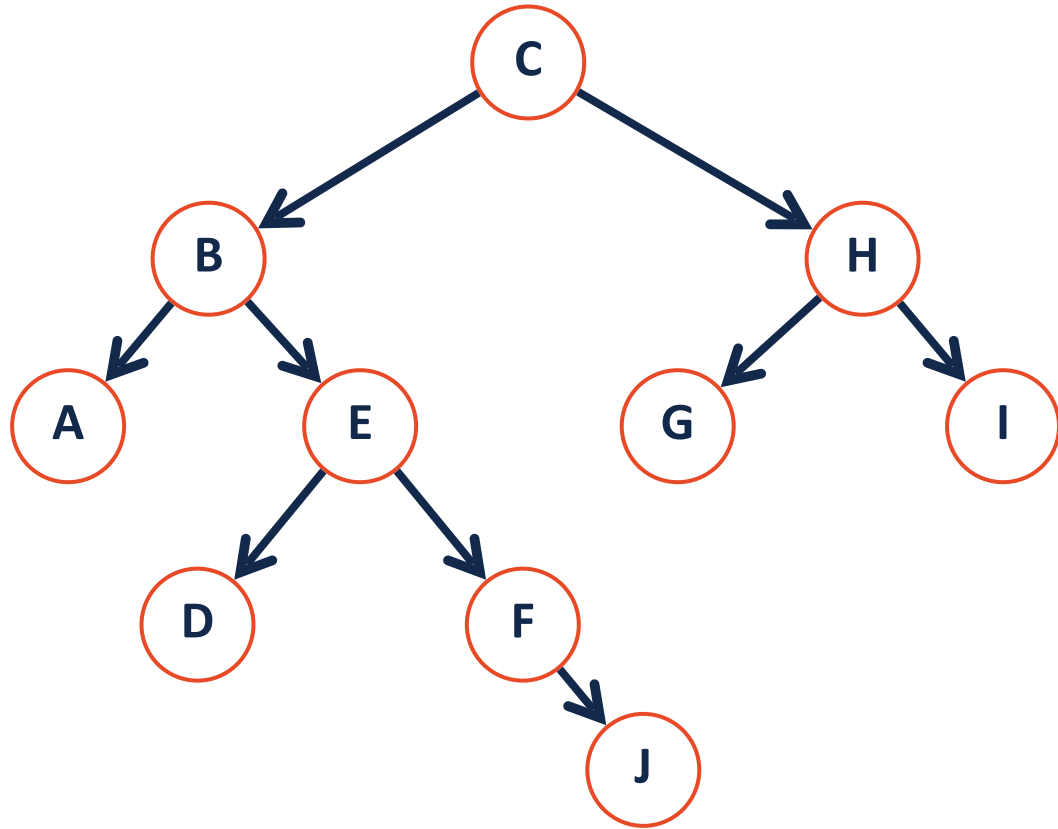


**Node:** The vertex of a tree

**Edge:** The [theoretical] connecting path between nodes

**Path:** A list of the edges (or nodes) traversed to go from node *start* to node *end*

# Tree Terminology



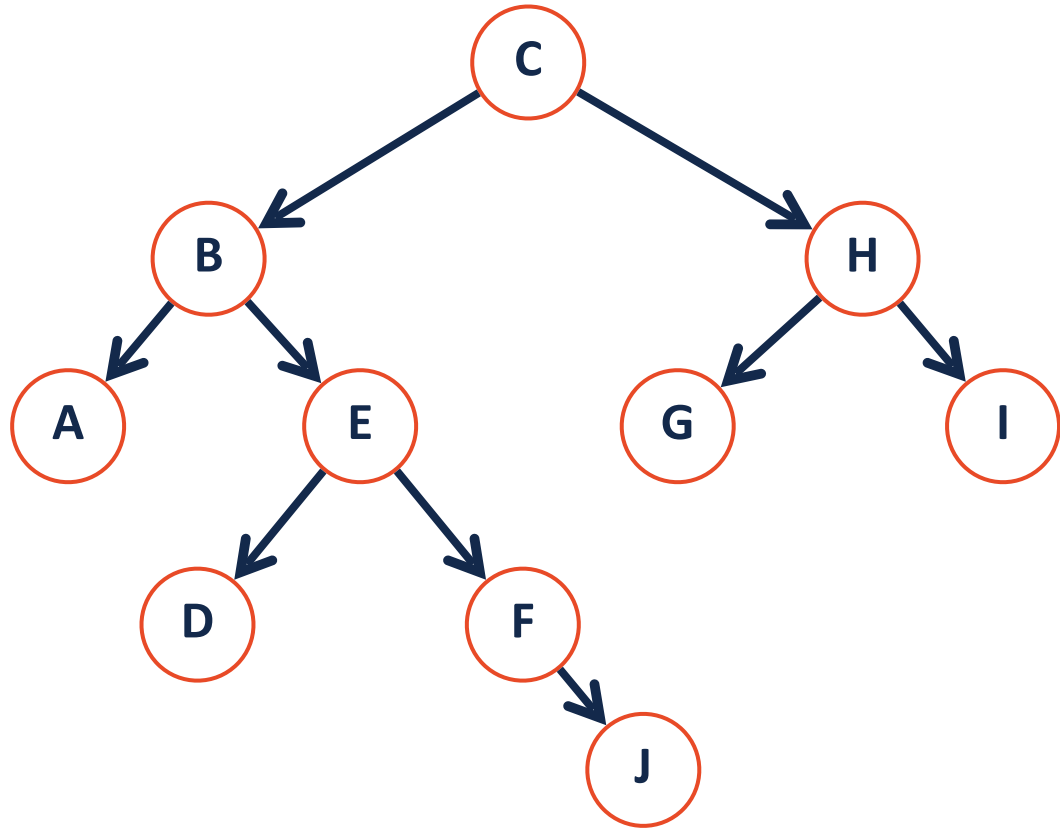
**Parent:** The precursor node to the current node is the 'parent'

**Child:** The nodes linked by the current node are its 'children'

**Neighbor:** Parent or child

**Degree:** The number of children for a given node

# Tree Terminology



**Root:** The start of a tree (the only node with no parent).

**Leaf:** The terminating nodes of a tree (have no children)

**Internal:** A node with at least one child



# Binary Tree

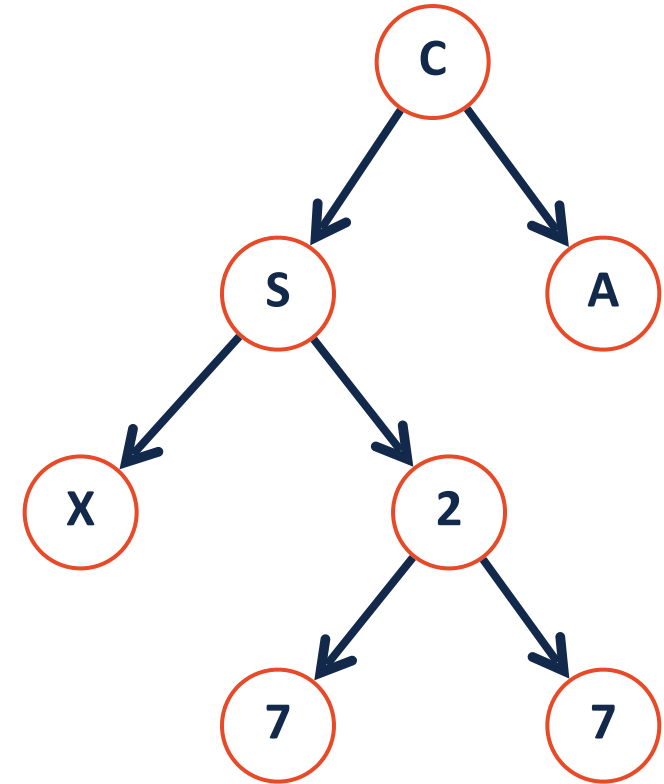


A **binary tree** is a tree  $T$  such that:

$T = \text{None}$

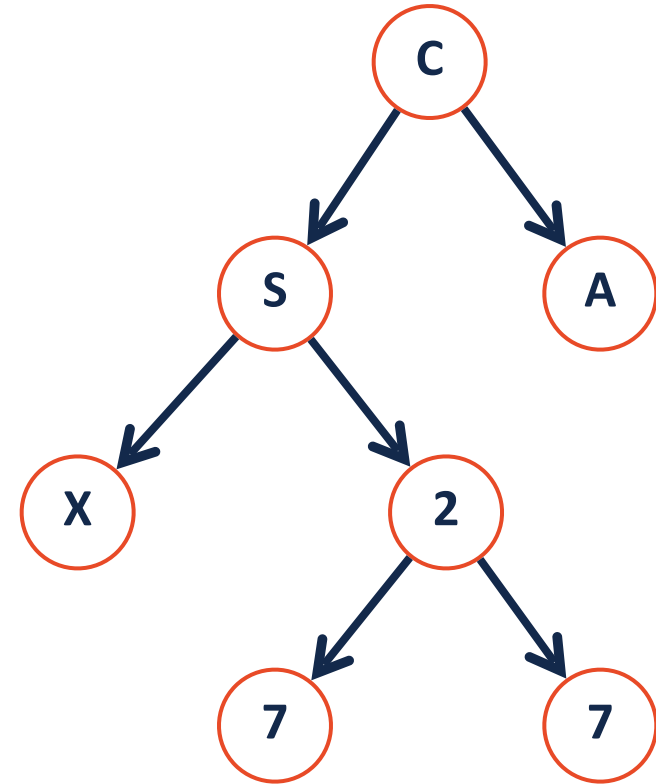
or

$T = \text{treeNode}(\text{val}, T_L, T_R)$



# Binary Tree

```
1 class treeNode:  
2     def __init__(self, _____, _____, _____):  
3  
4  
5     _____  
6  
7     _____  
8  
9     _____  
10  
11  
12  
13  
14  
15  
16 class binaryTree:  
17     def __init__(self, root=None):  
18         self.root = root  
19  
20  
21  
22  
23
```



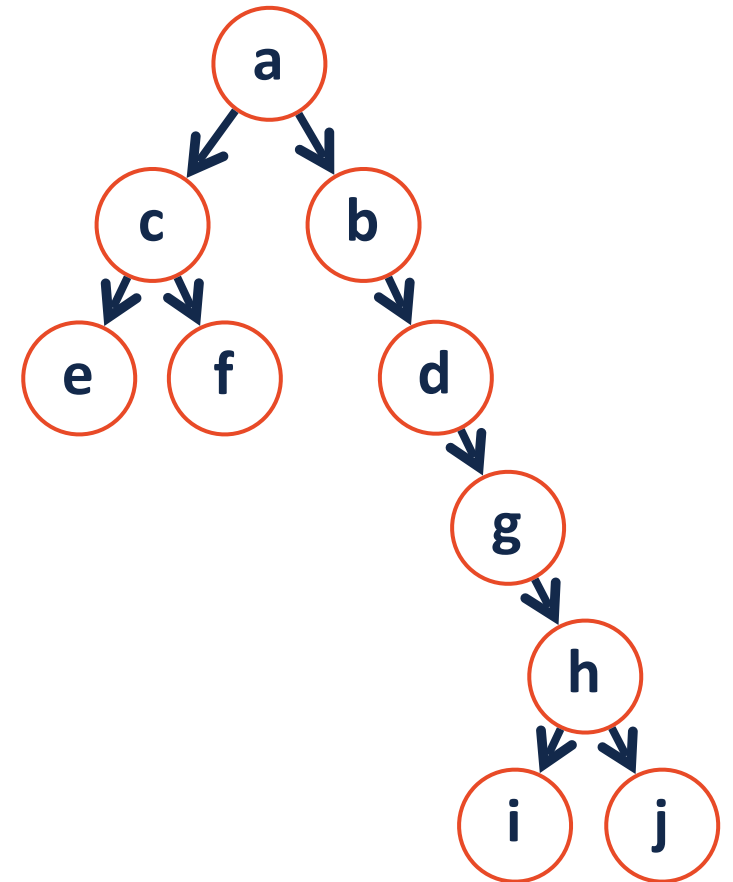
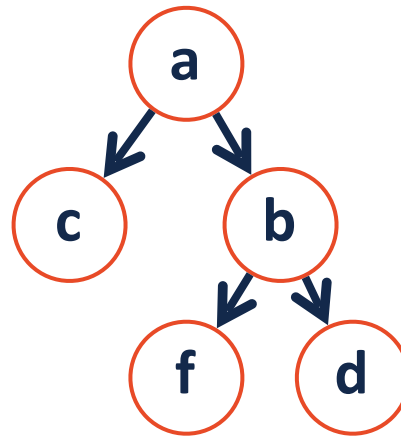
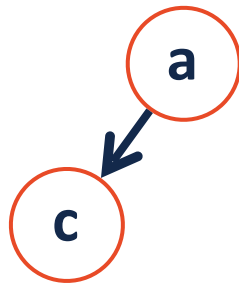
# Defining a tree

```
1 class treeNode:
2     def __init__(self, val, left=None, right=None):
3         self.val = val
4         self.left = left
5         self.right = right
6
7 tn1 = treeNode(1)
8
9 tn2 = treeNode(2)
10
11 tn3 = treeNode(3)
12
13 tn4 = treeNode(4)
14
15 tn5 = treeNode(5, tn1, tn2)
16
17 tn6 = treeNode(6, tn3, tn4)
18
19 tn7 = treeNode(7, tn5, tn6)
20
21 binaryTree(_____)
22
23
```



# Tree Terminology

**Height:** the length of the longest path from the root to a leaf



What is the height of a tree with **zero** nodes?

# Tree Height



**height(T) =**

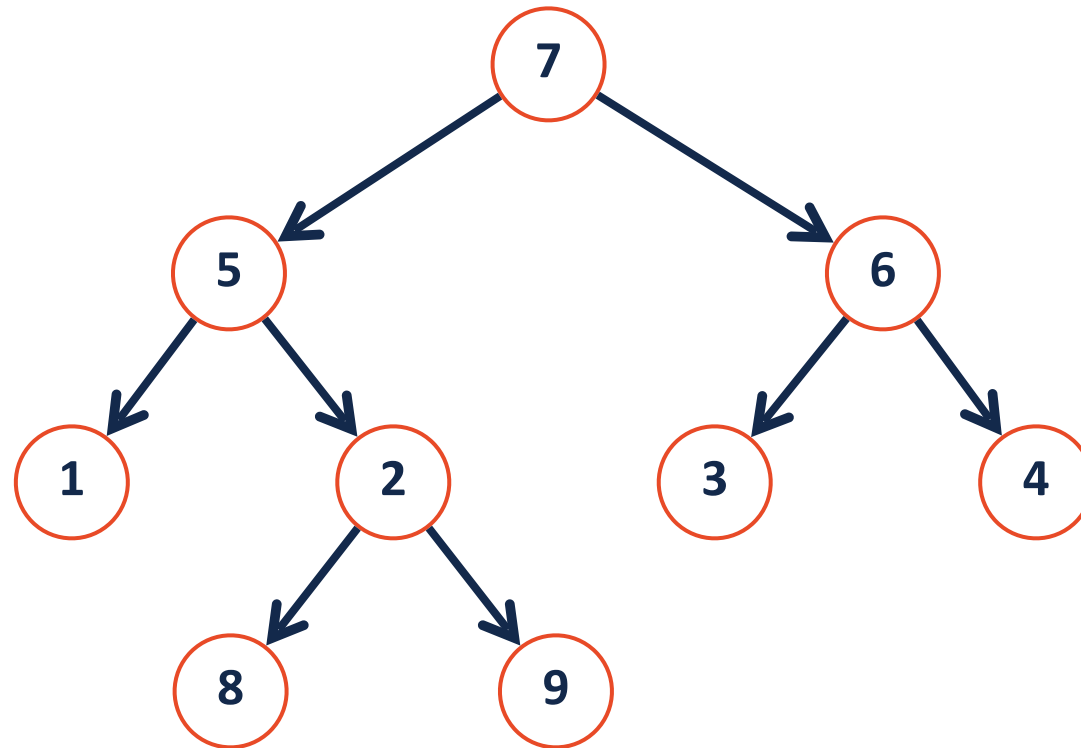
**Base Case:**

**Recursive Step:**

**Combining:**

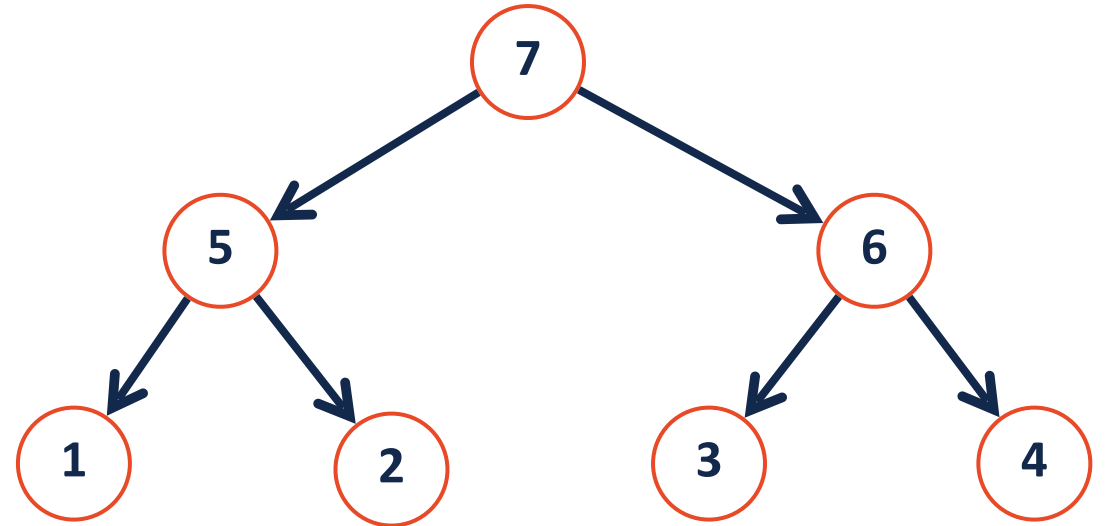
# Tree Traversals

A **traversal** of a tree  $T$  is an ordered way of visiting every node once.



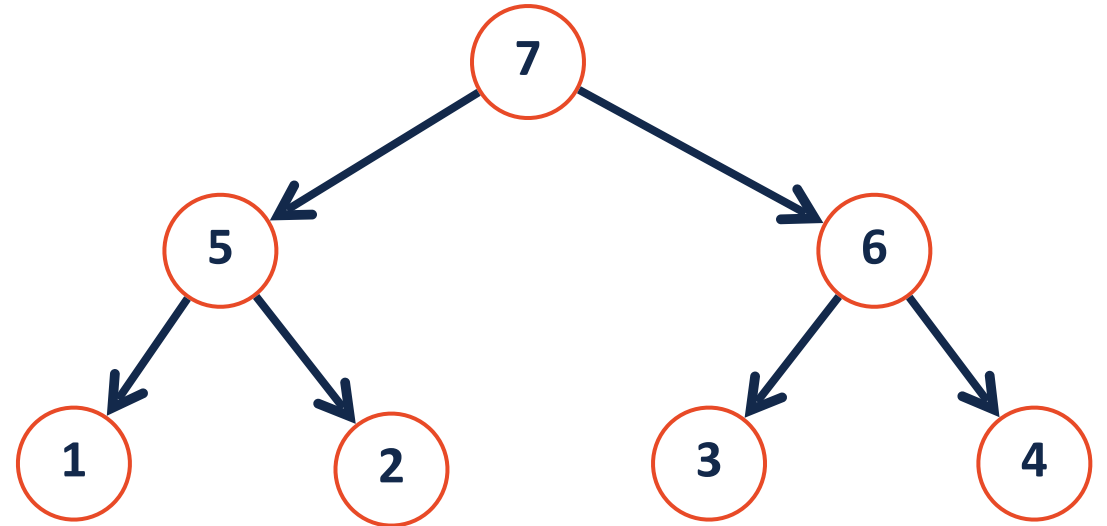
# Pre-Order Traversal

- 1) Get current node's value
- 2) Recurse left
- 3) Recurse right



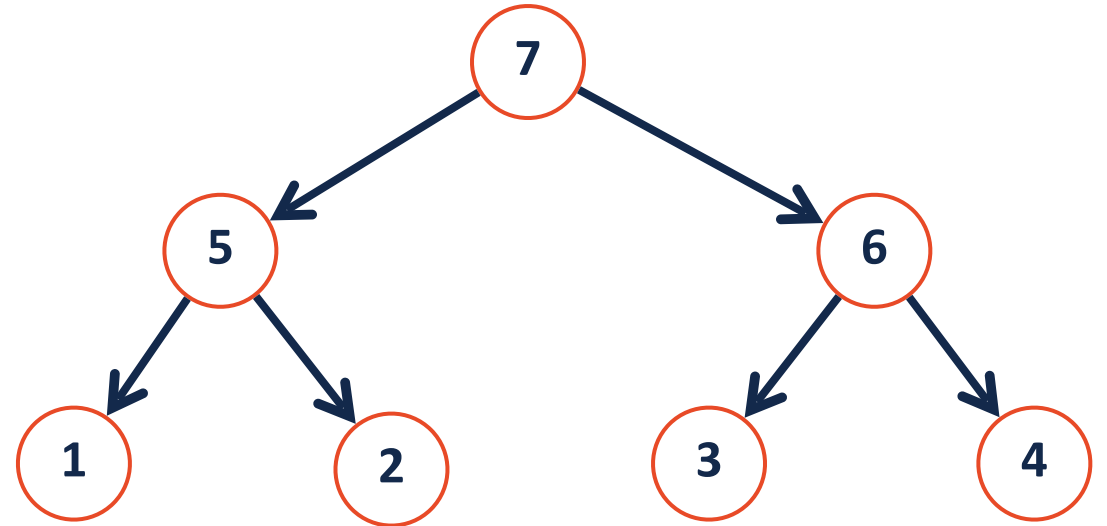
# Post-Order Traversal

- 1) Recurse left
- 2) Recurse right
- 3) Get current nodes value

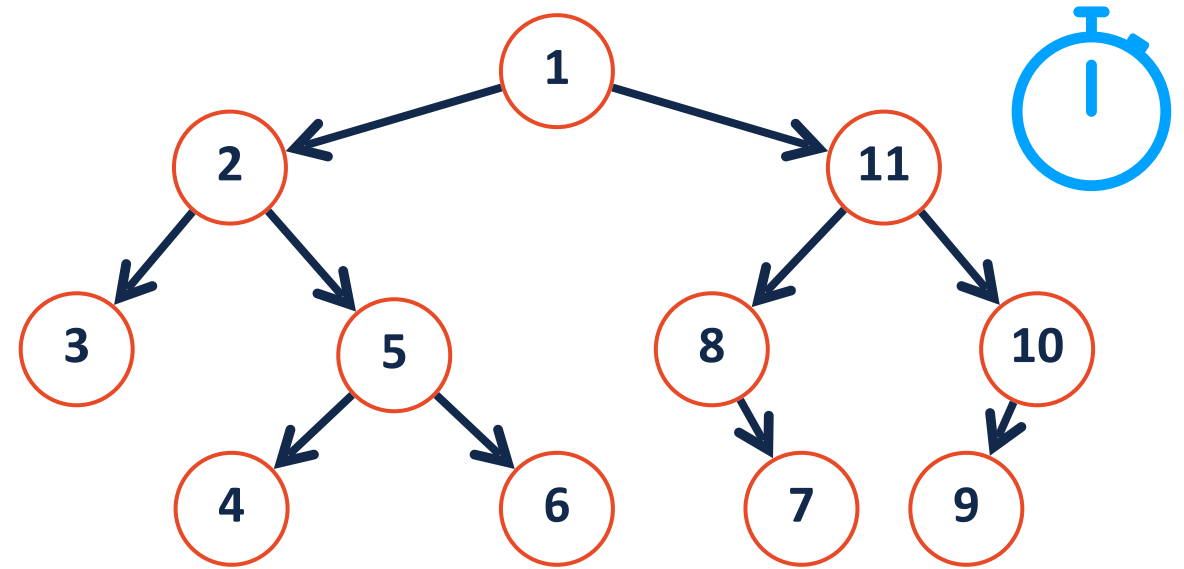


# In-Order Traversal

- 1) Recurse left
- 2) Get current nodes value
- 3) Recurse right



# Tree Traversals



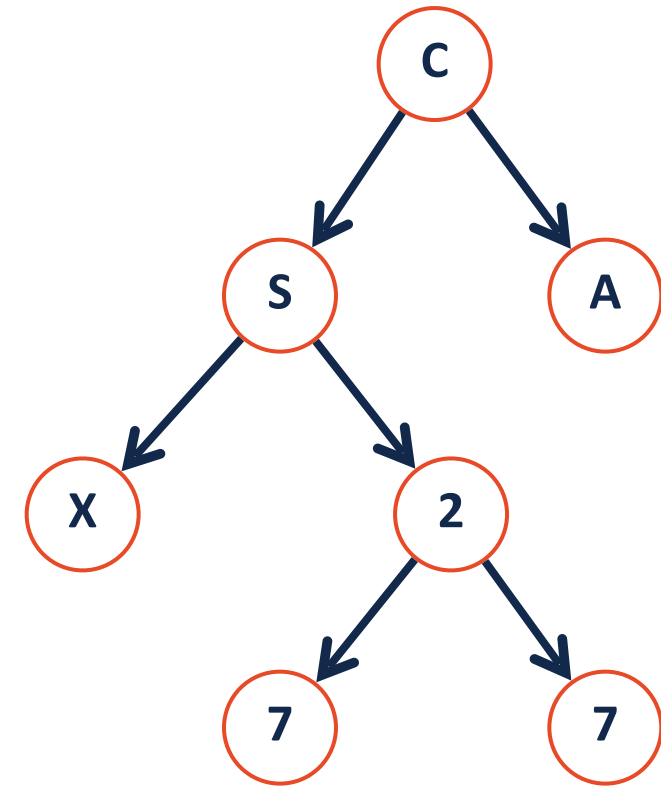
**Pre-order:**

**In-order:**

**Post-order:**

# Tree Traversals

**Pre-order:** Ideal for copying trees

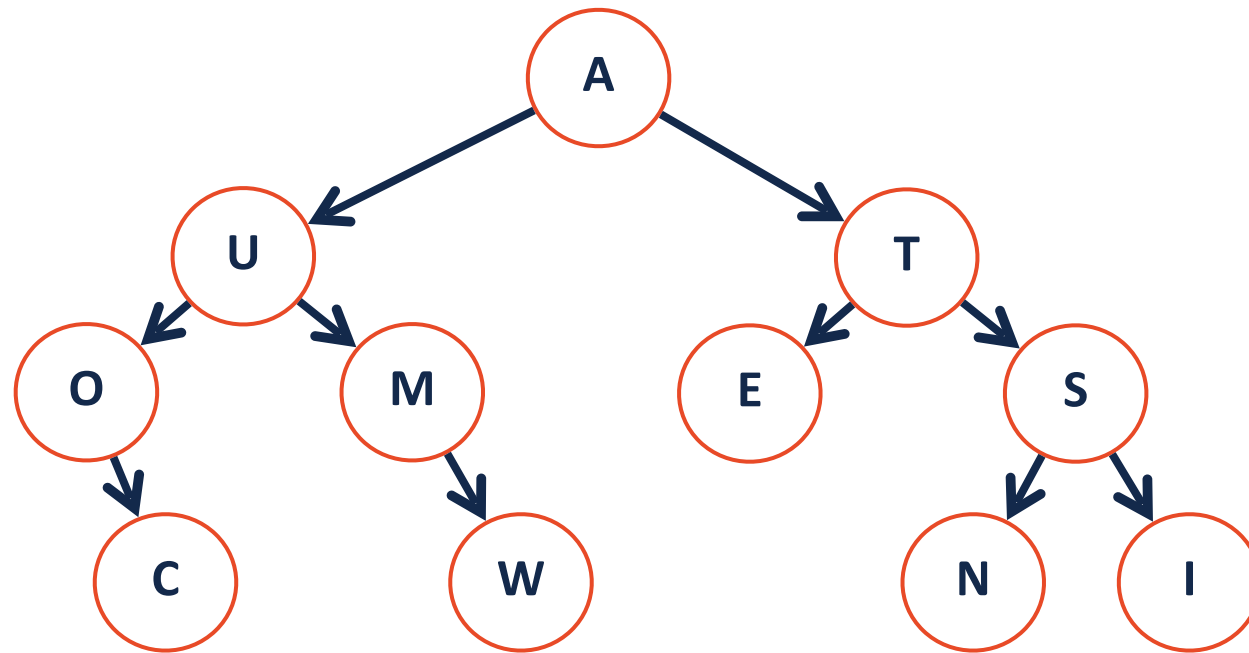


**Post-order:** Ideal for deleting trees



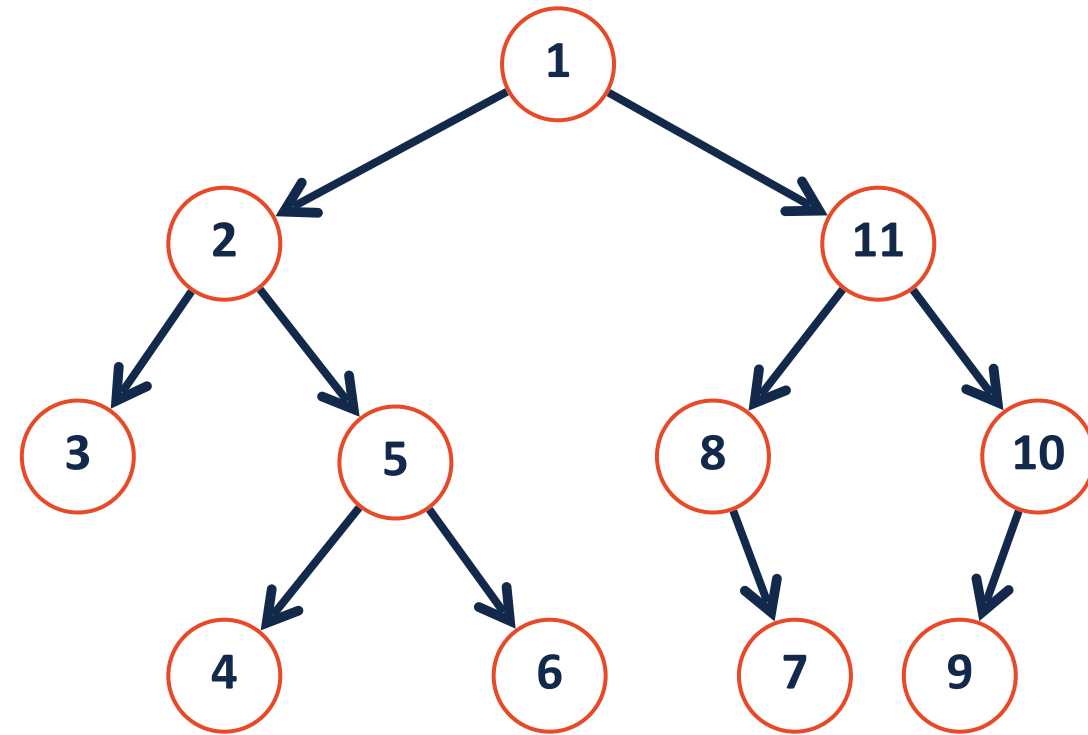
# Searching a Binary Tree

There are two main approaches to searching a binary tree:



# Depth First Search

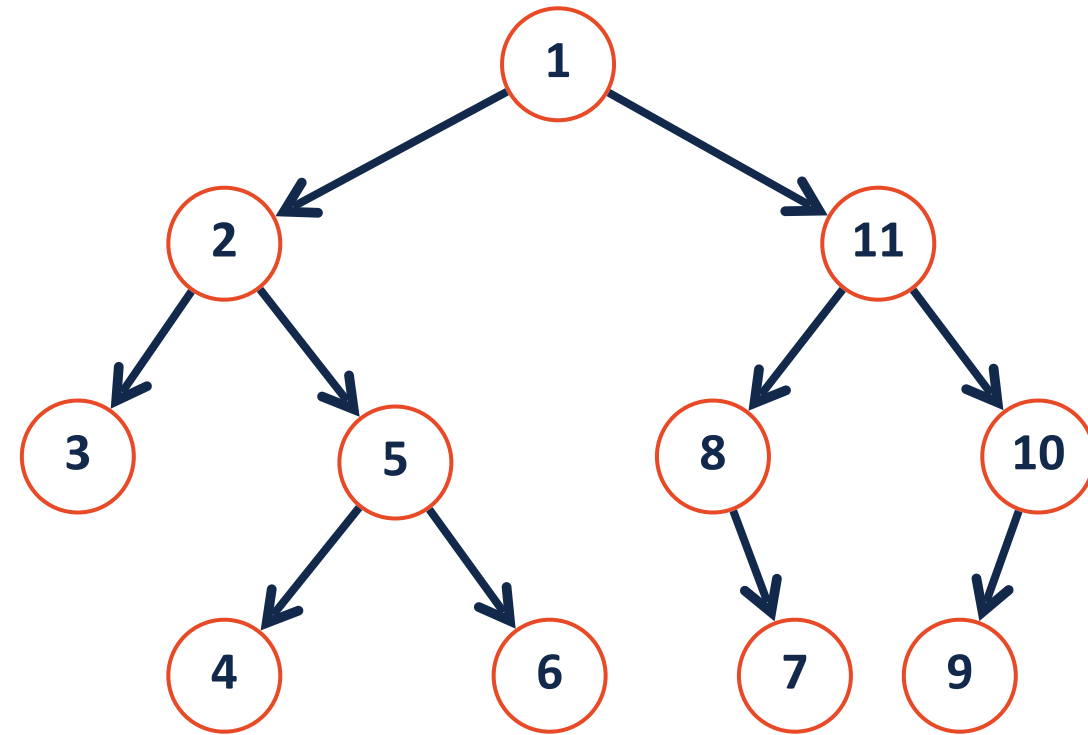
Explore as far along one path as possible before backtracking



# Breadth First Search



Fully explore depth  $i$  before exploring depth  $i+1$

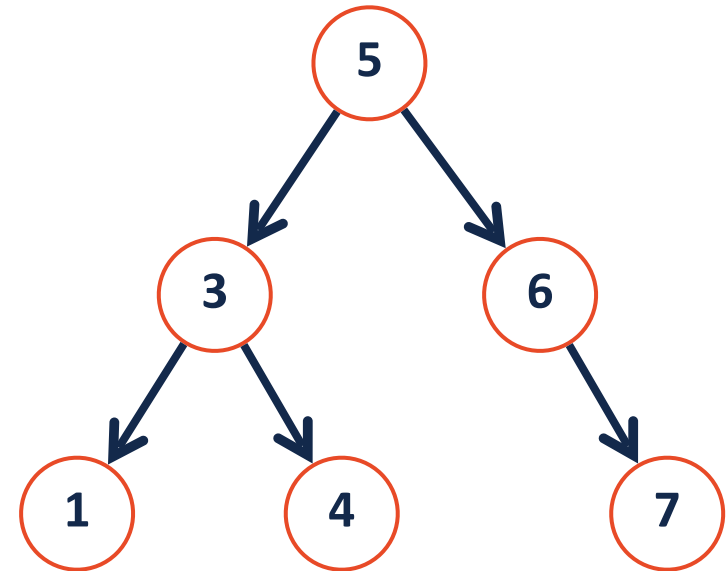
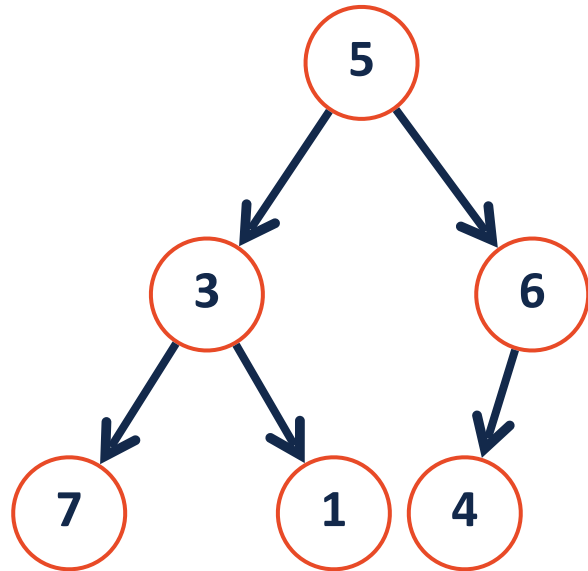
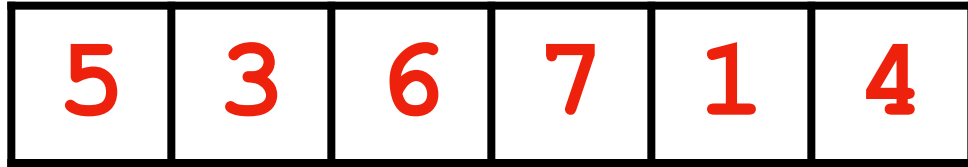


# What search algorithm is best?

The average 'branch factor' for a game of chess is  $\sim 31$ . If you were searching a decision tree for chess, which search algorithm would you use?



# Improved search on a binary tree



# Binary Search Tree (BST)

A **BST** is a binary tree  $T = treeNode(val, T_L, T_r)$  such that:

$\forall n \in T_L, n.val < T.val$

$\forall n \in T_R, n.val > T.val$

