

Algorithms and Data Structures for Data Science

Sorting

CS 277

September 27, 2021

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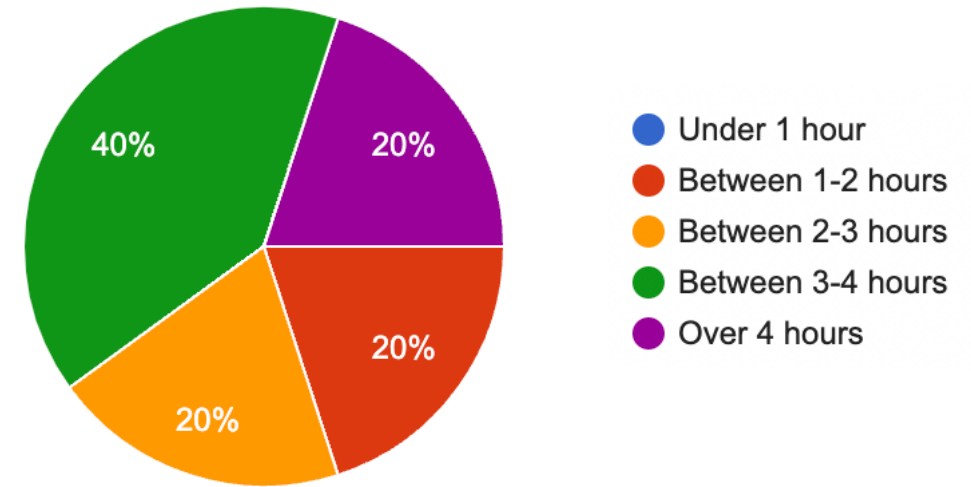
UNIVERSITY OF
ILLINOIS
URBANA - CHAMPAIGN

Department of Computer Science

Lab_hash Feedback

Average score: 82%

PL average time: 163 minutes



Material of neutral helpfulness to a sizable minority of students

Lab taught learning objectives and universally improved coding confidence

There *was* a problem with `double_hash` but it was resolved immediately



Learning Objectives

Motivate the need for sorting

Explore iterative solutions to sorting

Introduce recursion

The Sorting Problem

Given a collection of objects, C , with comparable values, order the objects such that $\forall x \in C, x_i \leq x_{i+1}$

Input:

8	4	3	1	2	5	6	9	0	7
---	---	---	---	---	---	---	---	---	---

Output:

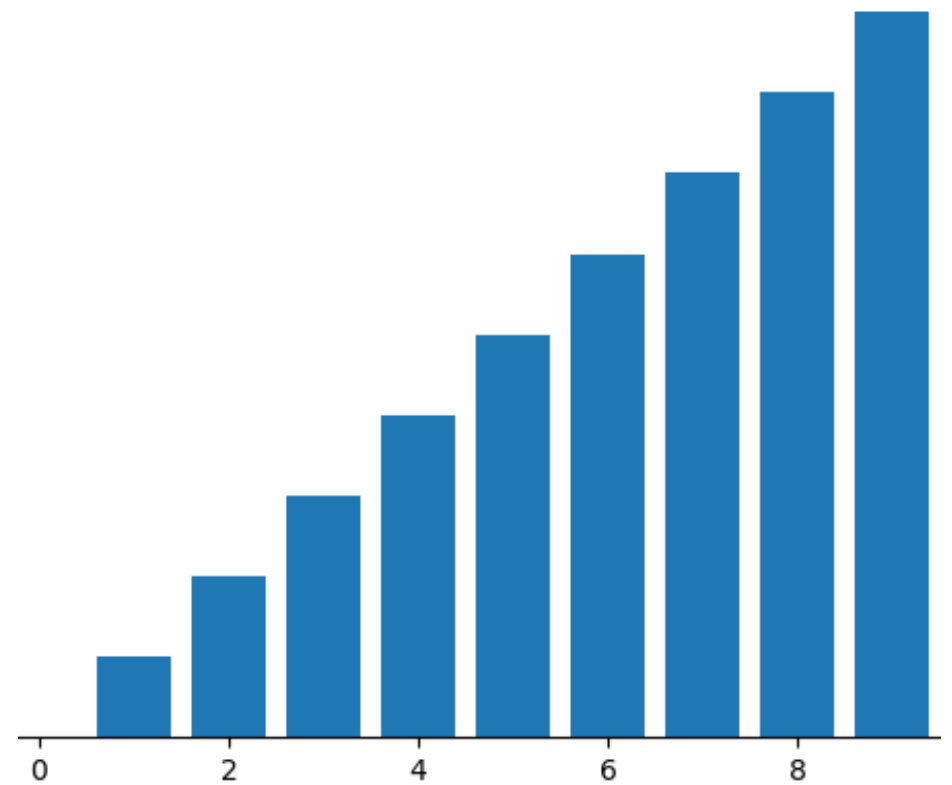
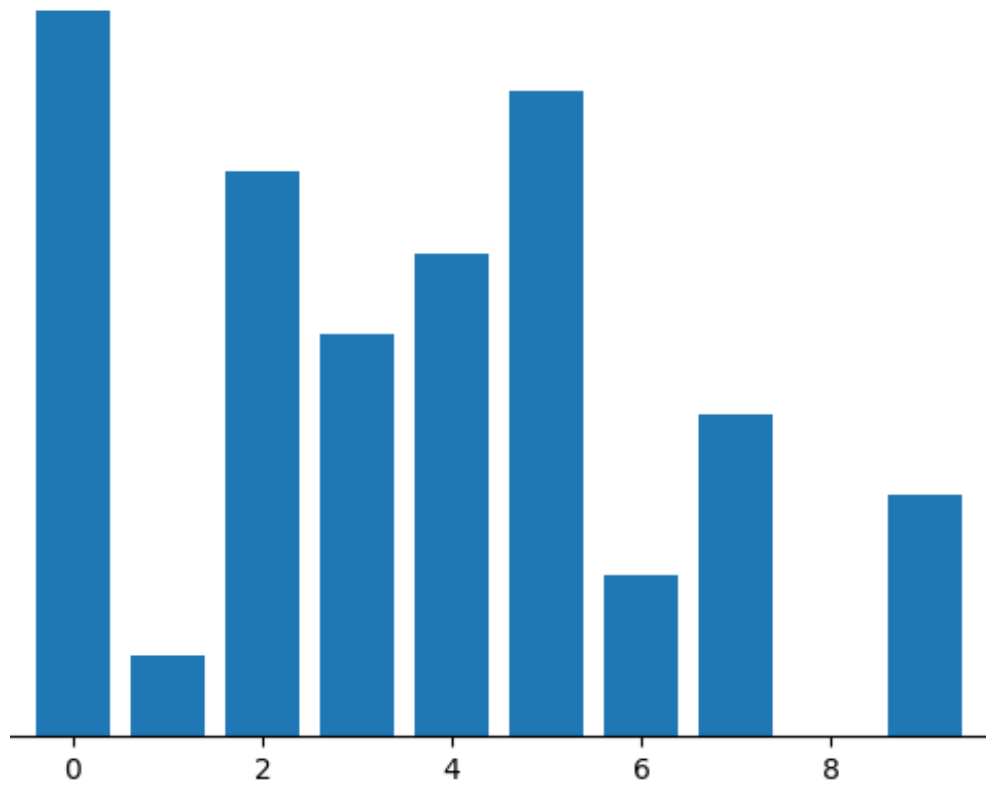
0	1	2	3	4	5	6	7	8	9
---	---	---	---	---	---	---	---	---	---

Sorting leads to efficient searching **Search (7)**

8	4	3	1	2	5	6	9	0	7
---	---	---	---	---	---	---	---	---	---

0	1	2	3	4	5	6	7	8	9
---	---	---	---	---	---	---	---	---	---

Sorting leads to better visualization



Sorting is a fundamental problem in CS

Many algorithms begin with or include a sorting step

Fundamental sorting algorithms are great for mastering concepts

Sorting algorithms are a classic introduction to algorithms

Optimizing sort is an ongoing challenge

GraySort: *Sort rate (TBs / minute)* achieved while sorting a very large amount of data (currently 100 TB minimum).

CloudSort: *Minimum cost (Dollars)* for sorting a very large amount of data on a public cloud. (currently 100 TB).

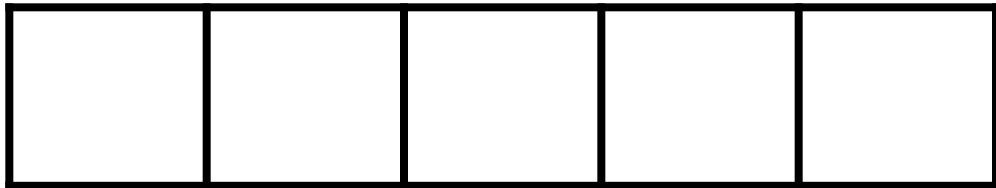
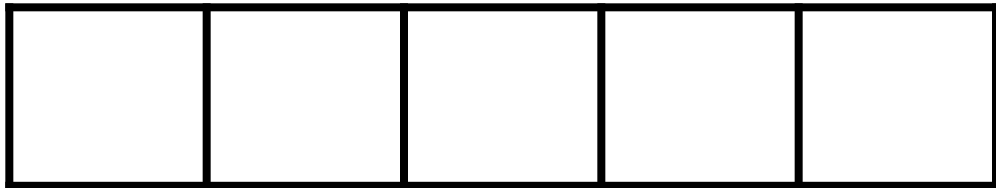
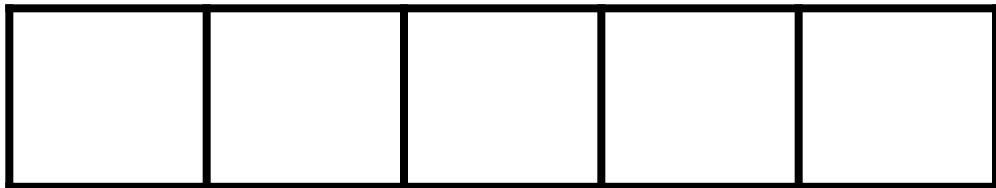
MinuteSort: *Amount of data* that can be sorted in 60 seconds or less.

TeraByteSort: *Elapsed time* to sort 1 TB of data

SelectionSort



```
1 def selectionSort(inList):
2     n = len(inList)
3
4     for i in range(n):
5         minindex = i
6         for j in range(i+1, n):
7             if inList[j] < inList[minindex]:
8                 minindex = j
9
10        inList[i], inList[minindex] = inList[minindex], inList[i]
```



InsertionSort

4	3	6	7	1
---	---	---	---	---

--	--	--	--	--

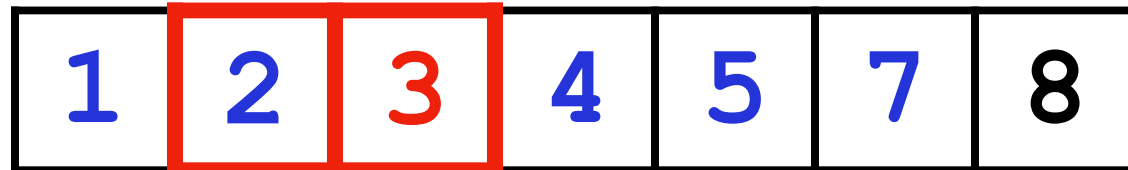
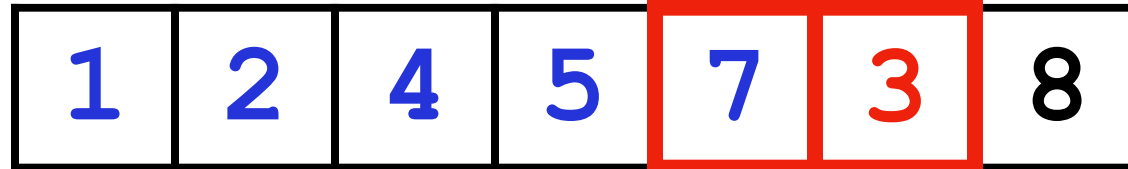
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--	--	--	--	--

1. Divide array into two parts
2. Insert the first unsorted item into the sorted position
3. Repeat until all items are sorted

InsertionSort "Insert"



InsertionSort

```
1 def insertionSort(inList):
2     n = len(inList)
3
4     for i in range(1, n):
5
6         val = inList[i]
7
8         j = i - 1
9         while j >= 0 and val < inList[j]:
10             inList[j+1]=inList[j]
11             j -= 1
12
13         inList[j+1]=val
```

8	6	3	1	0
---	---	---	---	---

1	2	3	4	5
---	---	---	---	---

Selection vs InsertionSort



Selection vs InsertionSort



Selection vs InsertionSort



```
1 def selectionSort(inList):
2     n = len(inList)
3
4     for i in range(n):
5         mindex = i
6         for j in range(i+1, n):
7             if inList[j] < inList[mindex]:
8                 mindex = j
9
10        inList[i], inList[mindex] =
11 inList[mindex], inList[i]
12
```

```
1 def insertionSort(inList):
2     n = len(inList)
3
4     for i in range(1, n):
5
6         val = inList[i]
7
8         j = i - 1
9         while j >= 0 and val < inList[j]:
10            inList[j+1]=inList[j]
11            j -= 1
12
13        inList[j+1]=val
```

Optimal Sorting

Claim: Any deterministic comparison-based sorting algorithm must perform $O(n \log n)$ comparisons to sort n objects.

0	1	2
---	---	---

1	0	2
---	---	---

2	0	1
---	---	---

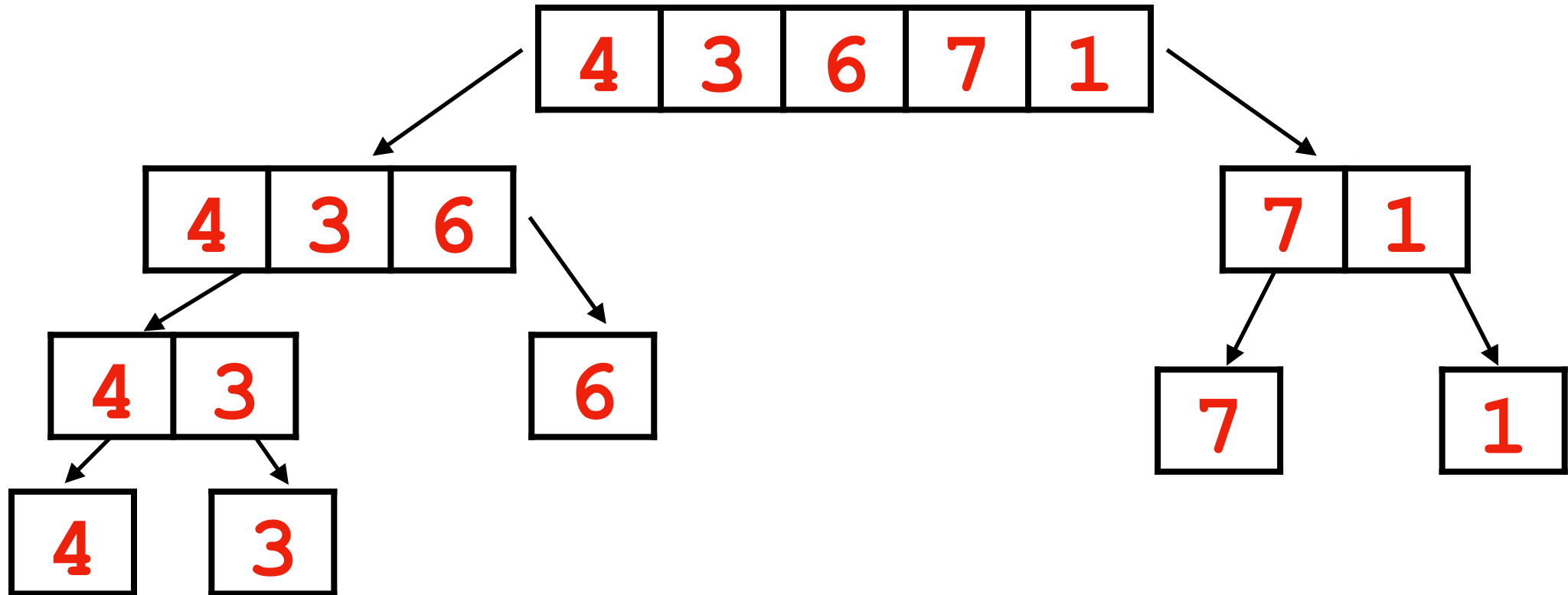
0	2	1
---	---	---

1	2	0
---	---	---

2	1	0
---	---	---

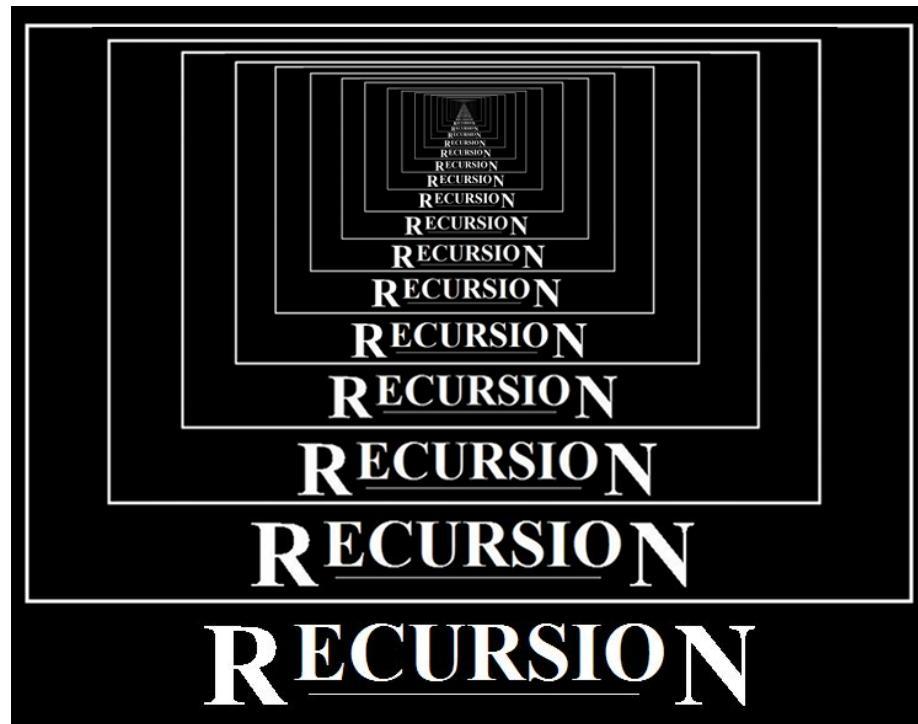
Divide and Conquer Algorithms

Recursively break a problem into sub-problems until the the problems become simple enough to solve directly



Recursion

*The process by which a function calls itself directly or indirectly is called **recursion**.*



Recursive For Loop

```
1 for i in range(n+1):  
2     print(i)
```

```
1 def recursiveFor(n):  
2     if n == 0:  
3         print(n)  
4         return  
5  
6     recursiveFor(n-1)  
7  
8     print(n)
```

```
1 def recursiveFor(n):  
2     if n == 0:  
3         print(0)  
4         return  
5  
6     print(n)  
7  
8     recursiveFor(n-1)
```

Recursive Sum

Given a list, sum all the items in the list *using recursion*

Base Case: What is the smallest sub-problem? What is the trivial solution?

Recursive Step: How can I reduce my problem to an easier one?

Combining: How can I build my solution from recursive pieces?

Recursive Sum

Given a list, sum all the items in the list *using recursion*

8	4	2	6	5
---	---	---	---	---

Recursive findMax

8	4	3	1	2	5	6	9	0	7
---	---	---	---	---	---	---	---	---	---

Base Case:

Recursive Step:

Combining:

Recursive Fibonacci



$$Fib(n) = Fib(n - 1) + Fib(n - 2), \quad n > 1$$

Base Case:

Recursive Step:

Combining:

Recursive List Partitioning

Using all elements in a list, can we make two lists which have equal sums?

6	5	4	2	7
---	---	---	---	---

1	1	1	1	1
---	---	---	---	---

2	3	3	3	1
---	---	---	---	---

Recursive List Partitioning

Using all elements in a list, can we make two lists which have equal sums?

Base Case:

Recursive List Partitioning

Using all elements in a list, can we make two lists which have equal sums?

Recursive Step:

Recursive List Partitioning

Using all elements in a list, can we make two lists which have equal sums?

(New) Base Case:

Recursive List Partitioning

Using all elements in a list, can we make two lists which have equal sums?

Combination Step:

Recursive List Partitioning

Using all elements in a list, can we make two lists which have equal sums?

4	3	1
---	---	---

Using all elements in a list, can we make two lists which have equal sums?

Input

[4, 3, 1] ([], [])

[3, 1] ([4], []) ([], [4])

[1] ([3, 4], []) ([4], [3]) ([3], [4]) ([], [3, 4])

[]

([1, 3, 4], []) ([1, 4], [3]) ([1, 3], [4]) ([1], [3, 4])

([3, 4], [1]) ([4], [1, 3]) ([3], [1, 4]) ([], [1, 3, 4])

Recursive Array Sorting



0	3	7	5	8	9	2	1	4	6
---	---	---	---	---	---	---	---	---	---

Base Case:

Recursive Step:

Combining: