

1. (a) The Loop has 10 instructions and 64 iterations of the loop are executed. Clearly, the number of instructions executed in course of program execution = $(64 \times 10) + 1$ (for the first instruction of program before the loop) = **641**
- (b) Assume that vectors A, B and C are stored in main memory, and their addresses are in registers \$t0, \$t1 and \$t2, respectively.

```

# i=0
lw    $t3, 0($t1)      # $t3 = b[0]
lw    $t4, 0($t2)      # $t4 = c[0]
add   $t4, $t3, $t4    # $t4 = b[0] + c[0]
sw    $t4, 0($t0)      # a[0] = b[0] + c[0]

# i=1
lw    $t3, 4($t1)      # $t3 = b[1]
lw    $t4, 4($t2)      # $t4 = c[1]
add   $t4, $t3, $t4    # $t4 = b[1] + c[1]
sw    $t4, 4($t0)      # a[1] = b[1] + c[1]
.....
.....
.....
# i=63
lw    $t3, 252($t1)    # $t3 = b[63]
lw    $t4, 252($t2)    # $t4 = c[63]
add   $t4, $t3, $t4    # $t4 = b[63] + c[63]
sw    $t4, 252($t0)    # a[63] = b[63] + c[63]

```

This pattern would be repeated for all values of $i < 64$. Notice how loop unrolling gets rid of the branch maintenance code, instructions such as `slti`, `bne` and the overhead of maintaining the loop index is also removed.

- (c) Each iteration of the loop would require writing 4 instructions as shown above. So the length of entire unrolled code = $(4 \times 64) = \mathbf{256 \text{ instructions}}$.
- (d) Loop code that has been unrolled by a factor of 2:

```

      add    $t4, $zero, $zero    # I1  i is initialized to 0, $t4 = 0
Loop:
      add    $a1, $t4, $t1        # UPDATE ADDRESS REGISTERS
      add    $a2, $t4, $t2        # I2  temp reg $a1 = address of b[i]
      add    $a0, $t4, $t0        # I3  temp reg $a2 = address of c[i]
                                      # I4  temp reg $a0 = address of a[i]
      lw     $t6, 0($a1)          # FIRST ADDITION
      lw     $t7, 0($a2)          # I5  temp reg $t6 = b[i]
      add    $t6, $t6, $t7        # I6  temp reg $t7 = c[i]
      sw     $t6, 0($a0)          # I7  temp reg $t6 = b[i] + c[i]
                                      # I8  a[i] = b[i] + c[i]
      lw     $t6, 4($a1)          # SECOND ADDITION
      lw     $t7, 4($a2)          # I9  temp reg $t6 = b[i + 1]
      add    $t6, $t6, $t7        # I10 temp reg $t7 = c[i + 1]
      sw     $t6, 4($a0)          # I11 temp reg $t6 = b[i + 1] + c[i + 1]
                                      # I12 a[i + 1] = b[i + 1] + c[i + 1]

```

```
                                # LOOP CODE
addi    $t4, $t4, 8             # I13 i = i + 8
slti    $t5, $t4, 256          # I14 $t5 = 1 if $t4 < 256, i.e. i < 64
bne     $t5, $zero, Loop       # I15 go to Loop if i < 256
```

- (e) Each unrolling adds 4 instructions (2 loads, an add, and a store) to the static program:

static program size = 11 instructions + (4 instructions \times (unrolling_factor - 1))

Each unrolling halves the number of overhead instructions executed:

number of instructions executed = $1 + (4 \times 64) + \left(\frac{6 \times 64}{\text{unrolling_factor}}\right)$