CS 225

Data Structures

February 17 – BST Balance G Carl Evans

Height-Balanced Tree

What tree makes you happier?



A tree is height balanced if:

BST Rotation

We will perform a rotation that maintains two properties: **1**.

2.

















BST Rotation Summary

- Four kinds of rotations (L, R, LR, RL)
- All rotations are local (subtrees are not impacted)
- All rotations are constant time: O(1)
- BST property maintained

GOAL:

We call these trees:

AVL Trees

Three issues for consideration:

- Rotations
- Maintaining Height
- Detecting Imbalance

AVL Tree Rotations

Four templates for rotations:



Finding the Rotation on Insert



Theorem:

If an insertion occurred in subtrees t_3 or t_4 and a subtree was detected at t, then a ______ rotation about t restores the balance of the tree.

We gauge this by noting the balance factor of **t->right** is _____.

Finding the Rotation on Insert



Theorem:

If an insertion occurred in subtrees t_2 or t_3 and a subtree was detected at t, then a ______ rotation about t restores the balance of the tree.

We gauge this by noting the balance factor of **t->right** is _____.

Insertion into an AVL Tree

_insert(6.5)



_insert(6.5)

Insertion into an AVL Tree

Insert (pseudo code):

- 1: Insert at proper place
- 2: Check for imbalance
- 3: Rotate, if necessary
- 4: Update height



1	<pre>struct TreeNode {</pre>
2	T key;
3	unsigned height;
4	TreeNode *left;
5	TreeNode *right;
6	};