## Combining bloom filters

Given the following bloom filters, write a bloom filter which contains all the items present in both filters.

|  | $[0]$ | $\mathbf{O}$ | $[0]$ | $\mathbf{O}$ | $[0]$ |
| :---: | :---: | :--- | :--- | :--- | :--- |
| $[1]$ | $\mathbf{1}$ | ${ }^{[1]}$ | $\mathbf{1}$ | $[1]$ |  |
| $[2]$ | $\mathbf{1}$ | ${ }^{[2]}$ | $\mathbf{O}$ | $[2]$ |  |
| $[3]$ | $\mathbf{O}$ | $[3]$ | $\mathbf{O}$ | $[3]$ |  |
| $[4]$ | $\mathbf{1}$ | $[4]$ | $\mathbf{1}$ | $[4]$ |  |
| $[5]$ | $\mathbf{O}$ | $[5]$ | $\mathbf{1}$ | $[5]$ |  |
| $[6]$ | $\mathbf{O}$ | $[6]$ | $\mathbf{O}$ | $[6]$ |  |

## Sequence Bloom Trees

Given the bit vectors (1010), (0010), (0001), and (0101), draw a sequence bloom tree that stores all vectors as leaves. Consider how the arrangement of leaves can affect the usefulness of the tree!

## Counting Bloom Filter: Insertion

Construct a counting BF. $\mathbf{S}=\{\mathbf{1 6}, \mathbf{8}, \mathbf{4}, \mathbf{1 3}, \mathbf{2 9}, \mathbf{1 1}, 22\}$, $\mathbf{h 1}(\mathbf{k})=\mathbf{k} \% \mathbf{7}, \mathbf{h 2}(\mathbf{k})=\mathbf{2 k + 1} \% 7$

|  |  |
| :---: | :--- |
| $[0]$ |  |
| $[1]$ |  |
| $[2]$ |  |
| $[3]$ |  |
| $[4]$ |  |
| $[5]$ |  |
| $[6]$ |  |

## Counting Bloom Filter: Deletion

Which of the following items cannot be deleted at least once?
$\mathbf{S}=\{\mathbf{o}, \mathbf{1}, \mathbf{2}, \mathbf{3}, \mathbf{4}\}, \mathbf{h}(\mathbf{k})=\mathbf{k} \% \mathbf{5}$,

|  | $\mathbf{5}$ |
| :---: | :---: |
| $[1]$ | $\mathbf{2}$ |
| $[2]$ | $\mathbf{1}$ |
| $[3]$ | $\mathbf{3}$ |
| $[4]$ | $\mathbf{7}$ |

What is the downside to allowing deletion?

## CBF: Minimal Increase

If X hashes to indices $\mathrm{o}, 2$, and 3 what is our best estimate of X 's current count? How can we adjust insertion to take that into account?

|  | $\mathbf{3}$ |
| :---: | :---: |
| $[1]$ | $\mathbf{4}$ |
| $[2]$ | $\mathbf{2}$ |
| $[3]$ | $\mathbf{1}$ |
| $[4]$ | $\mathbf{4}$ |
| $[5]$ | $\mathbf{6}$ |
| $[6]$ | $\mathbf{8}$ |

## CBF: Recurring Minimum

In the above example, X only has a single minimum value. What does this mean and what can we do to improve our accuracy for counting the frequency of $X$ ?

## Cardinality

Cardinality is a measure of:

## Cardinality Estimation

If I randomly sampled values from $0-1000$ (no repeats) and told you that the minimum value was 300 , what is your best estimate for the cardinality in the random set?

What if the minimum value was 20 ?

## K-minimum Estimation

Will the k-th minimum give me a better, worse, or the same estimation accuracy as the minimum? Why?

## CS 225 - Things To Be Doing:

1. Continue working on mp _schedule
2. Either work on your final project or prepare for final exam
