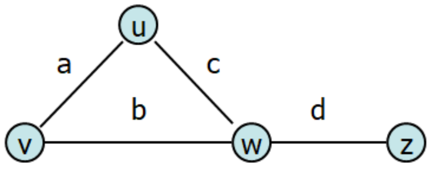
#28: Graph Implementation

March 30, 2022 · *G Carl Evans*

Graph Implementation #1: Edge List

Vert.	Edges
u	
v	
w	
z	

		a
		b
		c
		d



Data Structures:

Vertex Collection:

Edge Collection:

Operations on an Edge List implementation:

insertVertex(K key):
- What needs to be done?

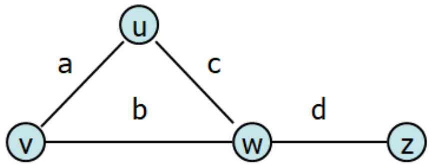
removeVertex(Vertex v):
- What needs to be done?

incidentEdges(Vertex v):
- What needs to be done?

areAdjacent(Vertex v1, Vertex v2):
- Can this be faster than **`G.incidentEdges(v1).contains(v2)`**?

insertEdge(Vertex v1, Vertex v2, K key):
- What needs to be done?

Graph Implementation #2: Adjacency Matrix



Vert.	Edges	Adj. Matrix
u		
v		
w		
z		

		a
		b
		c
		d

▩	u	v	w	z
u				
v				
w				
z				

Data Structures:

Operations on an Adjacency Matrix implementation:

insertVertex(K key):
- What needs to be done?

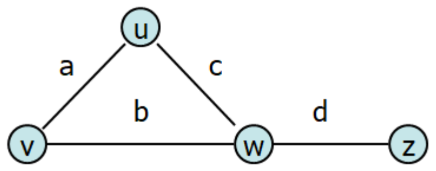
removeVertex(Vertex v):
- What needs to be done?

incidentEdges(Vertex v):
- What needs to be done?

areAdjacent(Vertex v1, Vertex v2):
- Can this be faster than **`G.incidentEdges(v1).contains(v2)`**?

insertEdge(Vertex v1, Vertex v2, K key):
- What needs to be done?

Graph Implementation #3: Adjacency List



Vertex List	Edges		
u			a
v			b
w			c
z			d

Operations on an Adjacency Matrix implementation:

insertVertex(K key):

removeVertex(Vertex v):

incidentEdges(Vertex v):

areAdjacent(Vertex v1, Vertex v2):

insertEdge(Vertex v1, Vertex v2, K key):

Running Times of Classical Graph Implementations

	Edge List	Adj. Matrix	Adj. List
Space	**n+m**	**n^2**	**n+m**
insertVertex	**1**	**n**	**1**
removeVertex	**m**	**n**	**deg(v)**
insertEdge	**1**	**1**	**1**
removeEdge	**1**	**1**	**1**
incidentEdges	**m**	**n**	**deg(v)**
areAdjacent	**m**	**1**	**min(deg(v), deg(w))**

Q: If we consider implementations of simple, connected graphs, what relationship between n and m?

- On connected graphs, is there one algorithm that underperforms the other two implementations?

Q: Is there clearly a single best implementation?

- Optimized for fast construction:

- Optimized for areAdjacent operations:

CS 225 – Things To Be Doing:

1. mp_mazes AMA tonigt at 8pm
2. lab_btree starts today
3. Weekly Development Log starts this week
4. POTD today!