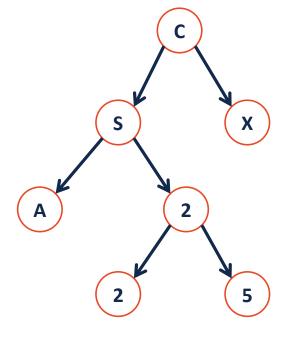
CS 225

Data Structures

February 21 – Trees G Carl Evans

Binary Tree – Defined A *binary tree* T is either:

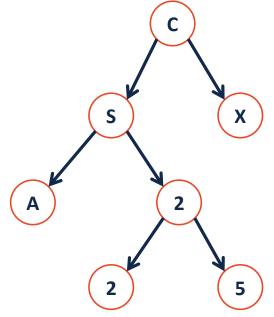
OR



Tree Property: height

height(T): length of the longest path
from the root to a leaf

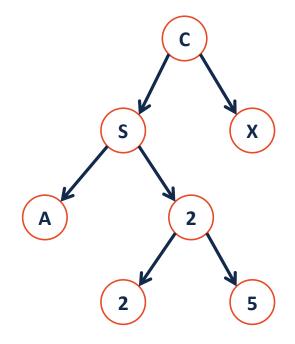
Given a binary tree T:



height(T) =

Tree Property: full A tree F is full if and only if:

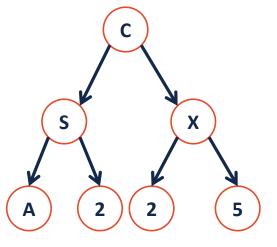
- 1.
- 2.



Tree Property: perfect

A **perfect** tree **P** is defined in terms of the tree's height.

Let **P**_h be a perfect tree of height **h**, and:



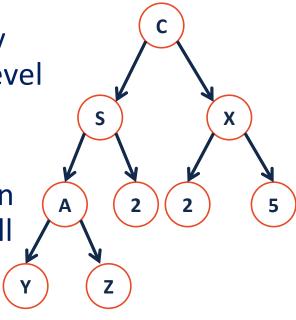
1.

2.

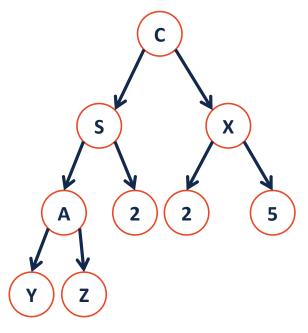
Tree Property: complete

Conceptually: A perfect tree for every level except the last, where the last level if "pushed to the left".

Slightly more formal: For all levels k in [0, h-1], k has 2^k nodes. For level h, all nodes are "pushed to the left".

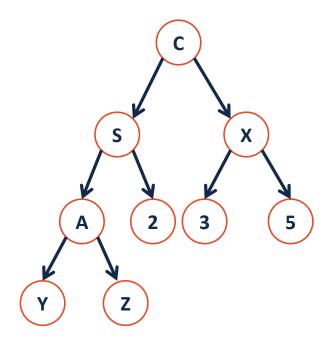


Tree Property: complete A complete tree C of height h, C_h : 1. $C_1 = \{\}$ 2. C_h (where h > 0) = {r, T_L , T_R } and either: T_L is ______ and T_R is _____ OR T_L is ______ and T_R is _____



Tree Property: complete Is every full tree complete?

If every **complete** tree **full**?



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1. Understand the problem, don't just give up.

- "I segfaulted" is not enough. Where? Any idea why?

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2. Your topic must be specific to one function, one test case, or one exam question.

- Helps us know what to focus on before we see you!
- Helps your peers to ensure all get questions answered!

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3. Get stuck, get help – not the other way around.
- If you immediately re-add yourself, you're setting yourself up for failure.

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4. Be awesome.

Tree ADT

Tree ADT

insert, inserts an element to the tree.

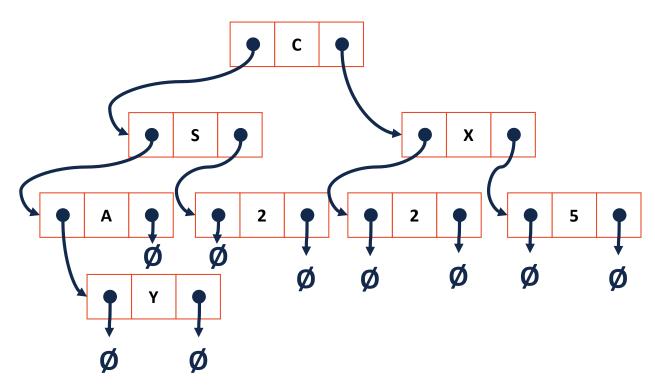
remove, removes an element from the tree.

traverse,

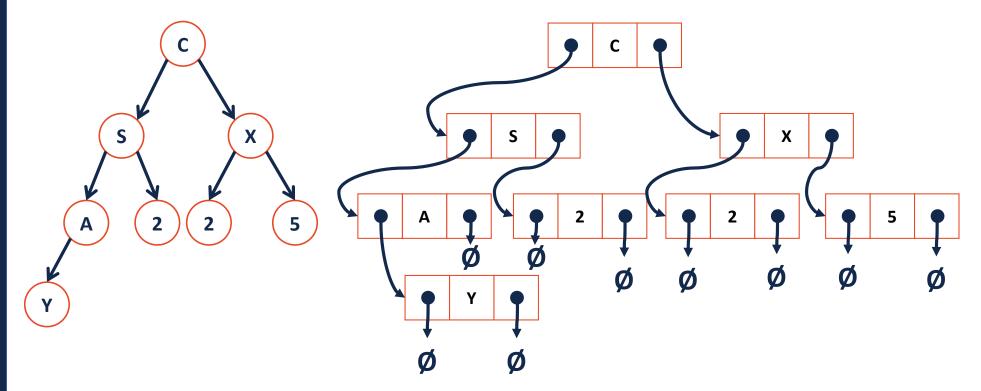
BinaryTree.h

```
#pragma once
 1
 2
 3
   template <class T>
   class BinaryTree {
 4
     public:
    /* ... */
 5
 6
 7
 8
     private:
 9
10
11
12
13
14
15
16
17
18
19 };
```

Trees aren't new:



Trees aren't new:



Theorem: If there are **n** data items in our representation of a binary tree, then there are ______ NULL pointers.

Base Cases:

n = 0:

n = 1:

n = 2:

Induction Hypothesis:

Consider an arbitrary tree **T** containing **n** data elements:

Traversals

