

CS 225

Data Structures

Feb. 26 – BST Balance

Wade Fagen-Ulmschneider

Course Logistics Update

CBTF exams will go on as-scheduled:

- Theory Exam 2 starts tomorrow
- Sample Exam available on PL

MPs and Lab assignments will be released on schedule:

- MP3 is due tonight (11:59pm)
- MP4 will be released tomorrow
- lab_huffman will be released on Wednesday

We'll chat about additional logistics on Wednesday regarding lab sections (*if necessary*)

Interactive Lecture Questions

- **Ask Questions:** Ask in-lecture questions using [this Google Form!](#) Questions are reviewed and answered live during lecture.
- **Detailed Answers After Lecture:** If we didn't get to answer your question in lecture, we provide detailed answers to common questions [here](#)>.
- You must be logged in with an account to use the interactive tab and be asked to log in.

Lecture Videos

- Recorded on [echo360.org](#), log

Schedule

Monday

January 15
MLK Day

January 22
Memory

[slides](#) | [handout](#) | [pointers.pdf](#) | [code](#) | [TA Notes](#)

[slides](#) | [handout](#) | [Binky Pointer Fun](#) | [code](#) | [TA Notes](#)

[slides](#) | [handout](#) | [arrays.pdf](#) | [parameters](#) | [code](#) | [TA Notes](#)

CS 225 - Lecture Questions

Your email address ([waf@illinois.edu](#)) will be recorded when you submit this form. Not you? [Switch account](#)

* Required

Question for Lecture: *

Your answer

SUBMIT

Never submit passwords through Google Forms.

BST Analysis

Therefore, for all BST:

Lower bound: $O(\lg(n))$

Upper bound: $O(n)$

BST Analysis

The height of a BST depends on the order in which the data is inserted into it.

ex: 1 3 2 4 5 7 6

vs.

4 2 3 6 7 1 5

Q: How many different ways are there to insert keys into a BST?

Q: What is the average height of all the arrangements?

BST Analysis

Q: How many different ways are there to insert keys into a BST?

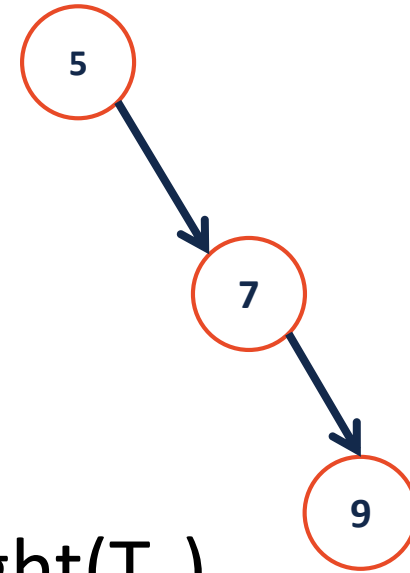
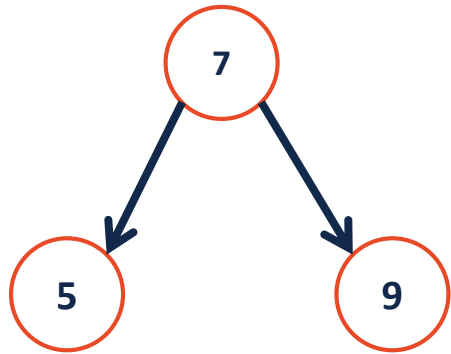
Q: What is the average height of all the arrangements?

BST Analysis – Running Time

Operation	BST Average case	BST Worst case	Sorted array	Sorted List
find				
insert				
delete				
traverse				

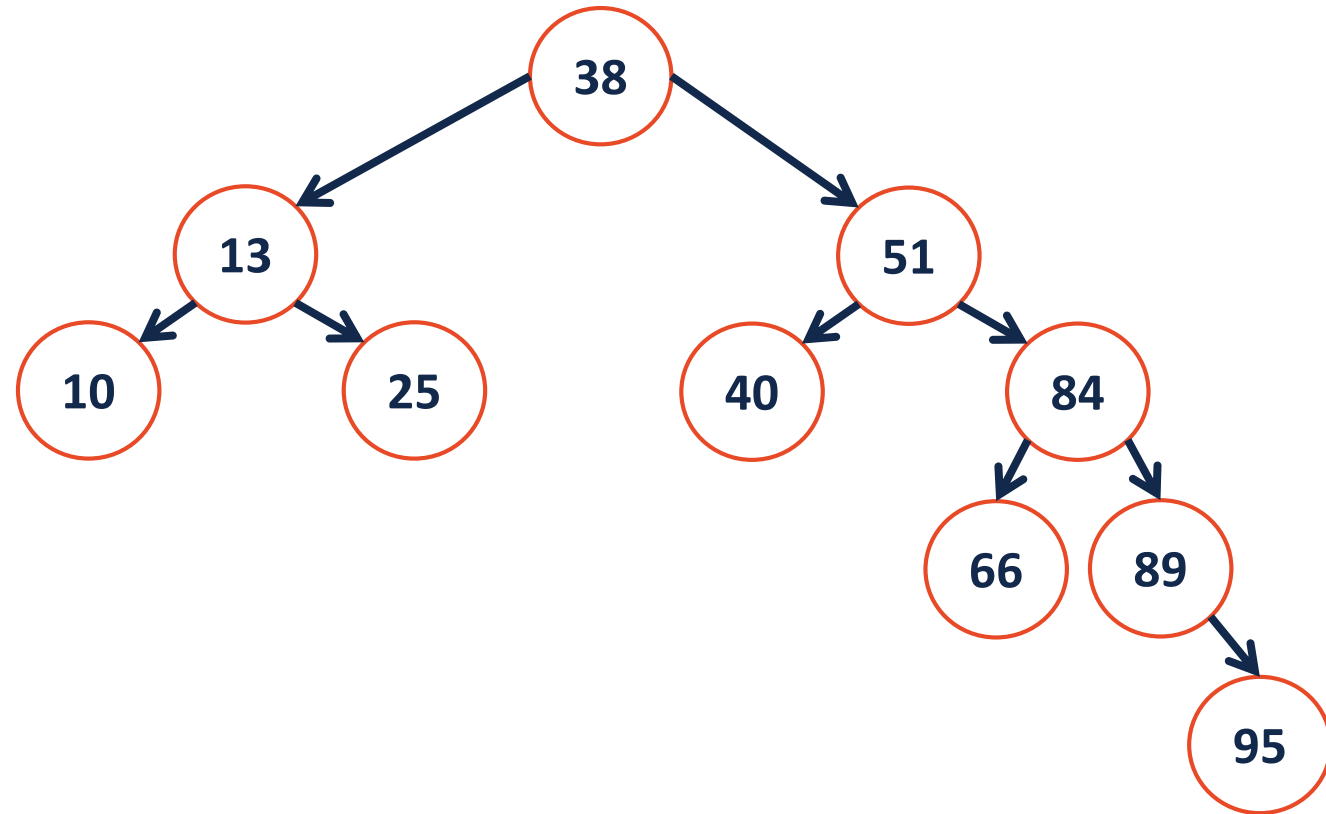
Height-Balanced Tree

What tree makes you happier?



Height balance: $b = \text{height}(T_L) - \text{height}(T_R)$

A tree is height balanced if:

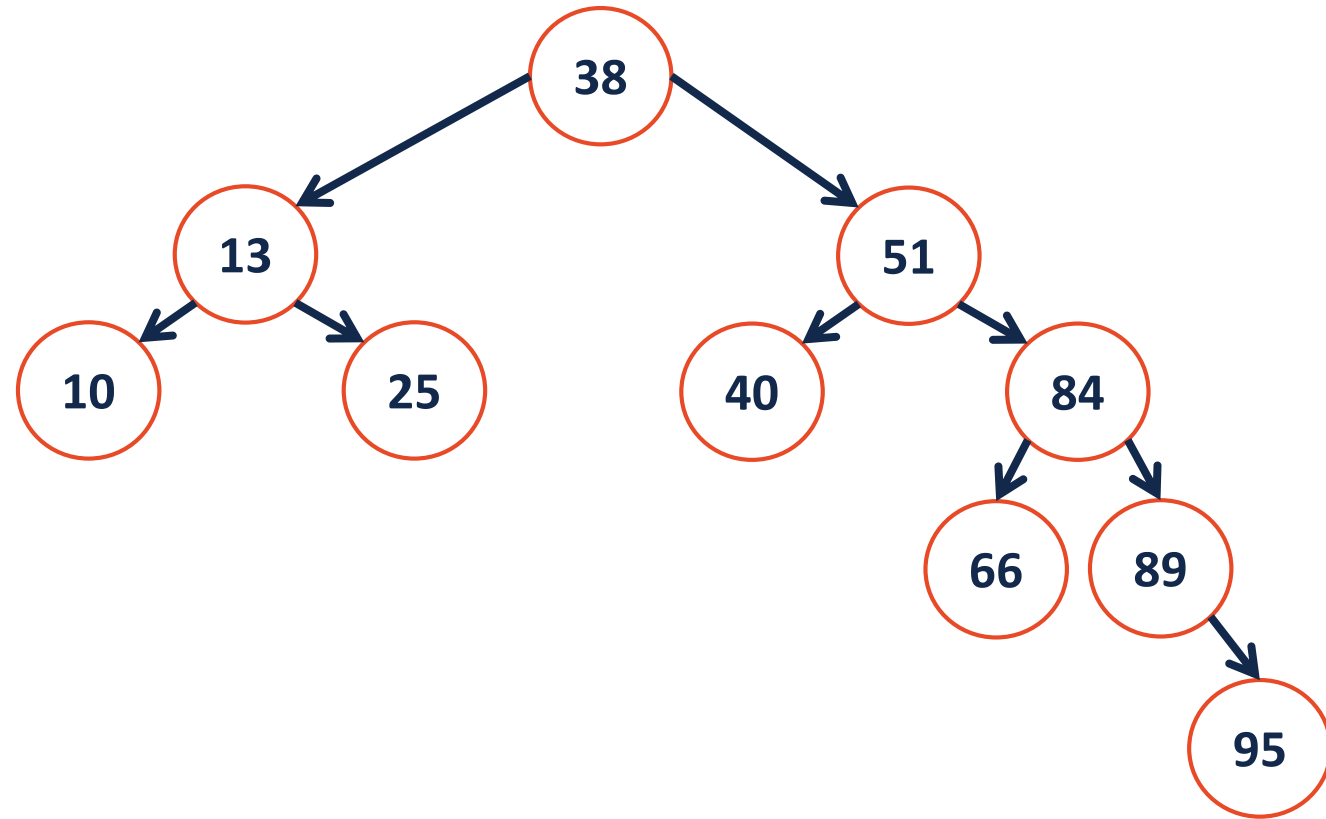


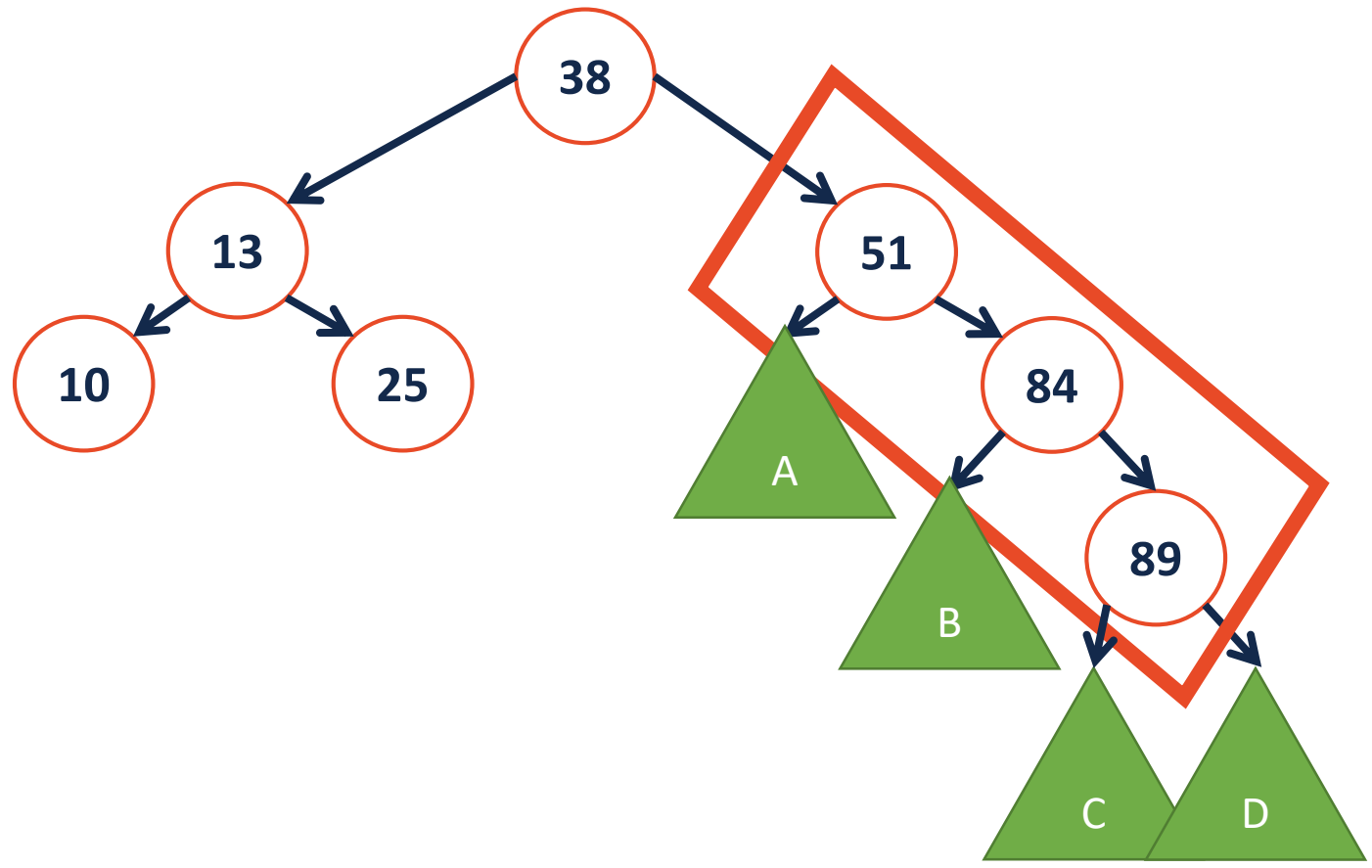
BST Rotation

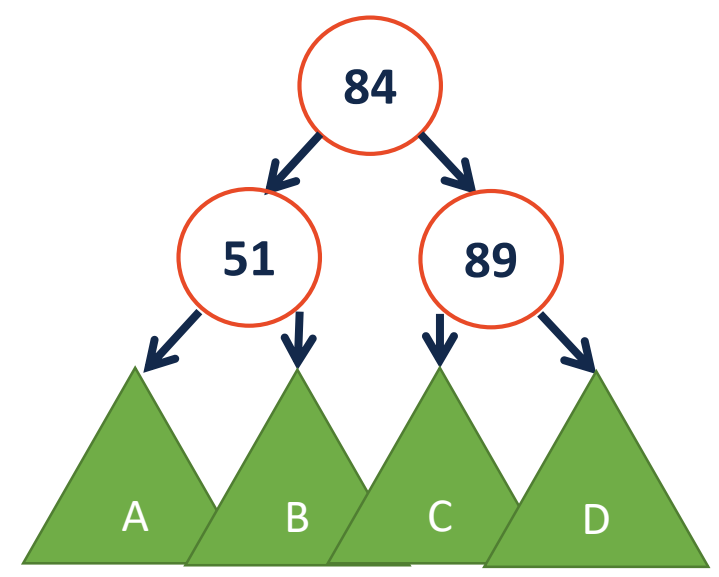
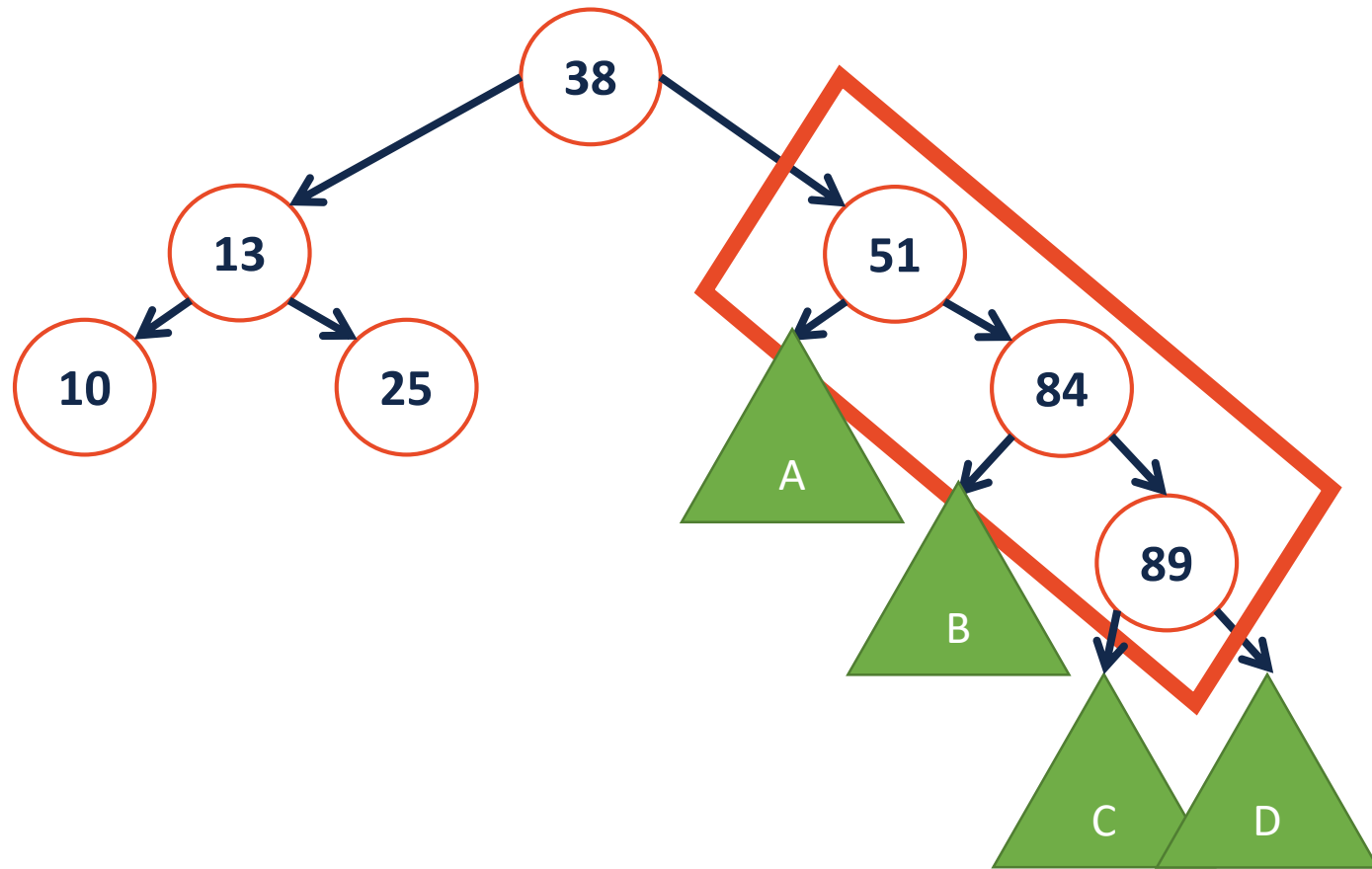
We will perform a rotation that maintains two properties:

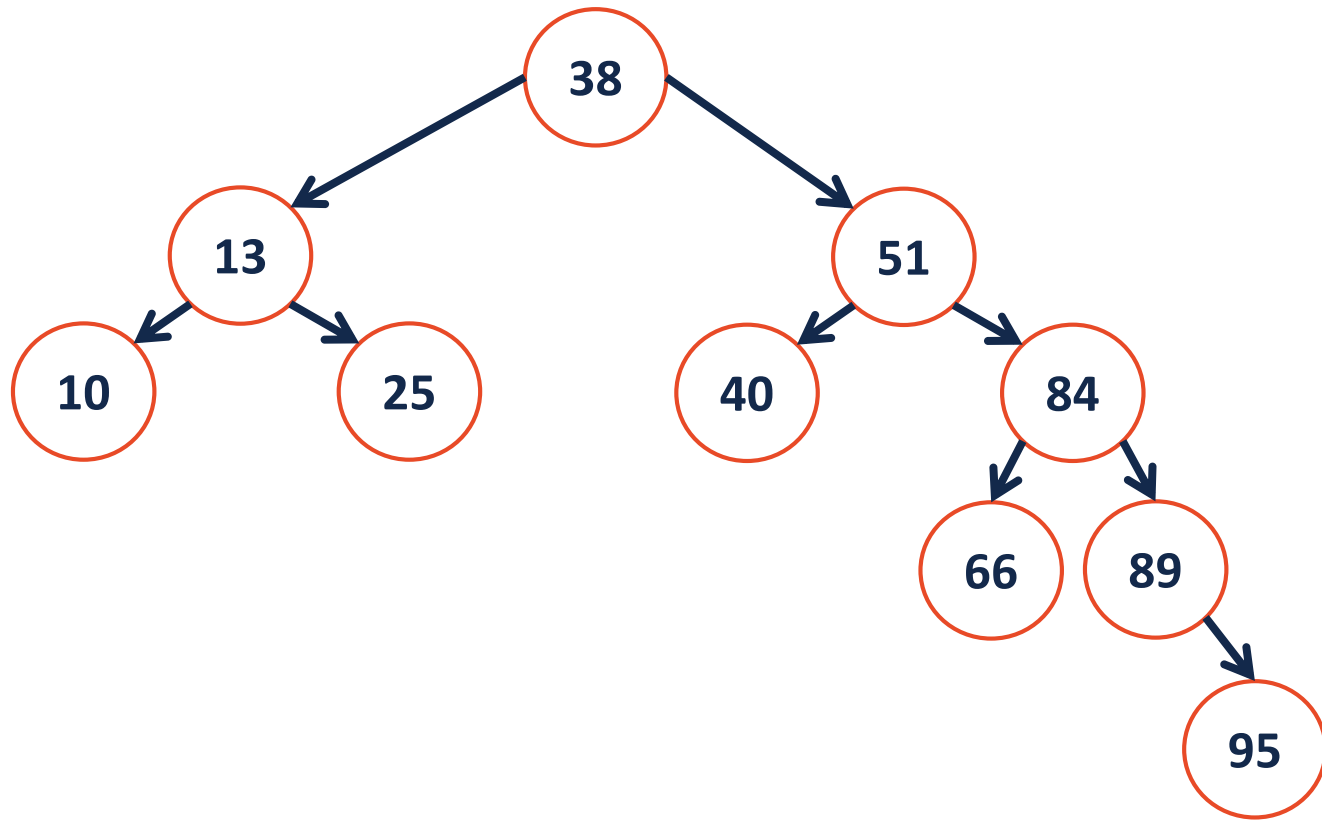
- 1.

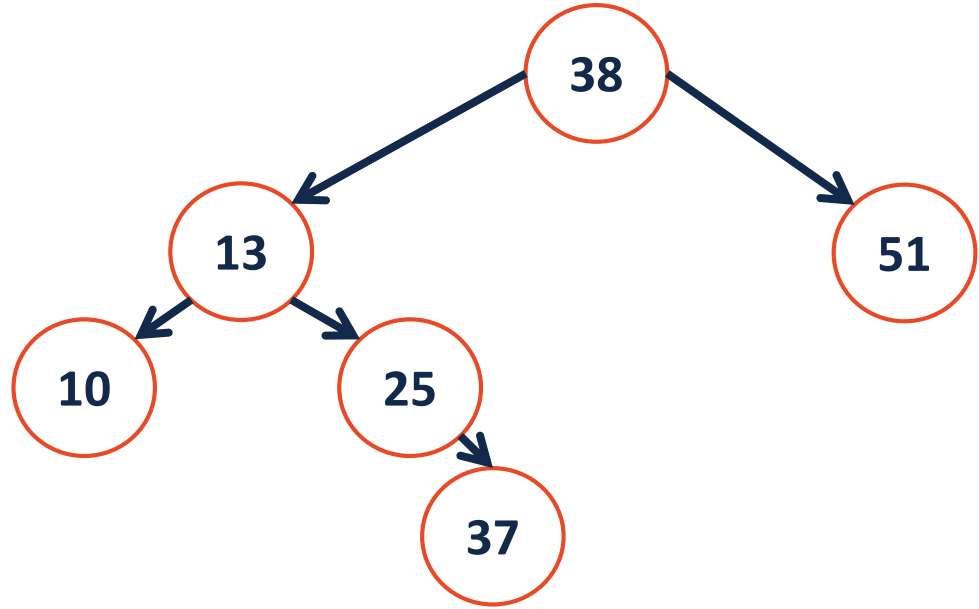
- 2.

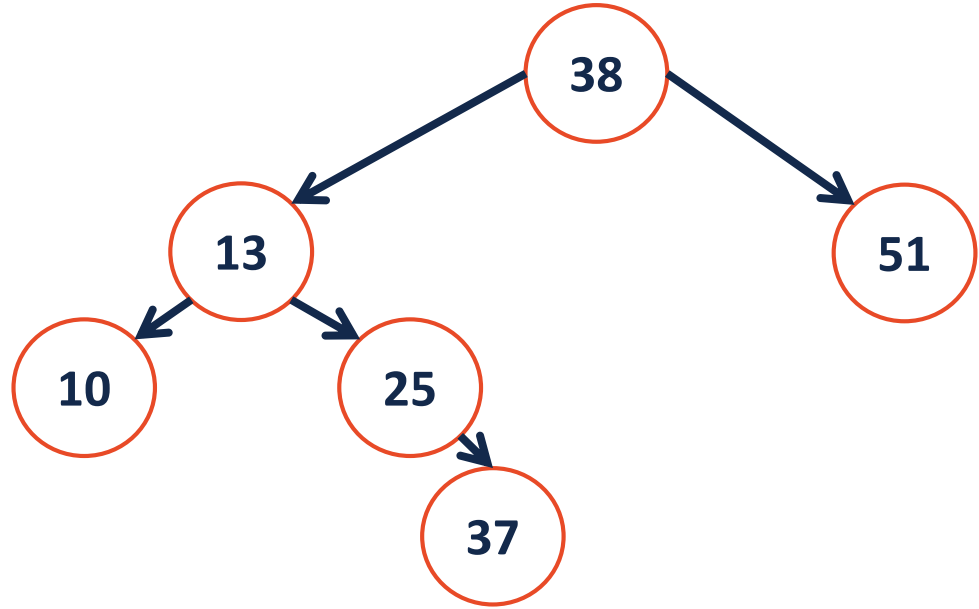












BST Rotation Summary

- Four kinds of rotations (L, R, LR, RL)
- All rotations are local (subtrees are not impacted)
- All rotations are constant time: $O(1)$
- BST property maintained

GOAL:

We call these trees:

AVL Trees

Three issues for consideration:

- Rotations
- Maintaining Height
- Detecting Imbalance