

Data Structures

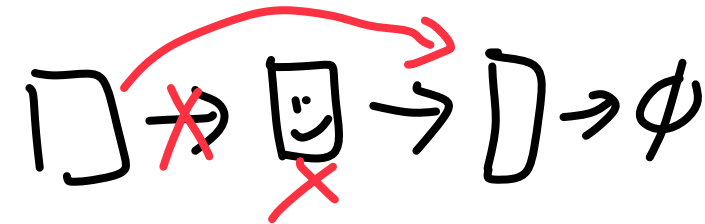
Linked Lists & (maybe) Array Lists

CS 225

Brad Solomon

September 2, 2026

remove(" ")



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Info Nights

Monday, August 24th 6 PM | CIF Room 4025

Monday, August 31st 7 PM | Wohlers Room 141

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Case Training + Meet & Greet

Wednesday, September 2nd, 6 PM | CIF Room 4025

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Women in Consulting Night

Friday, September 4th 5 PM | Wymer 1010

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Application Deadlines

Cycle 1 - Friday, August 28th @ 11:59 PM

Cycle 2 - Friday, September 4th @ 11:59 PM



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Learning Objectives

Review the importance of index in a linked list

Finish implementing the List ADT (as a linked list)

Discuss data variables for implementing array lists

Explore the List ADT (as an array list) ↪ Time permitting

List ADT

A list is an **ordered** collection of items

Items can be either **heterogeneous** or **homogenous**

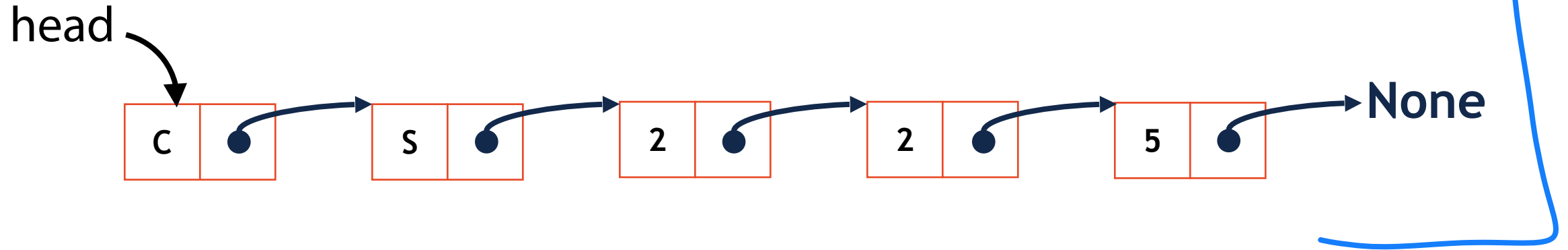
The list can be of a **fixed size** or is **resizable**

A minimal set of operations (that can be used to create all others):

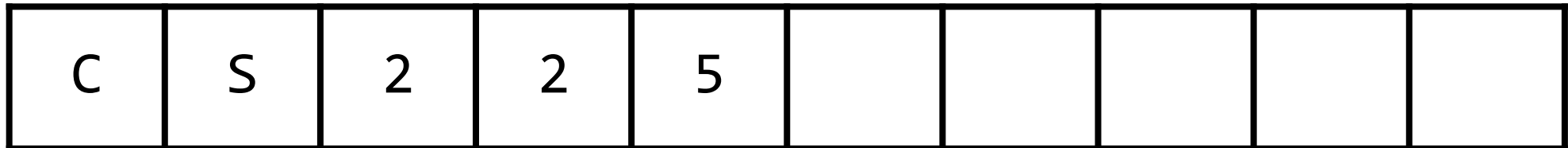
1. Insert
2. Delete
3. isEmpty
4. getData
5. Create an empty list

List Implementations

1. Linked List



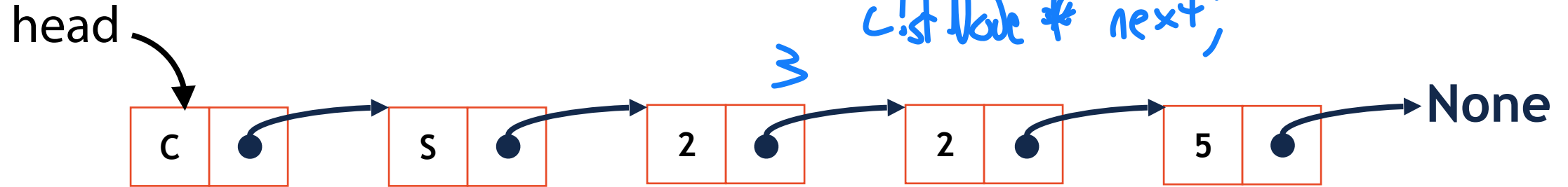
2. Array List



Where we left off...

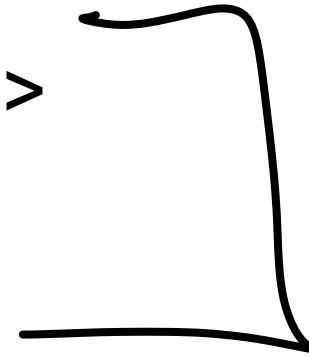
List Node {
↳ + data

List Node * next;



1. Singly linked list only accesses forward —>

↳ B/c we only have next



2. To insert in arbitrary position we need to access what value?

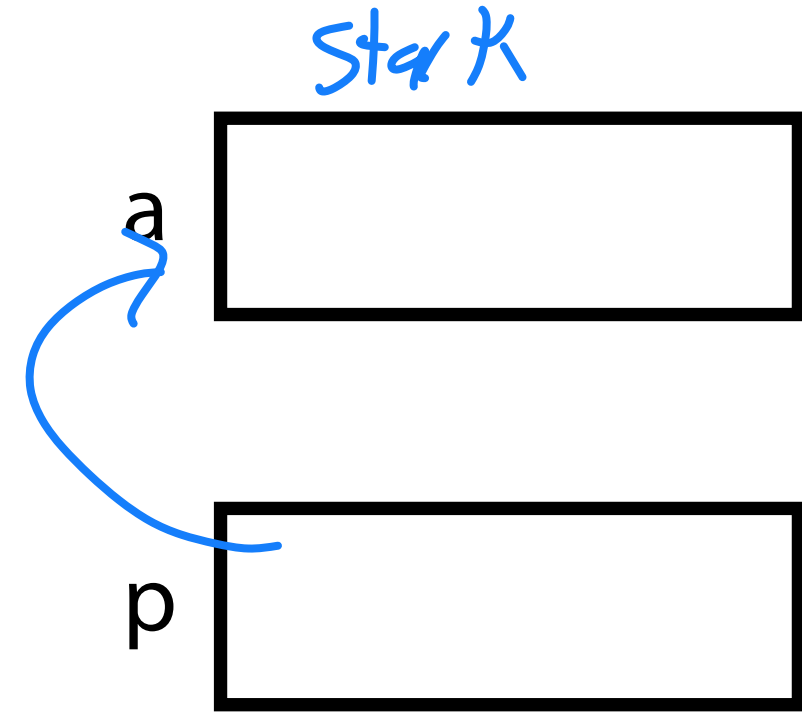
↳ prev → next is the reference (to a pointer)
that we modify

A review on memory management

A pointer stores a memory address

```
int a = 3;
```

```
int *p = &a;
```



A review on memory management

A reference assigns a new name to a variable

```
int a = 3;
```

$y = a$



```
void blackBox(int & y) {  
    y = 4;  
}
```

y inside this scope

```
blackBox(a);
```

a (local stack)

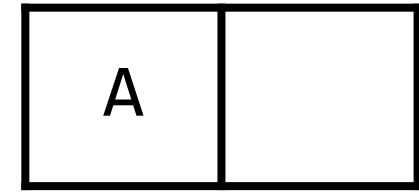


A review on memory management

Now let's think in terms of linked lists...

$\uparrow$
`ListNode* a = new ListNode(A);` $\uparrow$

$y = a$



$\uparrow$
`void blackBox(ListNode* &y) {`
 $\uparrow$
 Start pointer
 $\underline{y} = \text{new ListNode(B);}$
 $\uparrow$
 = 0x4
}

`blackBox(a->next);`

ref to

$\nwarrow$
 $\uparrow$
ListNode*

$\Leftrightarrow$ (*a).next

$a = 0x1$

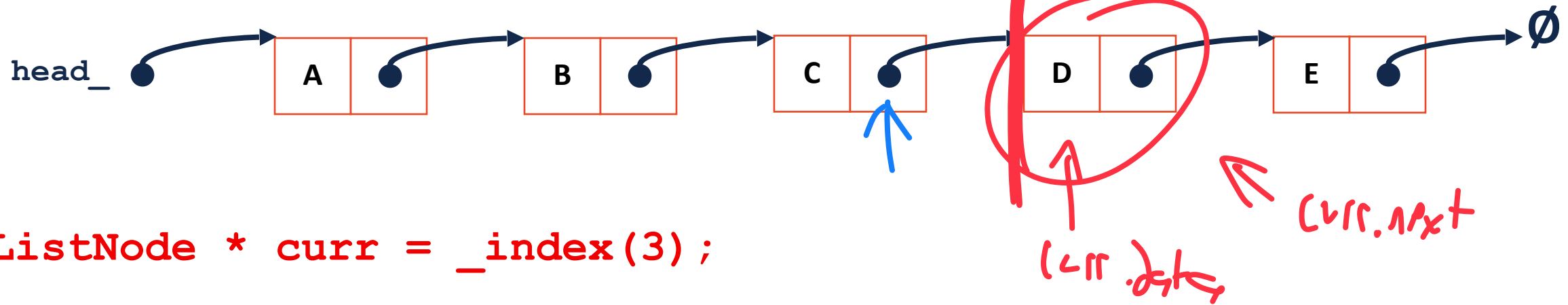
y is a

heap { ListNode }
0x4

```
1 // Iterative Solution:
2 template <typename T>
3 typename List<T>::ListNode *& List<T>::_index(unsigned index) {
4     if (index == 0) { return head; }
5     else {
6         ListNode *curr = head;
7         for (unsigned i = 0; i < index - 1; i++) {
8             curr = curr->next;
9         }
10        return curr->next;
11    }
12 }
```



Comparing pointer to reference-to-pointer



```
ListNode * curr = _index(3);
```

We can access **curr->data** and **curr->next** but not **previous.next**

```
ListNode *& curr = _index(3);
```

We can access **curr.data**, **curr.next** and...

curr == previous.next

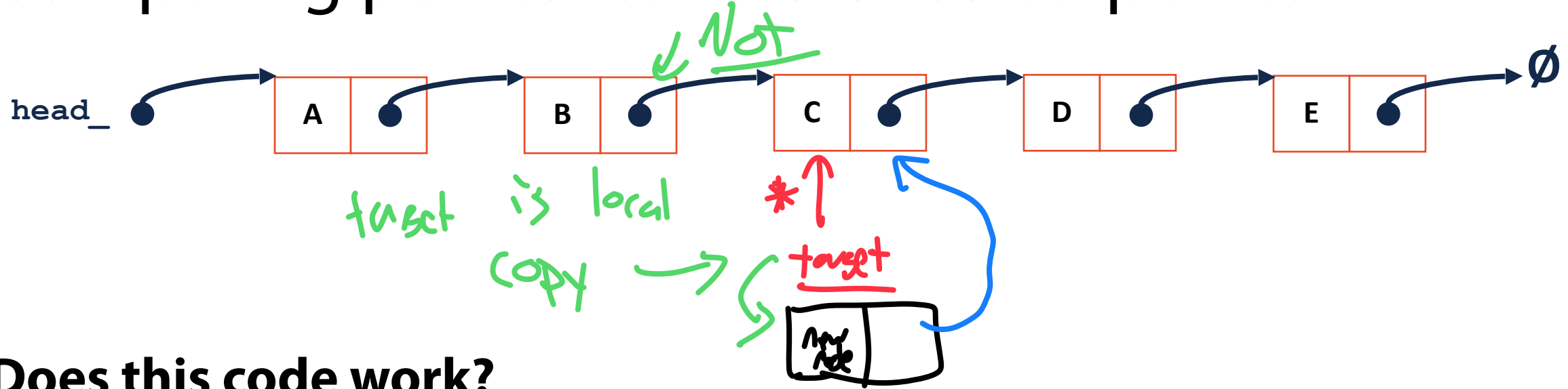
ref

(can modify
prev → next)



Included is the Bonus Video version of the next few slides

Comparing pointer to reference-to-pointer



Does this code work?

```
void insertAtNode(ListNode* target, int value) {
```

```
    1) ListNode* newNode = new ListNode(value);
```

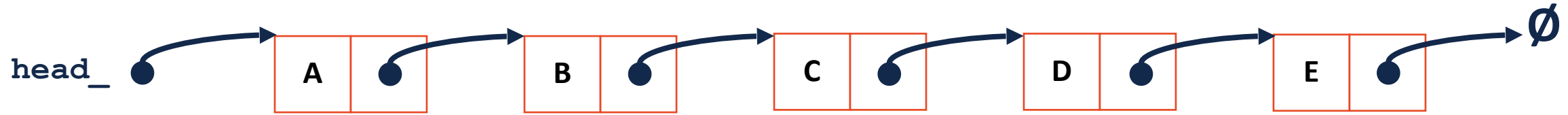
```
    2) newNode->next = target;
```

```
    3) target = newNode;
```



Join Code: 225

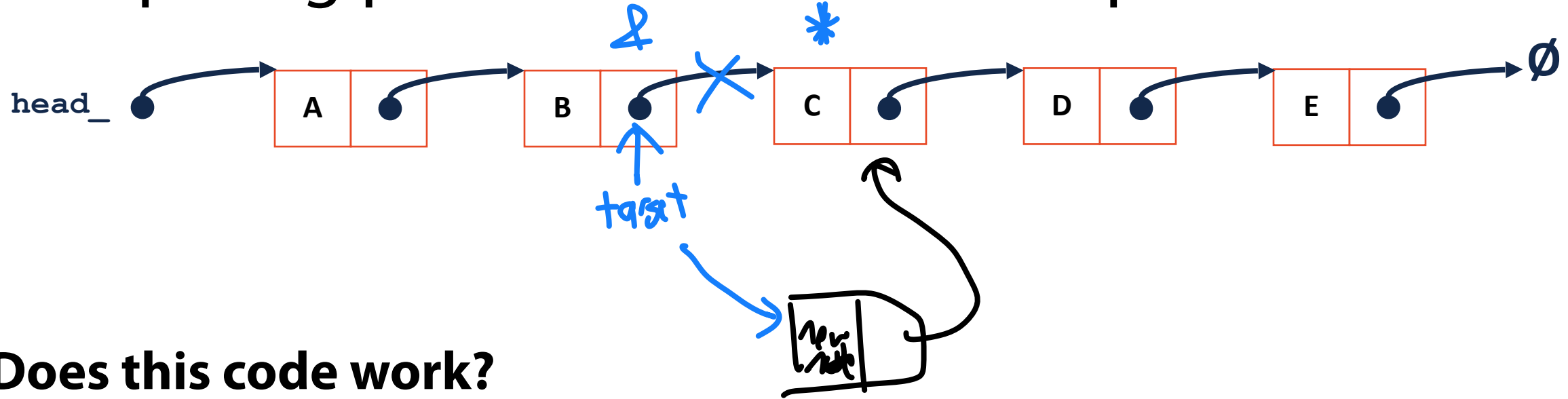
Comparing pointer to reference-to-pointer



This does not work! The pointer is a local stack object!

```
void insertAtNode(ListNode* target, int value) {  
    ListNode* newNode = new ListNode(value);  
    newNode->next = target;  
    target = newNode; // Only updates local copy!  
}
```

Comparing pointer to reference-to-pointer



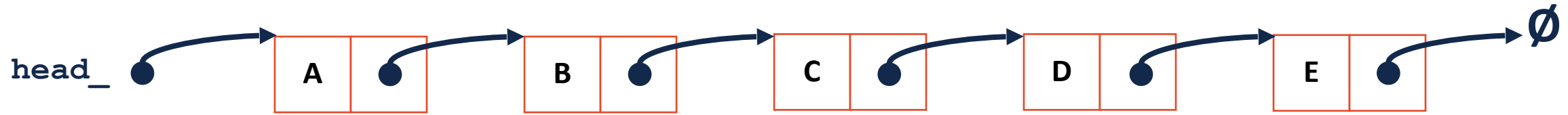
Does this code work?

```
void insertAtNode(ListNode*& target, int value) {  
    ListNode* newNode = new ListNode(value);  
    newNode->next = target;  
    target = newNode;  
}
```



Join Code: 225

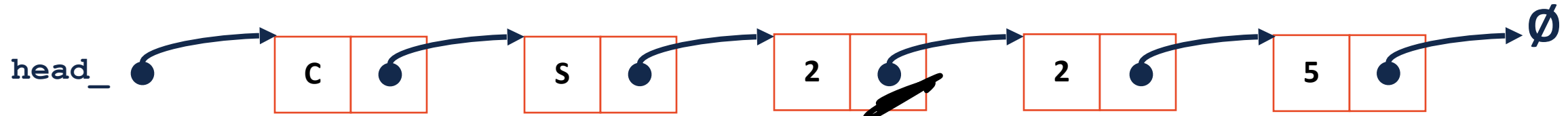
Comparing pointer to reference-to-pointer



Yes — because the reference is to a specific memory allocation

```
void insertAtNode(ListNode*& target, int value) {  
    ListNode* newNode = new ListNode(value);  
    newNode->next = target;  
    target = newNode;  
}
```

Linked List: insert(data, index)



1) Get reference to previous node's next

```
ListNode *& curr = _index(index);
```

2) Create new ListNode

```
ListNode * tmp = new ListNode(data);
```

3) Update new ListNode's next

```
tmp->next = curr;
```

4) Modify the previous node to point to new ListNode

```
curr = tmp;
```

Lets compare...

List.hpp



```
1
2 template <typename T>
3 void List<T>::insertAtFront(const T& t)
4 {
5     ListNode *tmp = new ListNode(t);
6
7     tmp->next = head_;
8
9     head_ = tmp;
10 }
11
12
13
14
15
16
17
18
19
20
21
22
```

all
O(1)
ops

```
1
2 template <typename T>
3 void List<T>::insert(const T & data,
4 unsigned index) {
5
6
7
8     ListNode *& curr = _index(index);
9
10
11
12     ListNode * tmp = new ListNode(data);
13
14
15
16     tmp->next = curr;
17
18
19
20     curr = tmp;
21 }
22
```

finding point,
is slow

Modifying
at location
in LL is
fast

What is the Big O of insert (given list of size n)?

List.hpp

15% $O(\log n)$

85% $O(n)$

$D \rightarrow D \rightarrow \emptyset$
↑
Last item

→
"work"

1 billion - 1 "work"

$D \rightarrow D \rightarrow \dots \rightarrow D \rightarrow \emptyset$
↑
1 billion
↑
Last item

```
1
2 template <typename T>
3 void List<T>::insert(const T & data,
4 unsigned index) {
5
6
7
8     ListNode *& curr = _index(index);
9     ↳ ???  $O(n)$ 
10
11     ListNode * tmp = new ListNode(data);
12     ↳  $O(1)$ 
13
14     tmp->next = curr;
15
16     ↳  $O(1)$ 
17
18     curr = tmp;
19     ↳  $O(1)$ 
20 }
21
22
```



Join Code: 225

List Random Access []

Given a list L, what operations can we do on L []?

↳ Get Data()

$x = L[i];$

↳ Set Data()

$L[i] = x;$

} Only type
T &

What return type should this function have?

$L[x]$ is type List Node *

$L(x) \rightarrow \text{data}$

List Random Access []

What return type should this function have?



Join Code: 225

[template <class T>]

(A) T &

36%

(B) ListNode

8%

(C) ListNode *

13%

(D) ListNode *&

40%

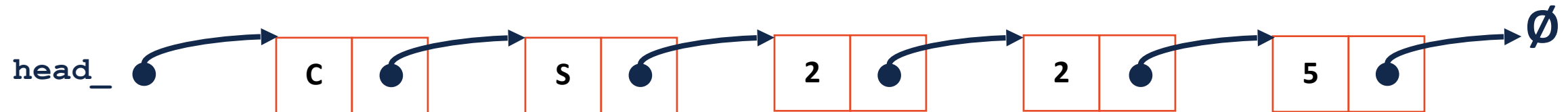
Not the expected interface

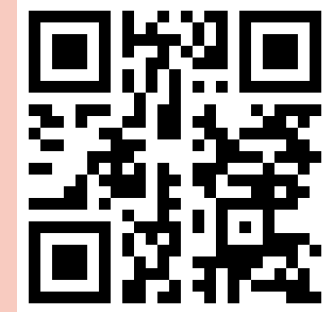
This could work

```
48 template <typename T>
49 T & List<T>::operator[] (unsigned index) {
50
51
52
53
54
55
56
57
58 }
```

List Node * & temp = _index (index);

return temp->data;





Join Code: 225

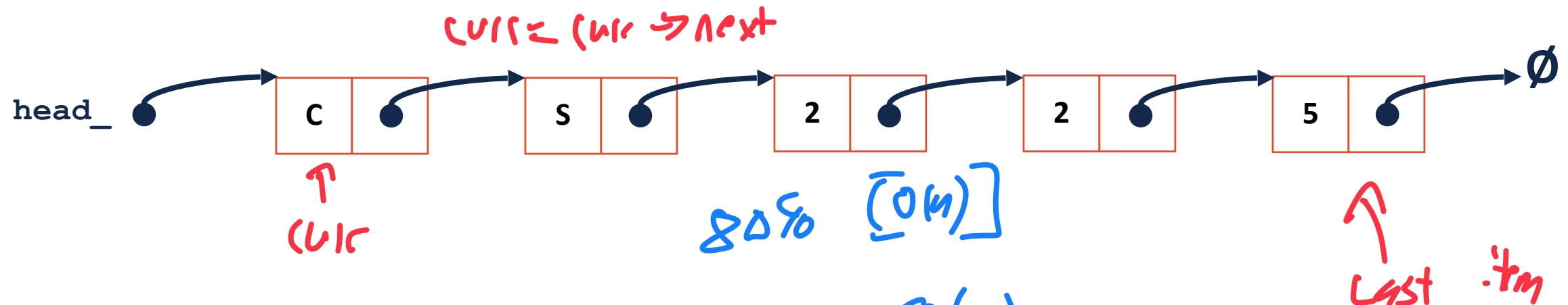
```

48 template <typename T>
49 T & List<T>::operator[](unsigned index) {
50
51
52 ListNode *&new_node = _index(index);
53
54
55 return new_node->data;
56
57
58 }

```

$\uparrow O(n)$

$\uparrow O(1)$



What is the Big O of random access?

$O(n)$

Linked List: remove(<parameters>)

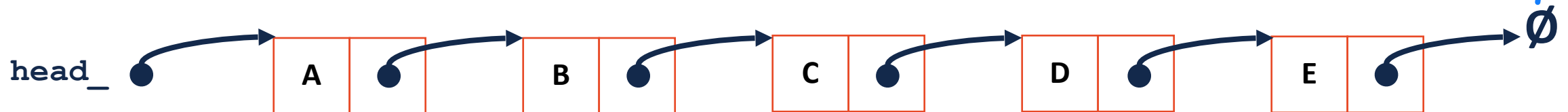
What input parameters make sense for remove?

remove (unsigned index)

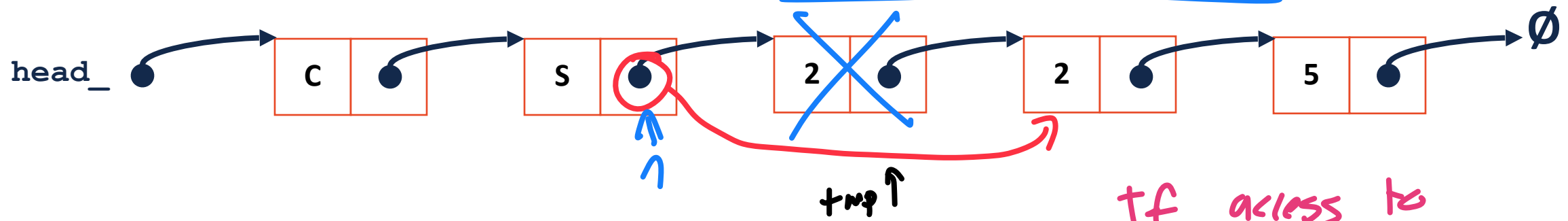
remove (T & value)

*remove (ListNode *& my N)*

*remove (ListNode *)
can work but
will be slower
& more complex*



Linked List: remove(ListNode *& n)^(target)



$O(1)$

ListNode * tmp = n;

$n = n \rightarrow \text{next};$

delete tmp;

If access to specific mem address, linked list remove is fast!

remove(ListNode *& n)^(target)

1) Loop through list until curr->next == n

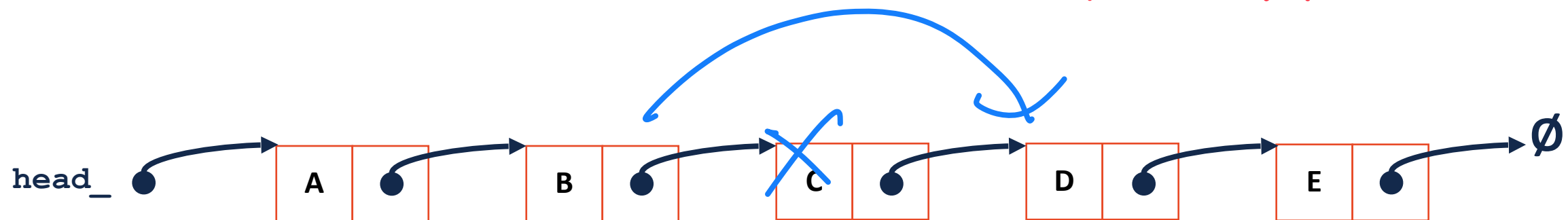
$O(n)$



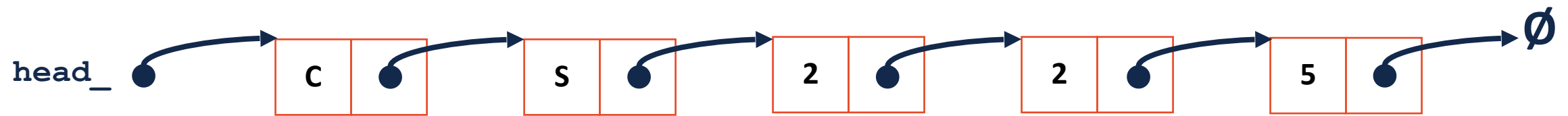
```
103 template <typename T>
104 T List<T>::remove(ListNode *& node) {
105
106     ListNode * temp = node;
107     node = node->next;
108     T data = temp->data;
109     delete temp;
110     return data;
111 }
112
```

local copy goes out of scope

If I want to return T I either return
by value or I add it to heap is another
poor choice



Linked List: remove(T & data)

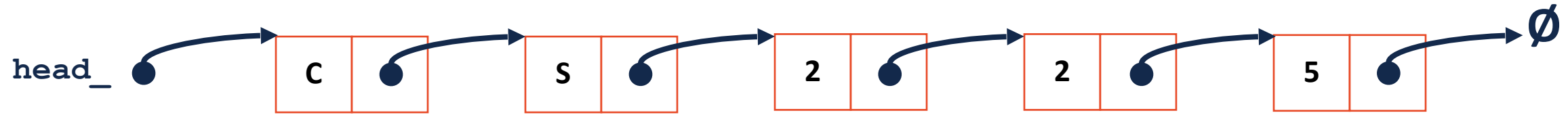


↑
curr

Stop when $curr \rightarrow data == T$

or ...
when $curr \rightarrow next == nullptr$

Linked List: remove



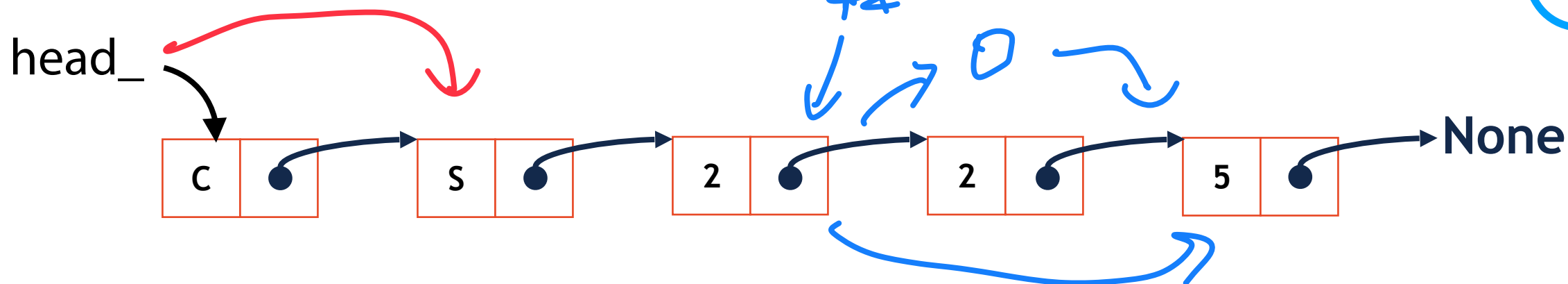
Running time for **remove(ListNode *&)**

↳ $O(1)$

Running time for **remove(T & data)**

↳ $O(n)$

Linked List Runtimes



	<u>@Front</u>	<u>@RefPointer</u>	@Index
Insert	$O(1)$	$O(1)$	$O(n)$
Delete	$O(1)$	$O(1)$	$O(n)$

Thinking critically about linked lists...



What is the runtime to filter a list of all odd valued items?

(A) $O(1)$

(B) $O(\log n)$

(C) $O(n)$

(D) $O(n^2)$

Thinking critically about linked lists...

An $O(n)$ runtime seems bad (and is) for finding a single item.

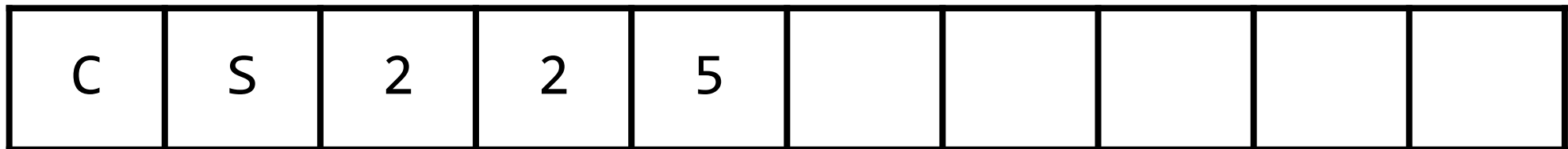
When might you want to use a linked list?

List Implementations

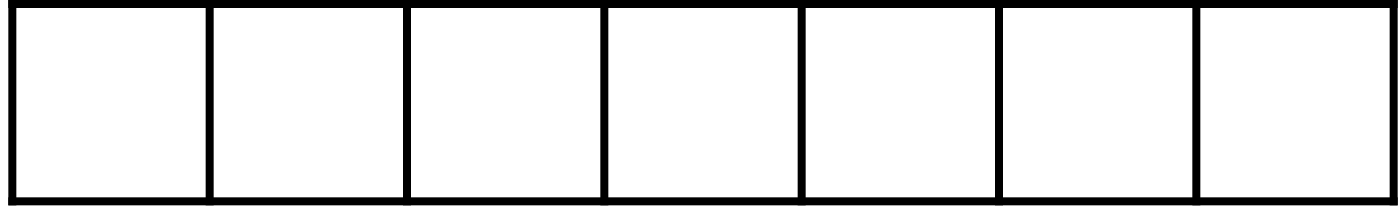
1. Linked List



2. Array List



Array List



An array is allocated as continuous memory.

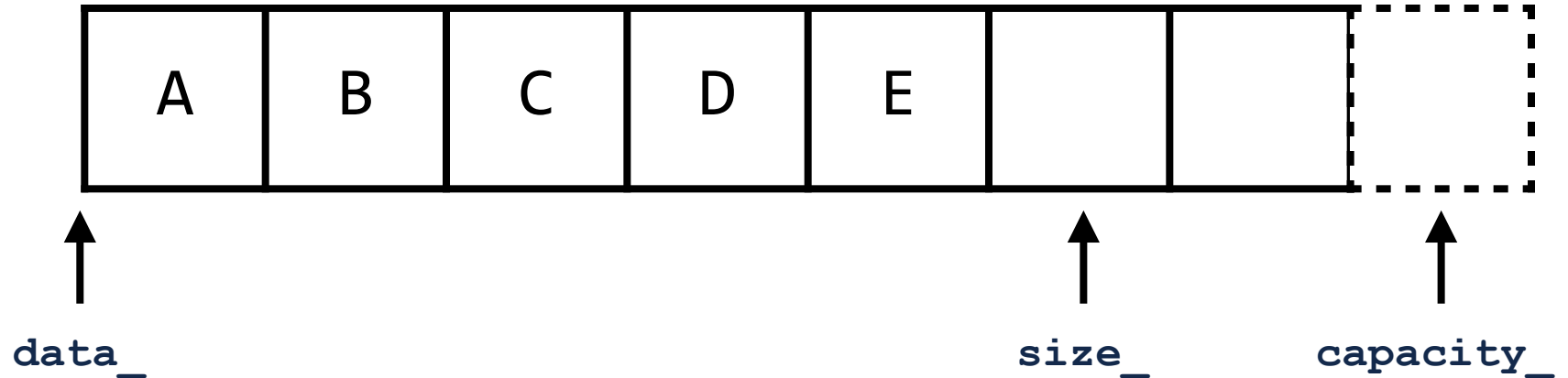
Three values are necessary for efficient array usage:

1)

2)

3)

Array List

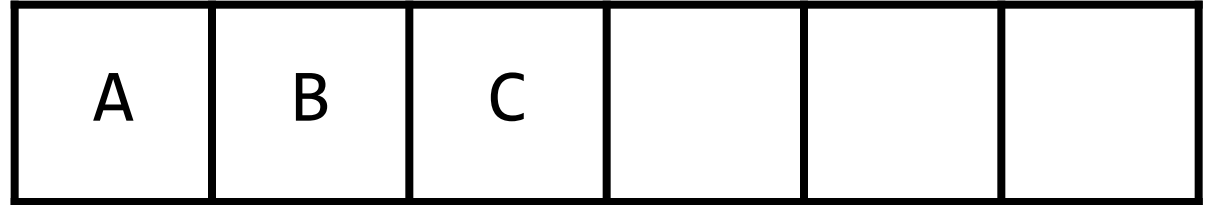


In C++, vector is implemented as:

- 1) **Data:** Stored as a pointer to array start
- 2) **Size:** Stored as a pointer to the next available space
- 3) **Capacity:** Stored as a pointer past the end of the array

List.h

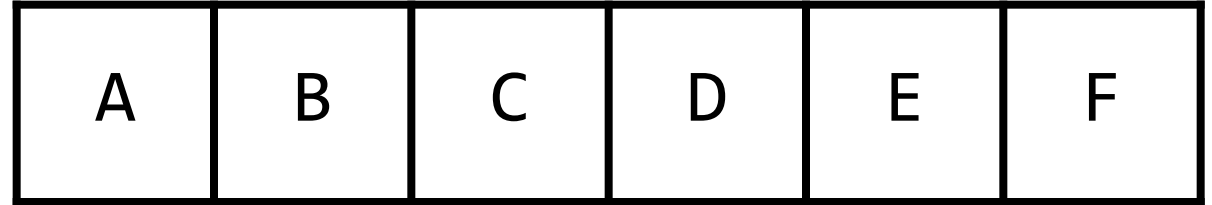
```
1  #pragma once
2
3  template <typename T>
4  class List {
5  public:
6      /* --- */
7  ...
8  private:
9      T *data_;
10
11     T *size_;
12
13     T *capacity_;
14
15     ...
16     /* --- */
17 };
```



If I want to know the number of items in the array:

List.h

```
1  #pragma once
2
3  template <typename T>
4  class List {
5  public:
6      /* --- */
7  ...
8  private:
9      T *data_;
10
11     T *size_;
12
13     T *capacity_;
14
15     ...
16     /* --- */
17 };
```



How do I know if I'm at capacity?

Array List: []

c	s	2	2	5					
---	---	---	---	---	--	--	--	--	--

Array List: insertFront(data)

c	s	2	2	5					
---	---	---	---	---	--	--	--	--	--

Array List: insertBack(data)

c	s	2	2	5					
---	---	---	---	---	--	--	--	--	--

Array List: insert(data, index)



C	S	2	2	5					
---	---	---	---	---	--	--	--	--	--

Array List: addspace(data)

N	O	S	P	A	C	E
---	---	---	---	---	---	---