

Data Structures

Queues, Iterators, and maybe Trees?

CS 225

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Exam 1 (9/17 — 9/19)

Autograded MC and one coding question

Manually graded short answer prompt

Practice exam is out on PL now

Topics covered can be found on website

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<https://courses.engr.illinois.edu/cs225/fa2025/exams/>

Learning Objectives



Queue!!

Discuss the importance of iterators



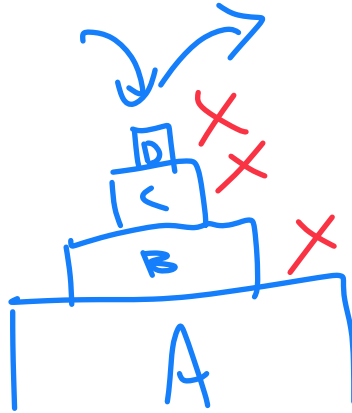
Review trees and binary trees



Discuss the tree ADT

Stack ADT

- [Order]: LIFO



- [Implementation]: Array (such as `std::vector`)

- [Runtime]: $O(1)$ Push and Pop (No random access)

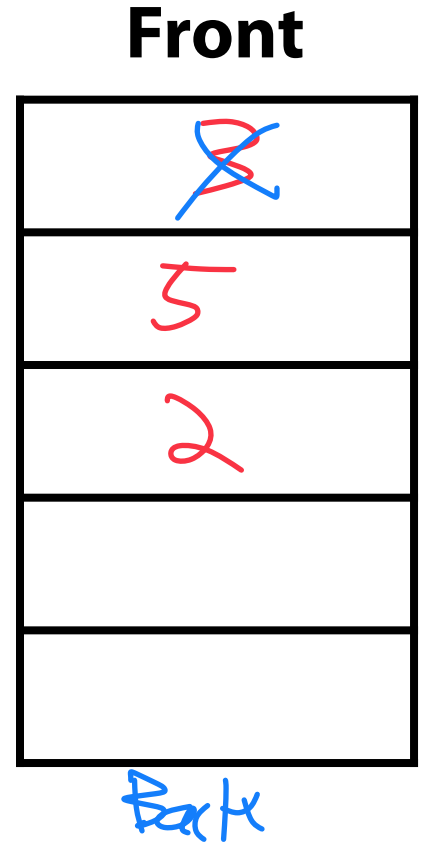
Queue Data Structure

A **queue** stores an ordered collection of objects (like a list)

However you can only do two* operations:

Enqueue: Put an item at the back of the queue

Dequeue: Remove and return the front item of the queue



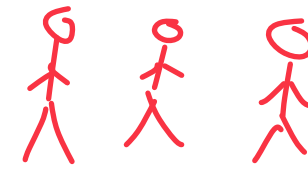
Front & back

↓ both 0

back
↓ index 1

enqueue(3) ; enqueue(5) ; dequeue() ; enqueue(2)

Queue Data Structure

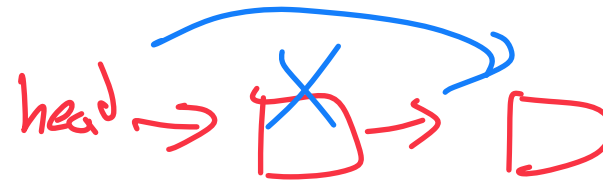


The queue is a **first in — first out** data structure (FIFO)



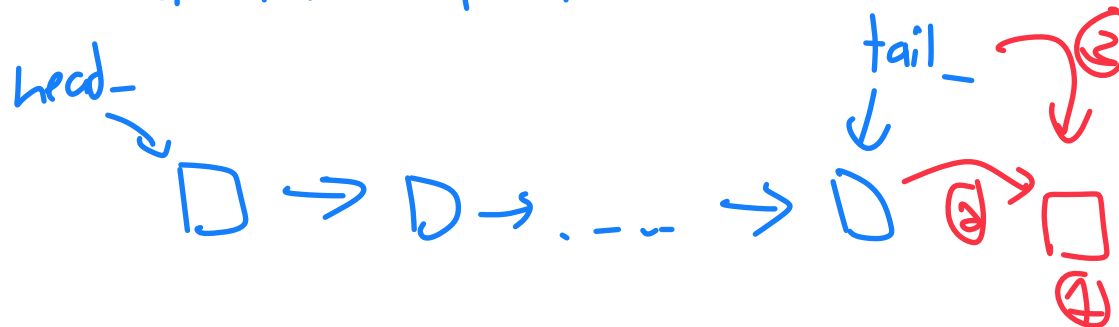
What data structure excels at removing from the front?

Linked List



Can we make that same data structure good at inserting at the end?

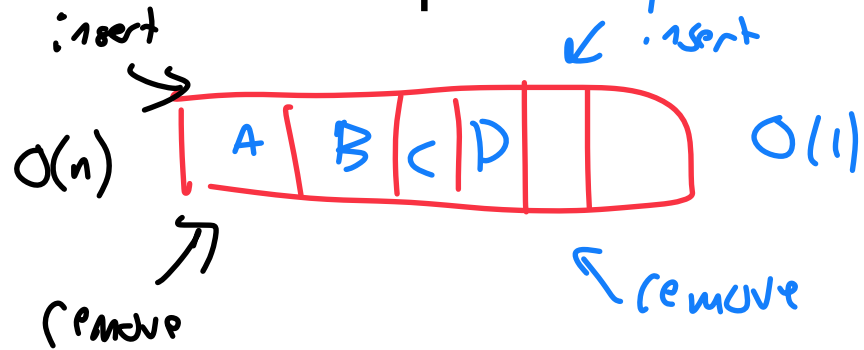
↳ Add a tail pointer



Queue Data Structure

an array!

The C++ implementation of a queue is also a vector or deque — why?



Two reasons

1) Engineering! $\leftarrow$ CS 225 will ignore this!

2) We can make theory better!

Engineering vs Theory Efficiency

	Time x1 billion	Like
L1 cache reference	0.5 seconds	Heartbeat 💖
Branch mispredict	5 seconds	Yawn 🥱
L2 cache reference	7 seconds	Long yawn 🥱 🥱 🥱
Mutex lock/unlock	25 seconds	Make coffee ☕
Main memory reference	100 seconds	Brush teeth
Compress 1K bytes	50 minutes	TV show 📺
Send 2K bytes over 1 Gbps network	5.5 hours	(Brief) Night's sleep 🛌
SSD random read	1.7 days	Weekend
Read 1 MB sequentially from memory	2.9 days	Long weekend
Read 1 MB sequentially from SSD	11.6 days	2 weeks for delivery 📦
Disk seek	16.5 weeks	Semester
Read 1 MB sequentially from disk	7.8 months	Human gestation 🐣
Above two together	1 year	🌍 ☀️
Send packet CA->Netherlands->CA	4.8 years	Ph.D. 🎓

(Care of <https://gist.github.com/hellerbarde/2843375>)

Engineering vs Theory Efficiency

	Time x1 billion	Like
L1 cache reference <i>↳ Live active memory</i>	0.5 seconds	Heartbeat 💓
Main memory reference <i>↳ RAM</i>	100 seconds	Brush teeth
SSD random read	1.7 days	Weekend
Disk seek	16.5 weeks	Semester
Send packet CA->Netherlands->CA	4.8 years	Ph.D. 🎓

Smallest

Largest

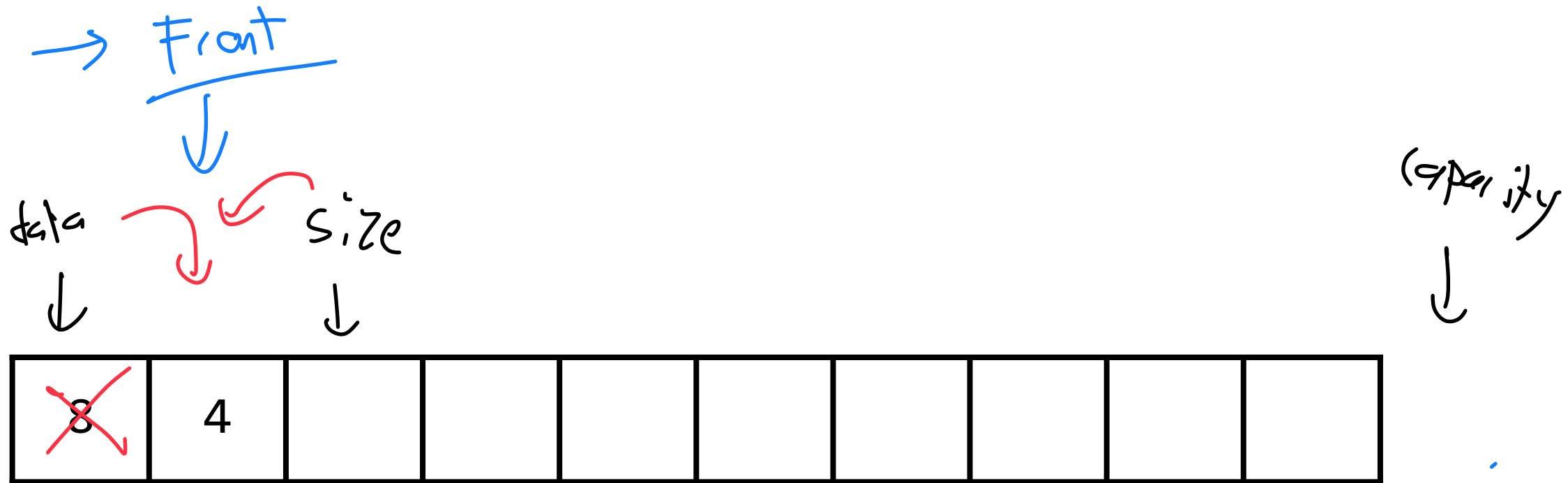
(Care of <https://gist.github.com/hellerbarde/2843375>)

Queue Data Structure

```
q.enqueue(8);  
q.enqueue(4);  
q.dequeue();
```

What do we need to track to maintain a queue with an array list?

Goal: Remove 8 in $O(1)$ time

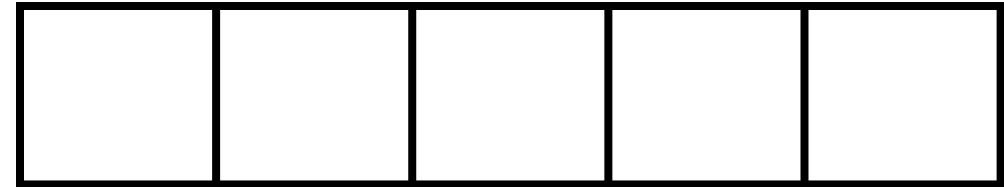


Queue Data Structure

Unlike the array list, it is easier to implement a Queue using unsigned ints

Queue.h

```
1 #pragma once
2
3 template <typename T>
4 class Queue {
5     public:
6         void enqueue(T e);
7         T dequeue();
8         bool isEmpty();
9
10    private:
11        T *data_;
12        unsigned size_;
13        unsigned capacity_;
14        unsigned front_;
15 };
```



↖ New entry "front"

(Circular) Queue Data Structure



Queue.h

```
1 #pragma once
2
3 template <typename T>
4 class Queue {
5     public:
6         void enqueue(T e);
7         T dequeue();
8         bool isEmpty();
9
10    private:
11        T *data_;
12        unsigned capacity_;
13        unsigned size_;
14        unsigned front_;
15 };
```

data
↓

↓ index of "start"

Front



Size

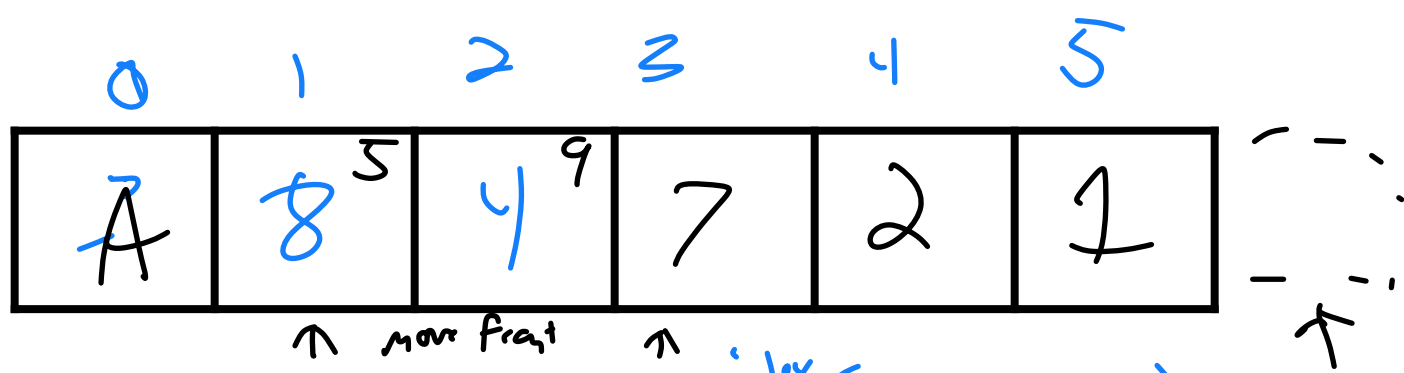
↪ # of items in array

total #
of spaces

Front



Size



Enqueue(D): Add D to ^{index} (front + size)
 size ++;

Dequeue(): Remove & return front
 size --;
 front ++;

Size: ~~0~~ ~~1~~ ~~2~~ ~~4~~ 3

Front: ~~0~~ 1

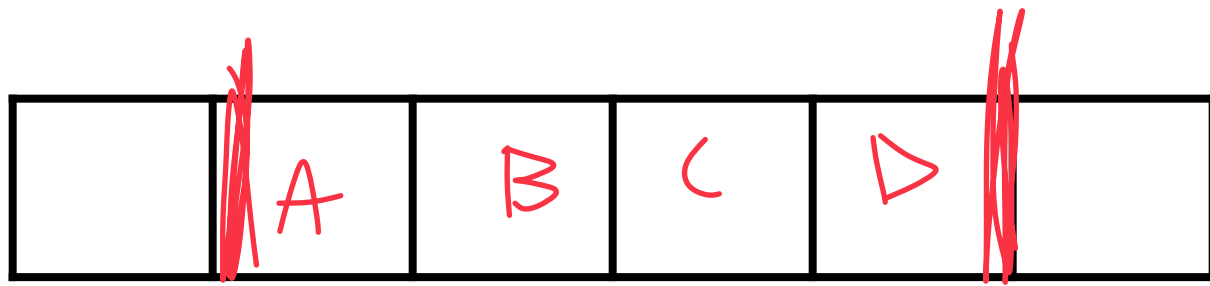
```

Queue<int> q;
q.enqueue(3); 1
q.enqueue(8); 2
q.enqueue(4); 3
0 → 1 q.dequeue(); 2
q.enqueue(7); 3
1 → 2 q.dequeue(); 2
2 → 3 q.dequeue(); 1
q.enqueue(2); 2
q.enqueue(1); 3
3 + 3 = 6 → q.enqueue(4); 4
q.enqueue(5); 5
q.dequeue(); 4
q.enqueue(9); 5

```

3 + 3 = 6
 ↓
 Insert @ 0

Capacity: 6



Back is
size + front

Enqueue(D): Insert @ $(\text{size} + \text{front}) \% \text{capacity}$
size++ until size == capacity

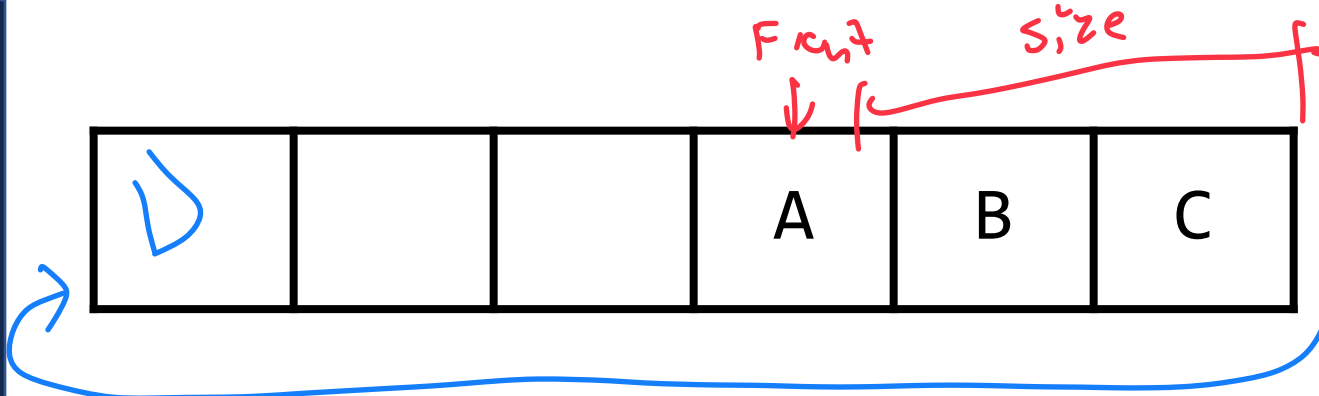
Dequeue(): Remove @front
 $\text{front} = (\text{front} + 1) \% \text{capacity}$
size--

Size:

Front:

Capacity:

```
Queue<int> q;  
q.enqueue(3);  
q.enqueue(8);  
q.enqueue(4);  
q.dequeue();  
q.enqueue(7);  
q.dequeue();  
q.dequeue();  
q.enqueue(2);  
q.enqueue(1);  
q.enqueue(3);  
q.enqueue(5);  
q.dequeue();  
q.enqueue(9);
```



Enqueue(D): Add data to 'back' of queue

Insert D at index $(\text{size} + \text{front}) \% \text{capacity}$

size++ (as long as $\text{size} \neq \text{capacity}$)

Dequeue(): Remove data at index front

front = $(\text{front} + 1) \% \text{capacity}$

size-- (as long as $\text{size} \neq 0$)

Size: 3

Front: 3

Capacity: 6

```
Queue<int> q;
```

```
...
```

```
q.enqueue(D);
```

```
q.dequeue();
```

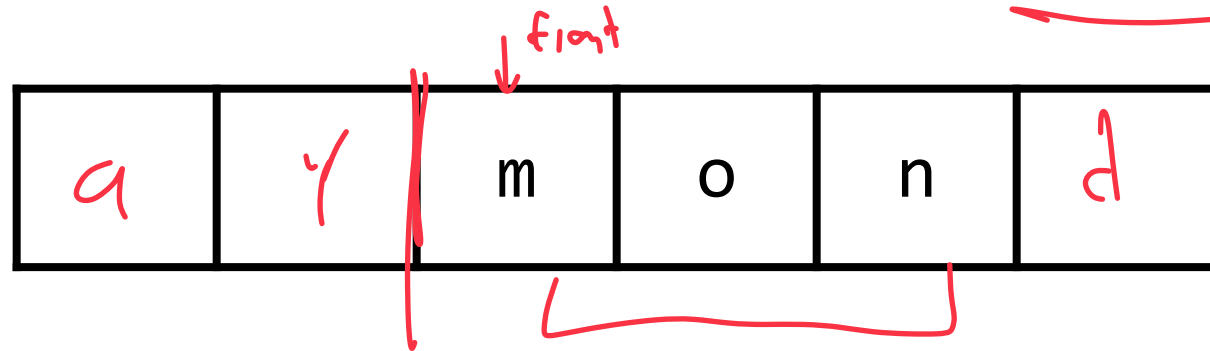
```
q.dequeue();
```

```
q.dequeue();
```

```
q.dequeue();
```

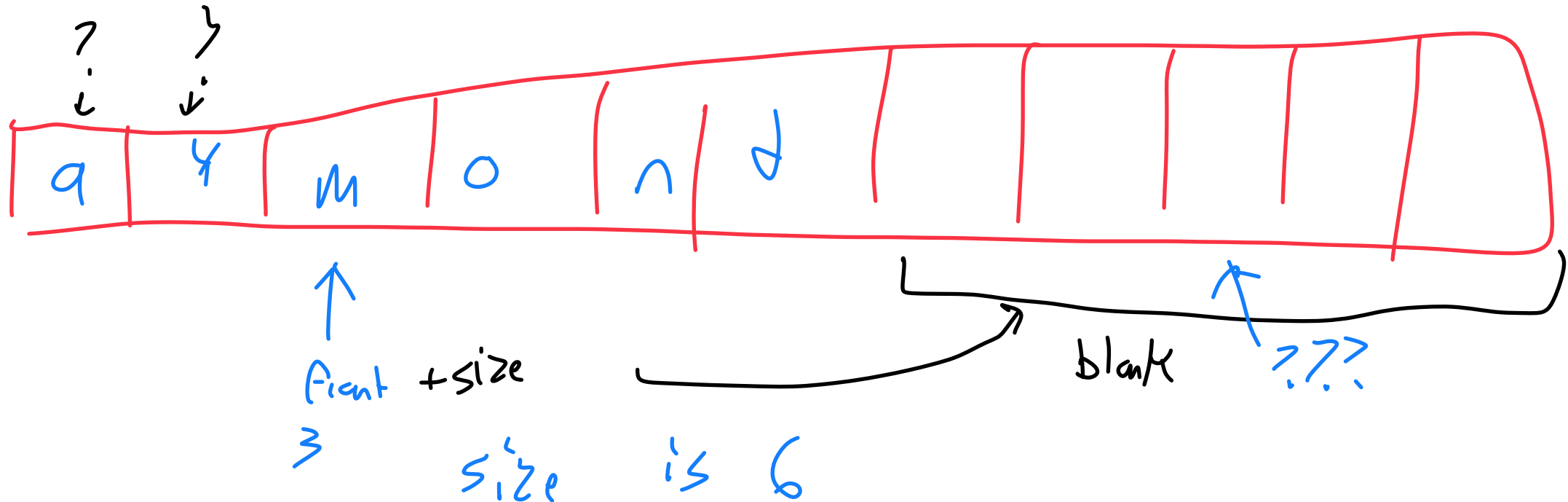
```
q.enqueue(E);
```

Queue Data Structure: Resizing



copy *

but not like this



```
Queue<char> q;  
...  
q.enqueue(d);  
q.enqueue(a);  
q.enqueue(y);  
q.enqueue(i);  
q.enqueue(s);
```

Queue Data Structure: Resizing

```
Queue<char> q;
```

```
...
```

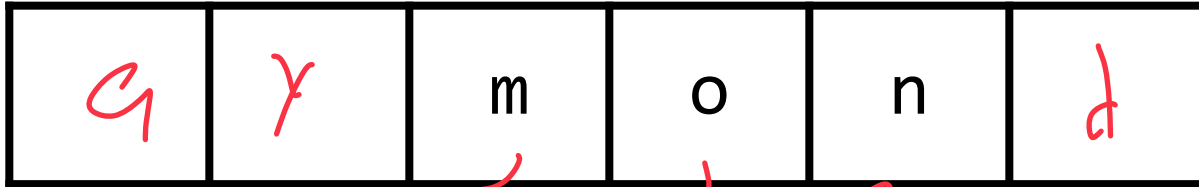
```
q.enqueue(d);
```

```
q.enqueue(a);
```

```
q.enqueue(y);
```

```
q.enqueue(i);
```

```
q.enqueue(s);
```



copy starting from front



front = 0

size = 6



6



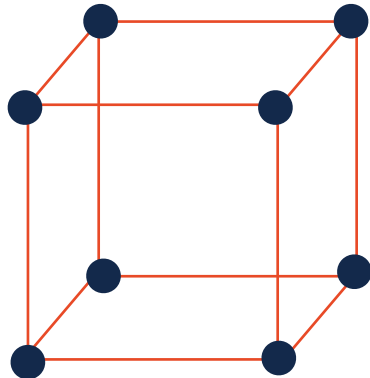
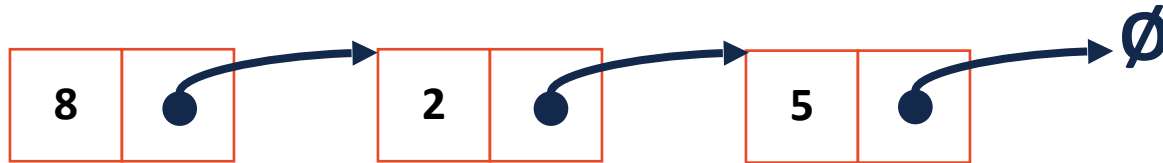
Queue ADT

- [Order]: First in first out
- [Implementation]: Trivially as LL
w/ circular queue as array
- [Runtime]: $O(1)$ * when array amortized $O(1)$

Iterators

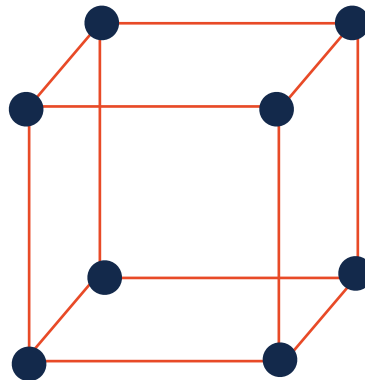
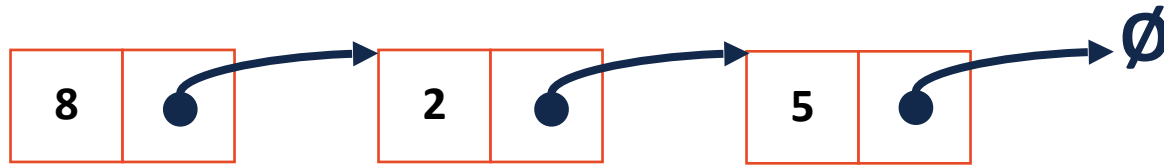
mp_lists!

We want to be able to loop through all elements for any underlying implementation in a systematic way



Iterators

We want to be able to loop through all elements for any underlying implementation in a systematic way

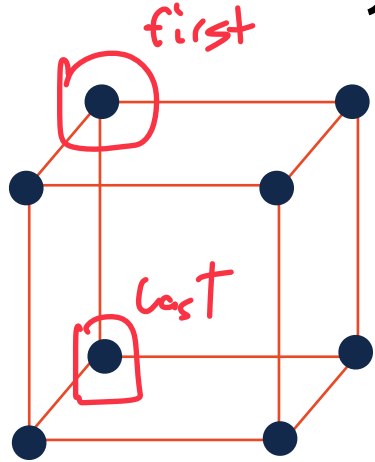


Cur. Location	Cur. Data	Next
<u>ListNode *</u> curr	<i>curr → data</i>	<i>curr → next</i>
unsigned index	<i>array[index]</i>	<i>index++</i>
Some form of (x, y, z)	<i>???</i> <i>...</i>	<i>???</i> <i>...</i>

Iterators

Cube defines its own Iterator

Iterators provide a way to access items in a container without exposing the underlying structure of the container



```
1 Cube::Iterator it = myCube.begin();  
2  
3 while (it != myCube.end()) {  
4     std::cout << *it << " ";  
5     it++;  
6 }  
7
```

increment
to get
next item

dereference
iterator

gives first item

gives last item

Iterators

For a class to implement an iterator, it needs two functions:

Iterator begin() $\leftarrow$ first item

Iterator end() $\leftarrow$ last item

Iterators

The actual iterator is defined as a class **inside** the outer class:

1. It must be of base class **std::iterator**

2. It must implement at least the following operations:

Iterator& operator ++() *← get next*

const T & operator *() *← dereference*

bool operator !=(const Iterator &) *← compare iterator objects*



Iterators

Here is a (truncated) example of an iterator:

```
1 template <class T>
2 class List {
3
4     class ListIterator : public
5     std::iterator<std::bidirectional_iterator_tag, T> {
6         public:
7             ListIterator& operator++();
8             ListIterator& operator--();
9             bool operator!=(const ListIterator& rhs);
10            const T& operator*();
11        };
12
13        ListIterator begin() const;
14
15        ListIterator end() const;
16    };
17
18
19
```

class inside class

get next

get prev

```
1 #include <list>
2 #include <string>
3 #include <iostream>
4
5 struct Animal {
6     std::string name, food;
7     bool big;
8     Animal(std::string name = "blob", std::string food = "you", bool big = true) :
9         name(name), food(food), big(big) { /* nothing */ }
10 };
11
12 int main() {
13     Animal g("giraffe", "leaves", true), p("penguin", "fish", false), b("bear");
14     std::vector<Animal> zoo;
15
16     zoo.push_back(g);
17     zoo.push_back(p);    // std::vector's insertAtEnd
18     zoo.push_back(b);
19
20     for ( std::vector<Animal>::iterator it = zoo.begin(); it != zoo.end(); ++it ) {
21         std::cout << (*it).name << " " << (*it).food << std::endl;
22     }
23
24     return 0;
25 }
```



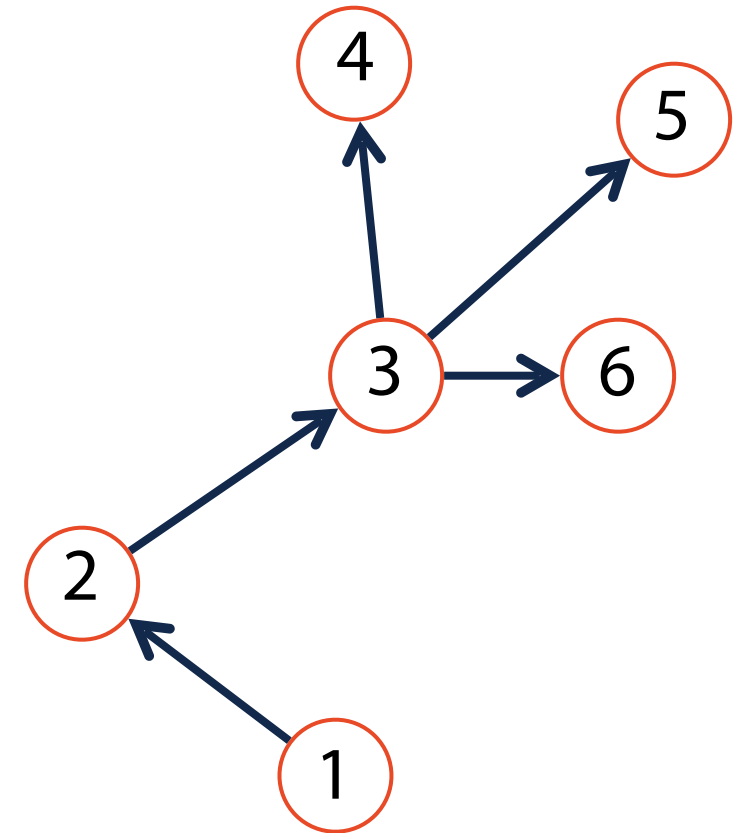
```
1
2 std::vector<Animal> zoo;
3
4
5 /* Full text snippet */
6
7 for ( std::vector<Animal>::iterator it = zoo.begin(); it != zoo.end(); ++it ) {
8     std::cout << (*it).name << " " << (*it).food << std::endl;
9 }
10
11
12 /* Auto Snippet */
13
14 for ( auto it = zoo.begin(); it != zoo.end(); ++it ) {
15     std::cout << (*it).name << " " << (*it).food << std::endl;
16 }
17
18 /* For Each Snippet */
19
20 for ( const Animal & animal : zoo ) {
21     std::cout << animal.name << " " << animal.food << std::endl;
22 }
23
24
25
```

Trees

A non-linear data structure defined recursively as a collection of nodes where each node contains a value and zero or more connected nodes.

[In CS 225] a tree is also:

- 1) Acyclic — No path from node to itself
- 2) Rooted — A specific node is labeled root

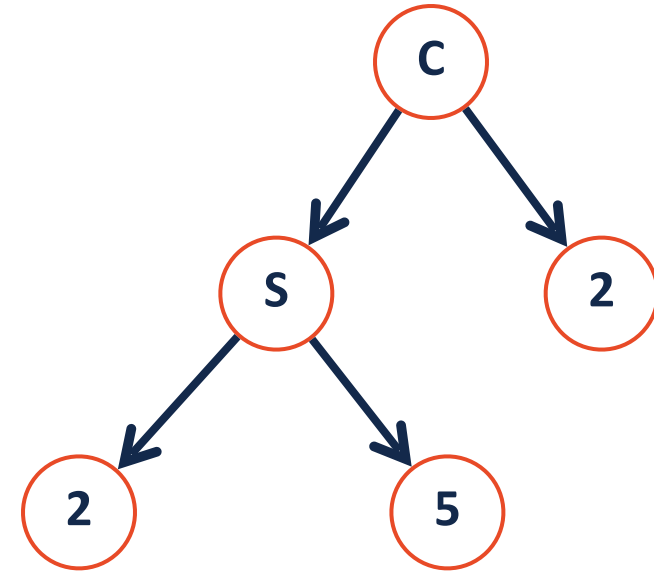


Binary Tree

A **binary tree** is a tree T such that:

1. $T = \emptyset$

2. $T = (data, T_L, T_R)$

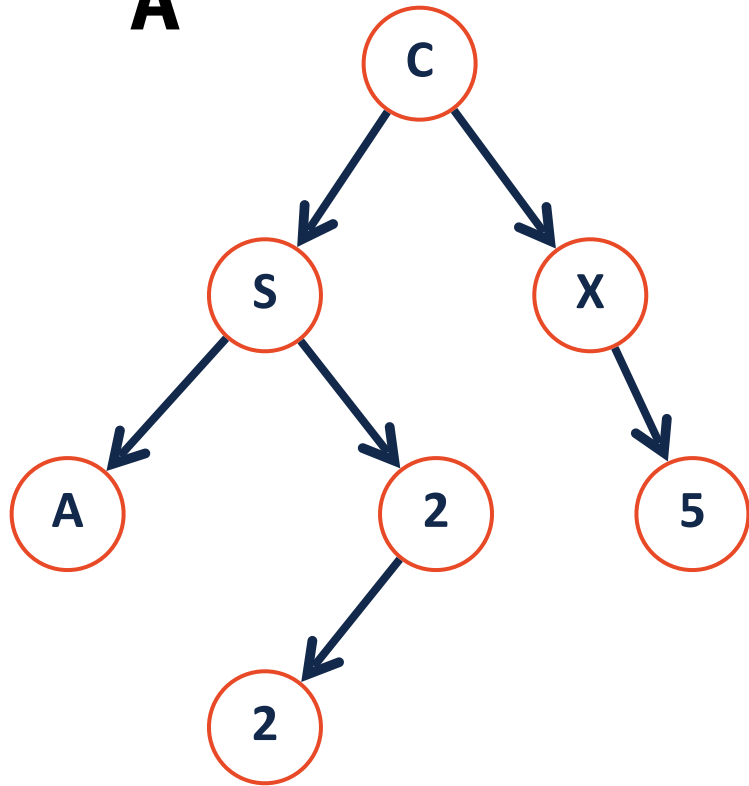


Which of the following are binary trees?

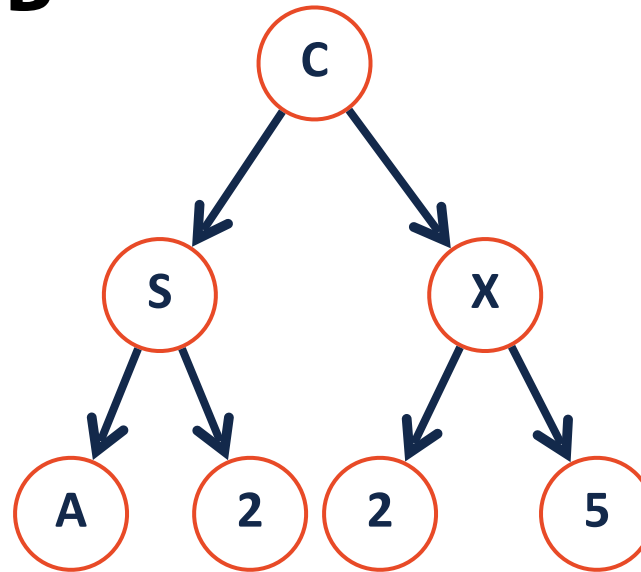


Join Code: 225

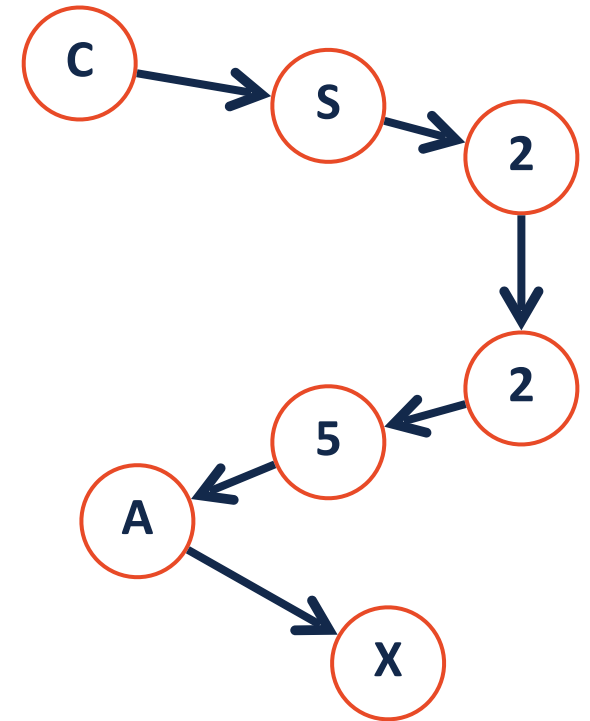
A



B



C





Tree ADT