

Exam 2 (10/02 — 10/04)

Autograded MC and one coding question

Manually graded short answer prompt

Practice exam on PL Corian (e!

Topics covered can be found on website

Registration started September 19

https://courses.engr.illinois.edu/cs225/fa2024/exams/

Additional Extra Credit / Research Opportunity <u>Research Survey</u> by <u>Morgan Fong</u>, PhD student studying CS Education

Study meant to measure sense of belonging in CS courses

You are asked to complete surveys periodically

Completing survey will award +2 bonus points

Points are awarded individually!

Research permission not necessary!

Learning Objectives

Briefly review BST in the context of height

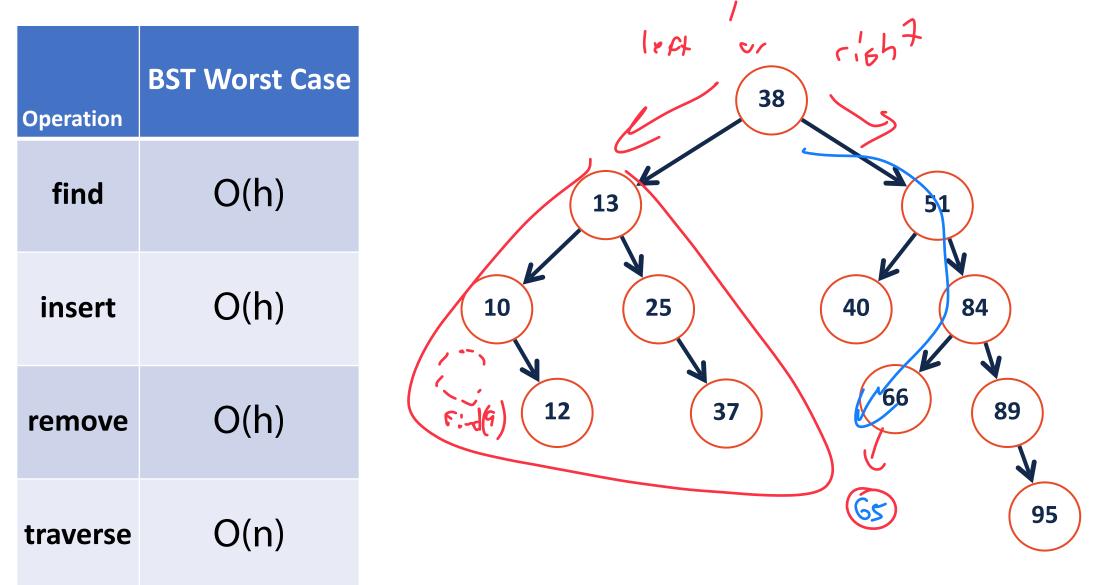
Discuss the big picture problem with BSTs

Introduce the self-balancing BST

BST Analysis – Running Time

BST Worst Case Operation O(h)find O(h)insert O(h)remove O(n) traverse

BST Analysis – Running Time



Every operation on a BST depends on the **height** of the tree.

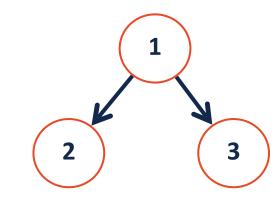
... how do we relate O(h) to n, the size of our dataset?

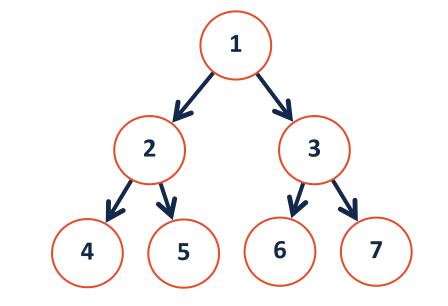
 $f(h) \leq n \leq g(h)$

n=11 of notes **BST** Analysis What is the **max** number of nodes in a tree of height *h* ? po (fect tree h=h = 0hp:54t 1=1 1=0 h=1N=3 りょう V=Q $\gamma = 7$ $\Lambda = \lambda^{h+1} \qquad \sum_{n=1}^{los} (1) \qquad \sum_{n+1}^{los} (1) \qquad \sum_{n+1}^{l$

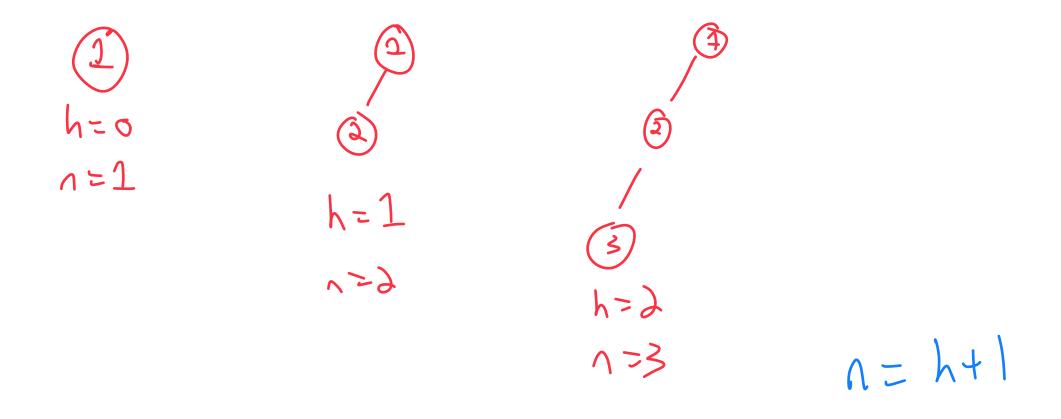
1

What is the **max** number of nodes in a tree of height *h* ?

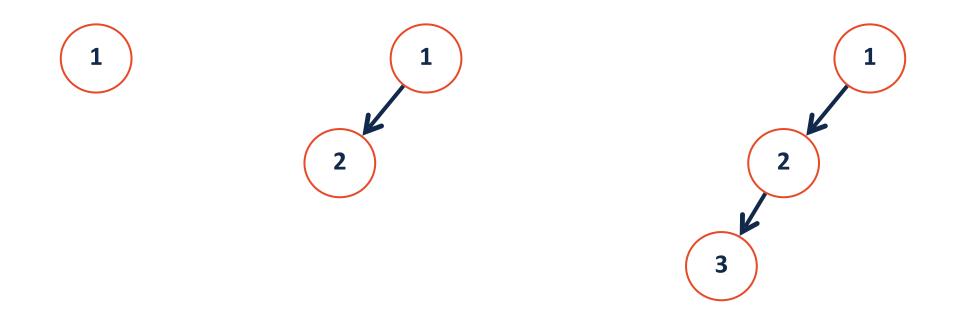


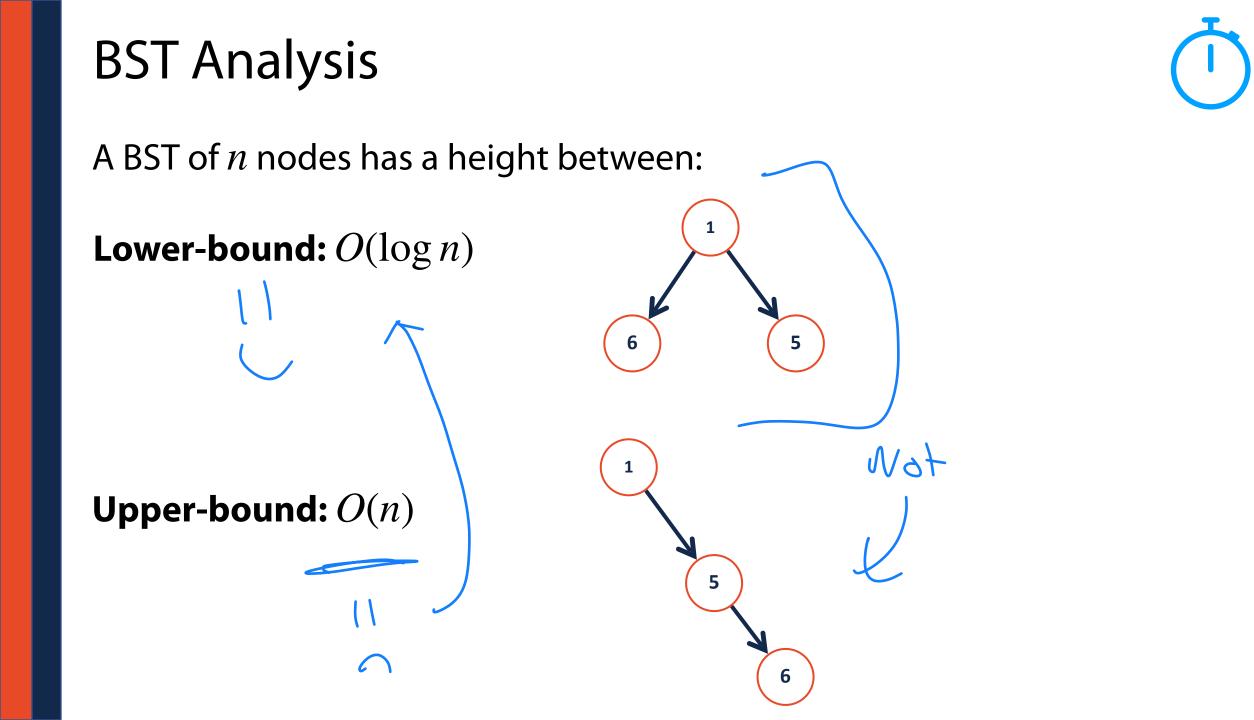


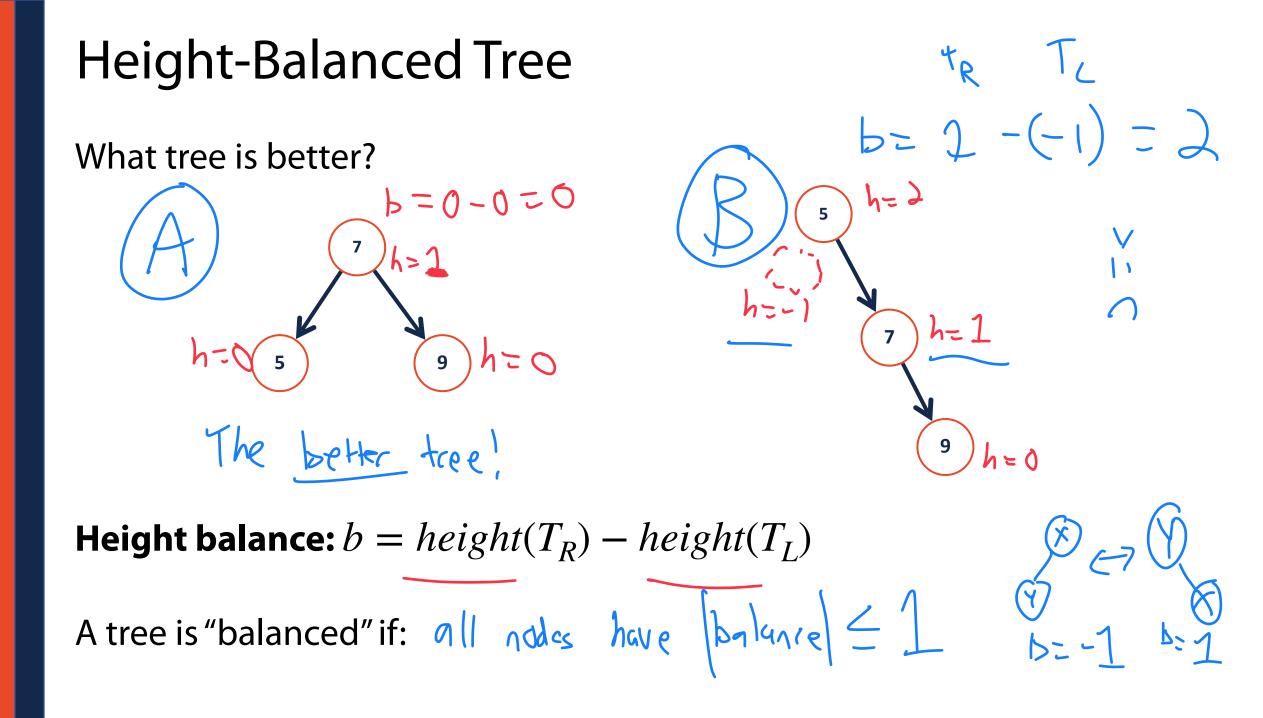
What is the **min** number of nodes in a tree of height *h* ?



What is the **min** number of nodes in a tree of height *h* ?







Option A: Correcting bad insert order

The height of a BST depends on the order in which the data was inserted

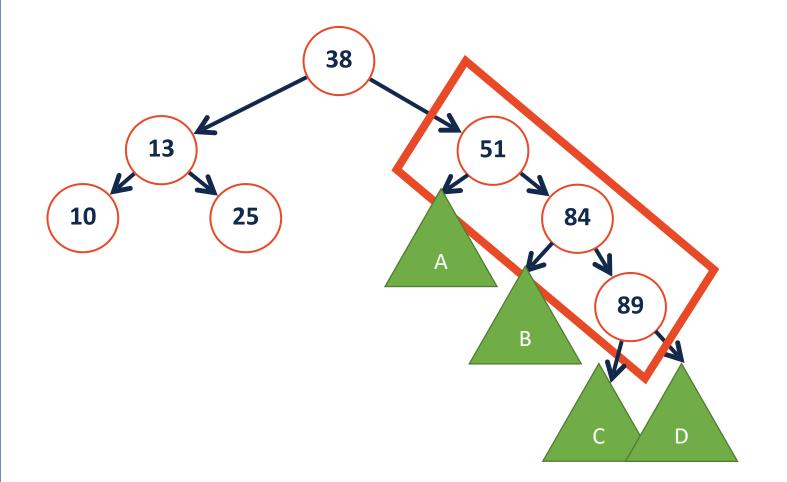
contentares More littely to tuild

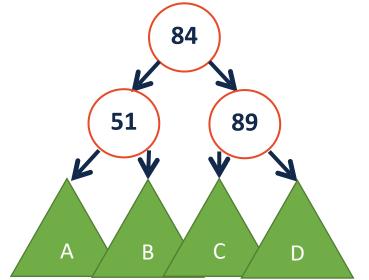
Insert Order: [1, 3, 2, 4, 5, 6, 7]

Insert Order: [4, 2, 3, 6, 7, 1, 5]

AVL-Tree: A self-balancing binary search tree

Rather than fixing an insertion order, just correct the tree as needed!





We can adjust the BST structure by performing **rotations**.

These rotations, when used correctly:

1.

2.

We can adjust the BST structure by performing **rotations**.

These rotations, when used correctly:

2.

1. Modify the arrangement of nodes while preserving BST property

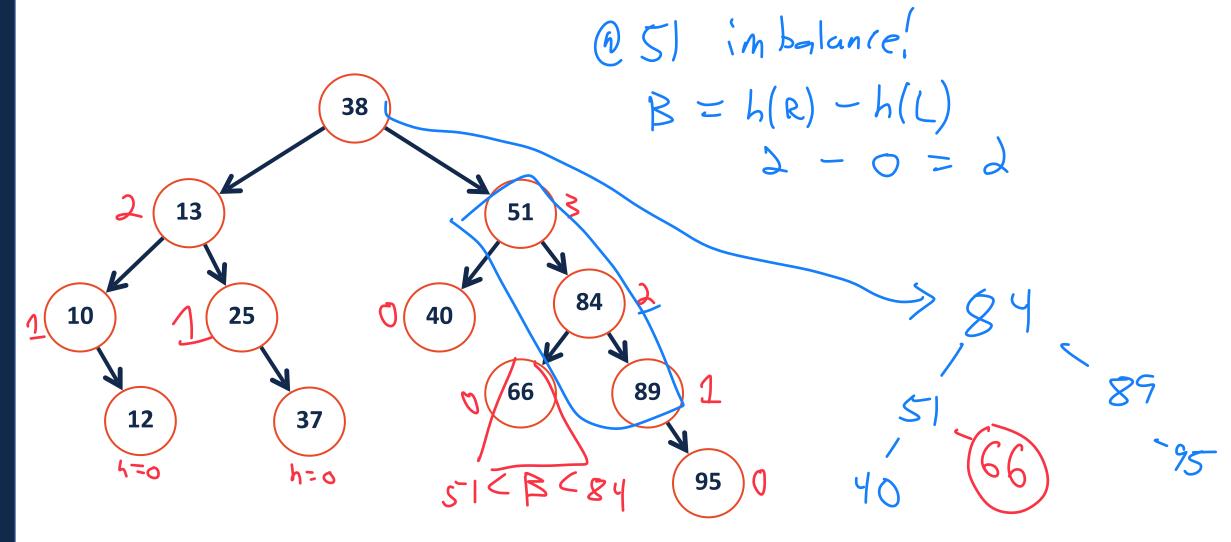
We can adjust the BST structure by performing **rotations**.

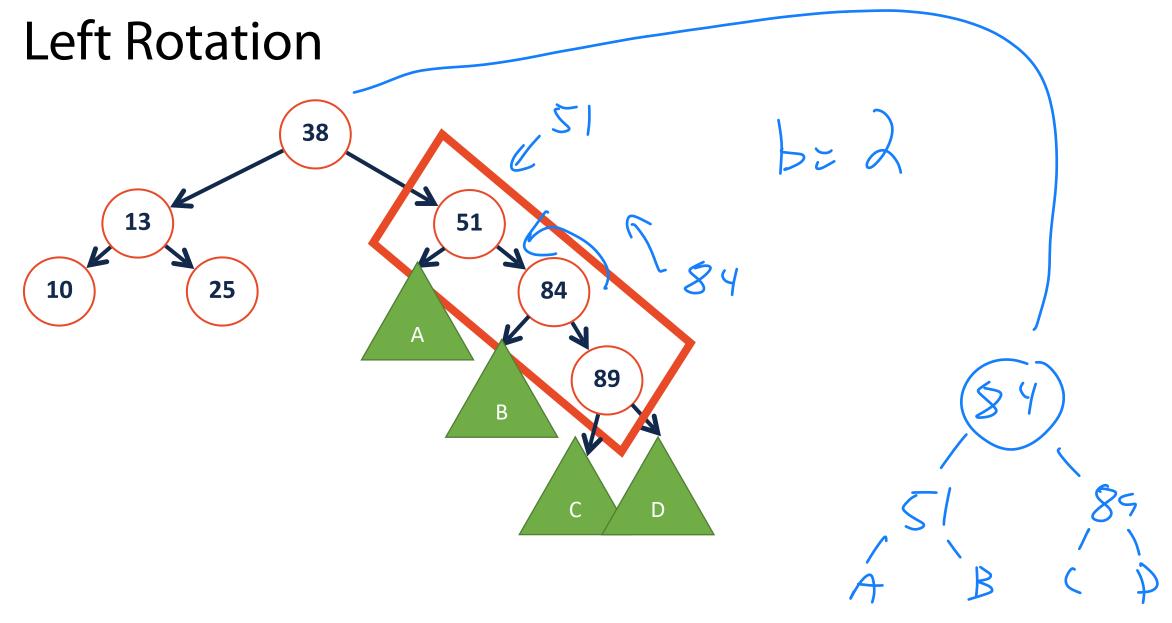
These rotations, when used correctly:

1. Modify the arrangement of nodes while preserving BST property

2. Reduce tree height by one

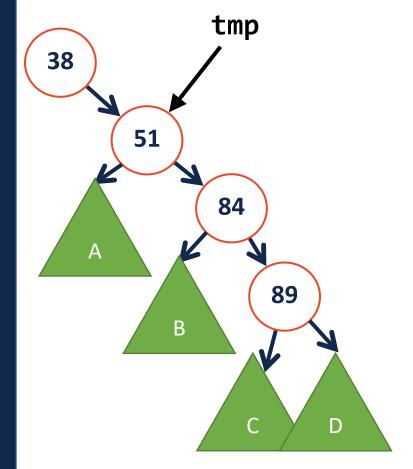
To begin, lets find the imbalance in the following tree:

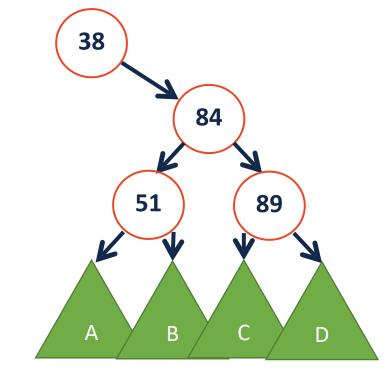




Left Rotation

1) Create a tmp pointer to root

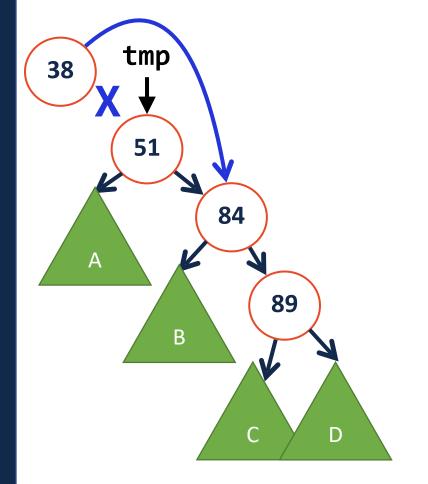


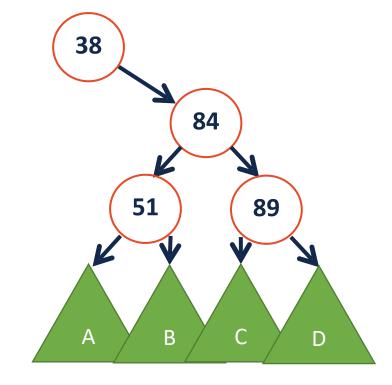




1) Create a tmp pointer to root

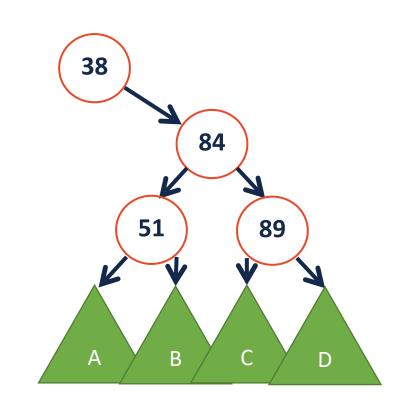
2) Update root to point to mid

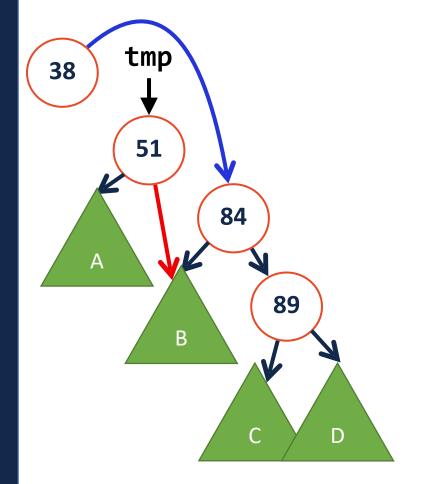




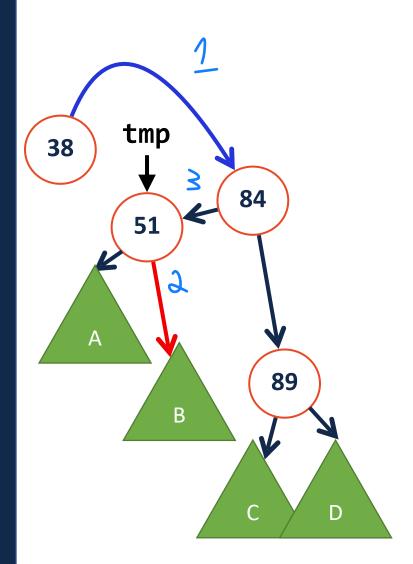
Left Rotation

Create a tmp pointer to root
 Update root to point to mid
 tmp->right = root->left

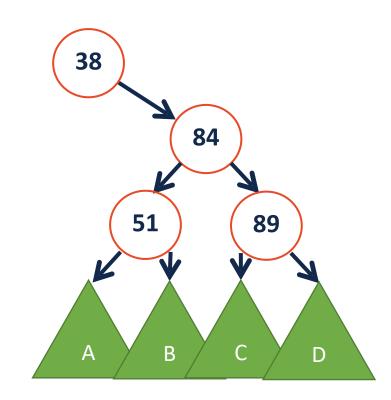




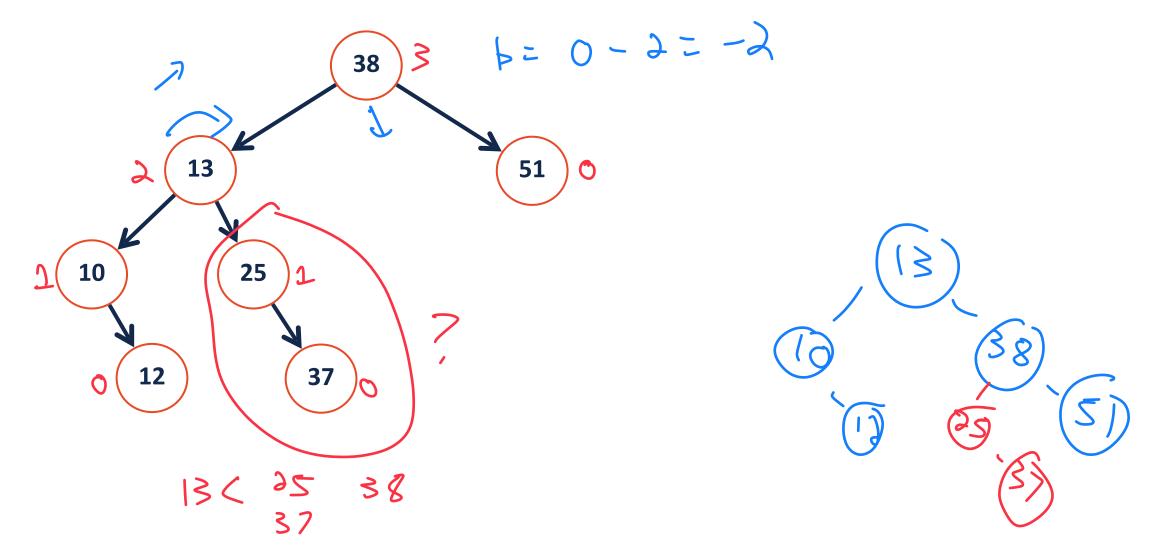
Left Rotation



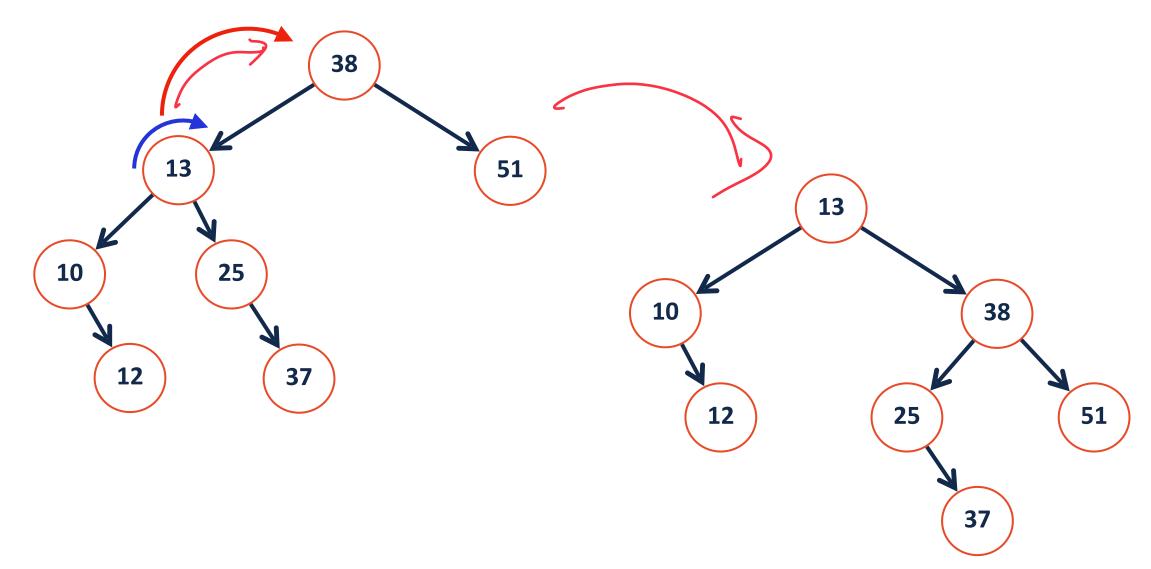
1) Create a tmp pointer to root
2) Update root to point to mid
3) tmp->right = root->left
4) root->left = tmp



Right Rotation



Right Rotation



Coding AVL Rotations

Two ways of visualizing:

1) Think of an arrow 'rotating' around the center

2) Recognize that there's a concrete order for rearrangements

51

В

Α

84

89

D

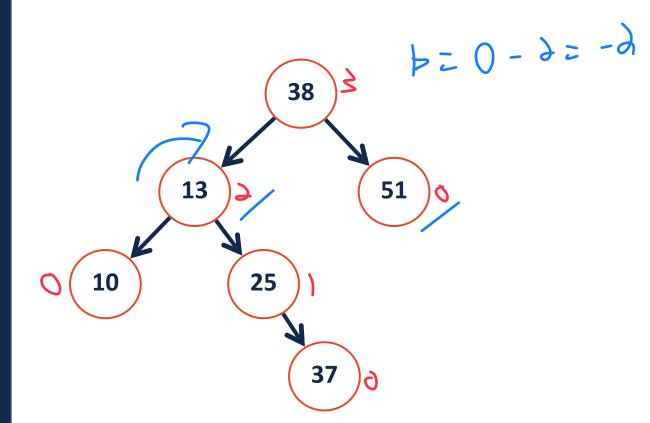
Ex: Unbalanced at current (root) node and need to *rotateLeft*?

Replace current (root) node with it's right child.

Set the right child's left child to be the current node's right

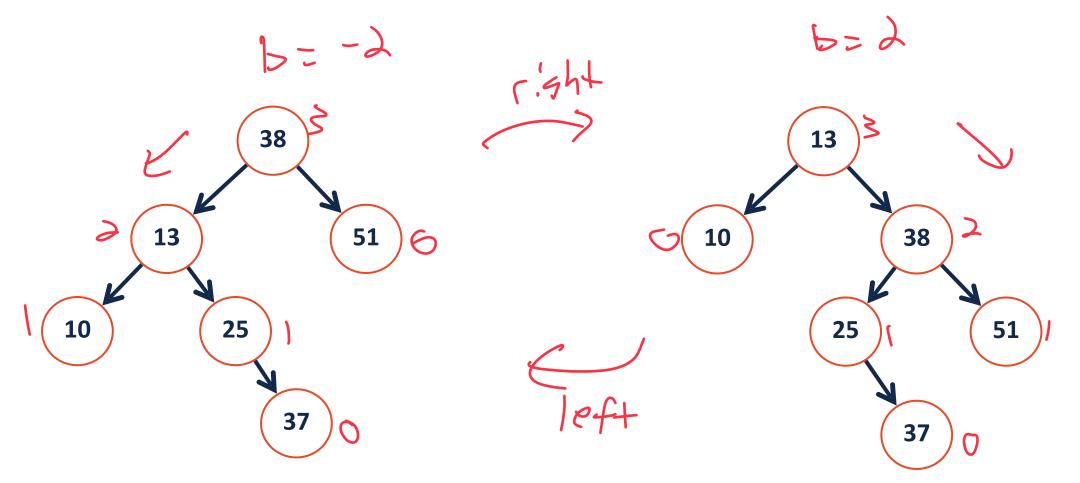
Make the current node the right child's left child

AVL Rotation Practice

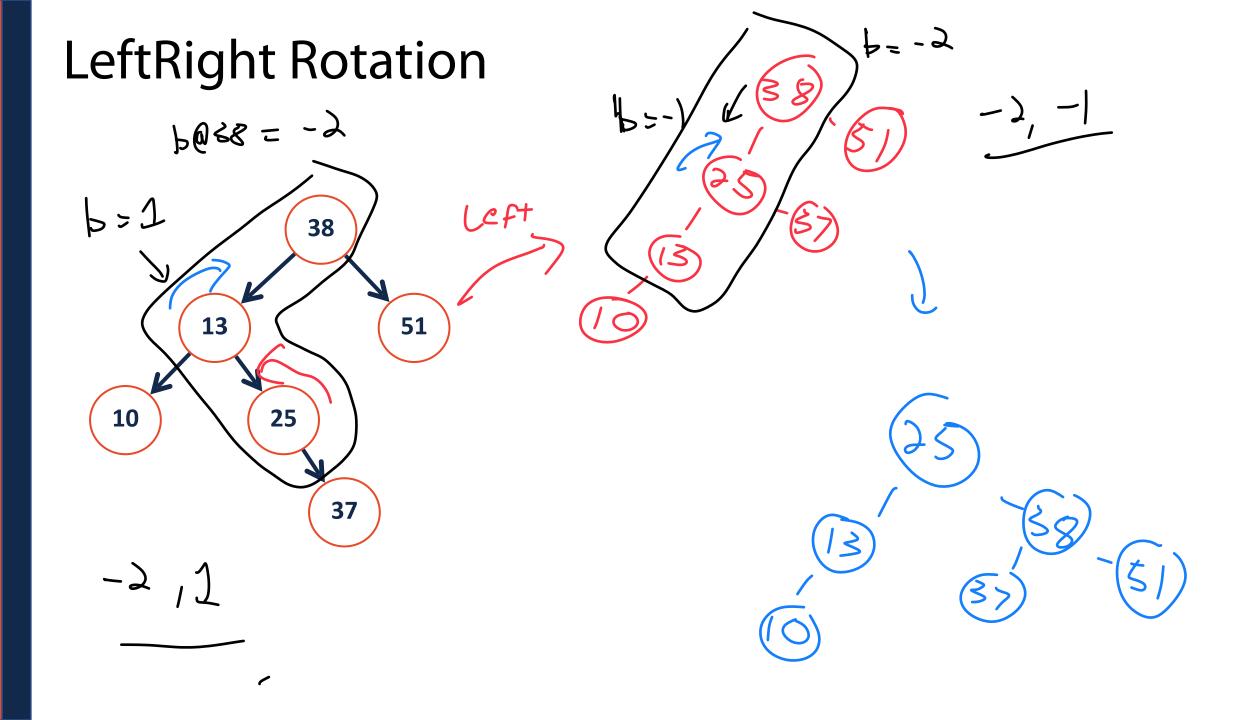


(3 38 0 \ 5 22 ~3>

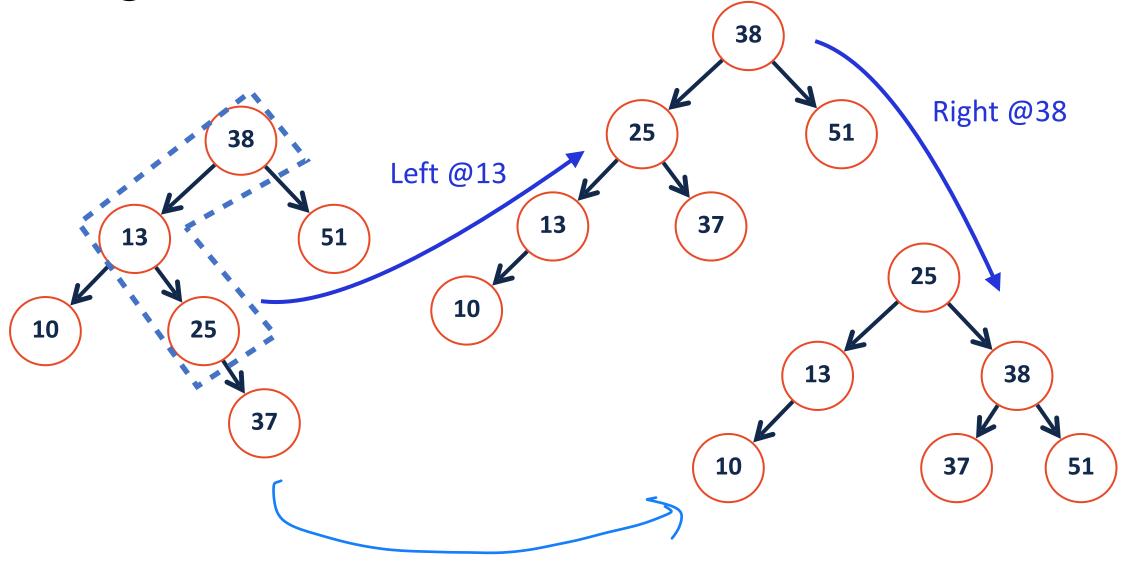
AVL Rotation Practice



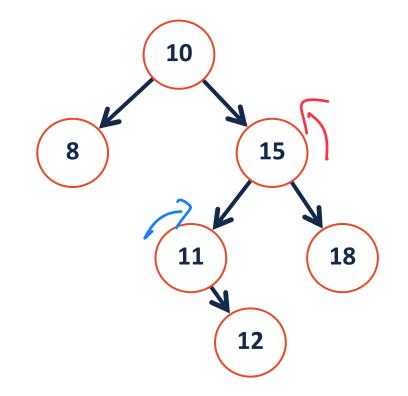
Somethings not quite right...

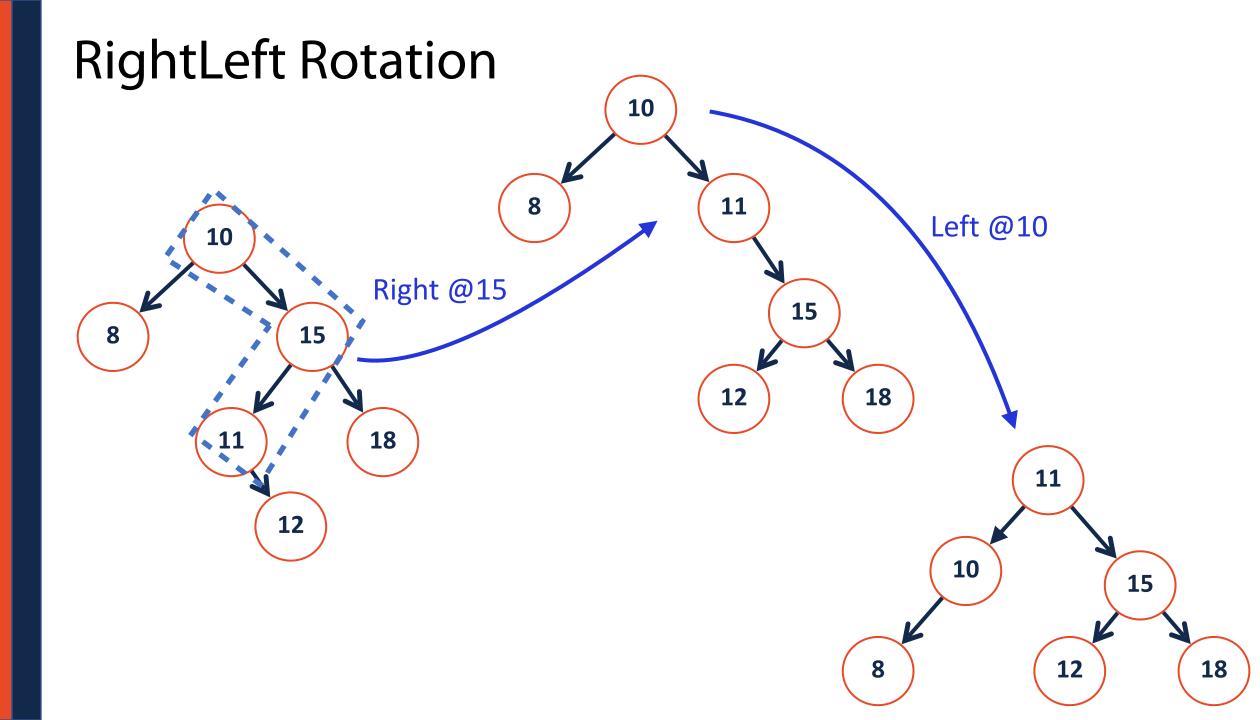


LeftRight Rotation



RightLeft Rotation





AVL Rotations Ceft : 1 ba Lefs inby Right imba Right imbg a _ 2 Э Left heavy left heavy Right heavy Rish heavy 0 Ceft Right Right Left Left Right

1) Vour best firend

AVL Rotations

Four kinds of rotations: (L, R, LR, RL)

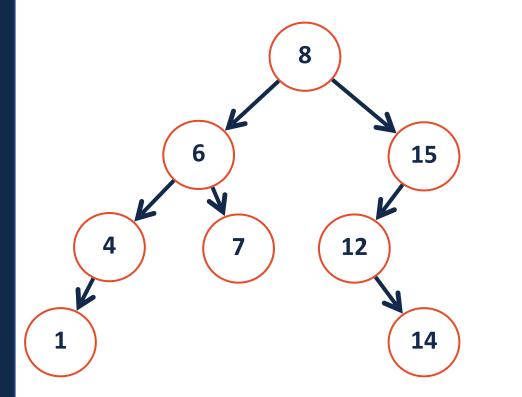
1. All rotations are local (subtrees are not impacted)

2. The running time of rotations are constant

3. The rotations maintain BST property

Goal: Reduce height by One each rotation Maintain q balanced tree

AVL Rotation Practice



AVL vs BST ADT

The AVL tree is a modified binary search tree that rotates when necessary

How does the constraint on balance affect the core functions?

Find

(at most) Insert - 1 colquion will fix this Remove - More than 1 rotation may needed!