

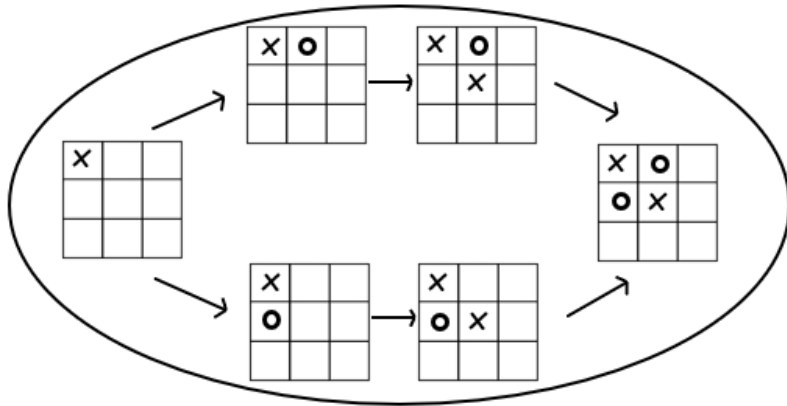
Welcome to Lab Machine Learning!

**Overview:**

In this lab you will learn how to teach computer how to learn to win a game. You will use a graph to represent a state space.

**Using a graph as a state space:**

Before an AI problem can be solved it must be represented as a state space. The state space is then searched to find a solution to the problem. A state space essentially consists of a set of nodes representing each state of the problem, arcs between nodes representing the legal moves from one state to another, an initial state and a goal state. Each state space takes the form of a tree or a graph. For visualization take a look partial state space for tic-tac-toe:



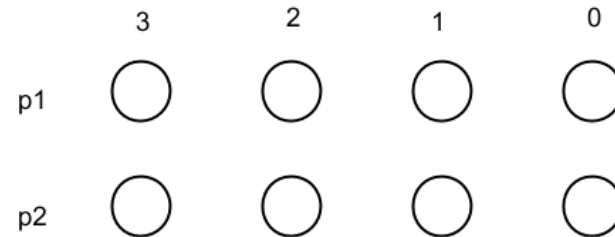
**The Game of Nim**

A game starts with  $k$  tokens. Players alternate turns with **Player 1** starting the game. Each turn, a player may pick up **1 or 2 tokens**. The player who picks up last token wins.

**Exercise 1.1:** How would you represent each state in this game?

*HINT:* What do we need to keep track of in each state?

**Exercise 1.2:** Connect the states in the following state space graph for a game with starting tokens  $k = 3$ : **Nim(3)**



**Exercise 1.3:** Which states are logically unreachable?

**Reinforcement learning:**

Finally, we need to apply reinforcement learning. In reinforcement learning, an algorithm is rewarded for making a good decision and punished for making a poor decision. We will define a good decision as all decisions made by the player who won. Therefore, if Player 1 took the last token, all choices made by Player 1 are rewarded.

The reward is captured in our algorithm as the edge weight. When we consider a path through the graph, we can find that all edges along a path that has Player 1 winning (eg: the last vertex in the path goes to Player 2 with no tokens remaining, or "p2-0", meaning that Player 1 took the last token), then all choices made by Player 1 (edges where Player 1 is the source vertex) are rewarded by increasing the edge weight by +1 and all choices made by Player 2 are punished by changing the edge weight by -1.

**Exercise 2.1:**

Let's label the state "Player 1 - 5 tokens available" as **p1-5**.  
 What is the label of the state where **p1** wins? What about where **p2** wins?

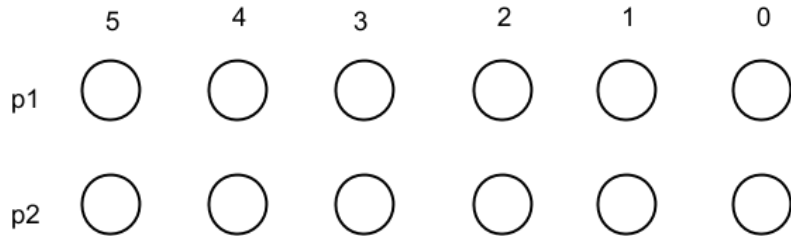
When **p1** wins: \_\_\_\_\_

When **p2** wins: \_\_\_\_\_

**Exercise 2.2:** Given initial edge weights as 0, what will be updated edge weights after the next two games :

1. **p1-5** -> **p2-4** -> **p1-2** -> **p2-1** -> **p1-0**

2. **p1-5** -> **p2-3** -> **p1-2** -> **p2-0**



**Exercise 2.3:** Given the following edge weights for a game **Nim(5)**, find how the trained players would play.

Give the path they will follow. Remember the start state is **p1-5**:

	p1-5	p1-4	p1-3	p1-2	p1-1	p1-0	p2-5	p2-4	p2-3	p2-2	p2-1	p2-0
p1-5								-3000	6000			
p1-4									9600	400		
p1-3										2	-1700	
p1-2											-15000	15000
p1-1												35000
p1-0												
p2-5		-5500	10000									
p2-4			7000	-10								
p2-3				-100	-15000							
p2-2					-18000	18000						
p2-1						32000						
p2-0												

**AFTER YOU'RE DONE WITH LAB CODING:**

**Exercise 2.4:** Would you prefer to go first or second in Nim(10)?

In the programming part of this lab, you will:

- Using a graph as a state space
- Reinforcement learning
- How to teach a computer how to learn to win the game of Ni
- Implement next functions:
  - NimLearner constructor - which creates the vertices and edges for the state space of a game of Nim;
  - playRandomGame - which returns a random path through the graph of the state space as a vector<Edge>.
  - updateEdgeWeights - which updates the edge weights along a given path on the graph of the state space.

**As your TA and CAs, we're here to help with your programming for the rest of this lab section! 😊**