## Bit Vectors

$\mathrm{A}=1011001001, \mathrm{~B}=0110001111$
$A \cup B=$
$A \cap B=$
$A \gg 2=$
$B \ll 2=$

## Cardinality

Cardinality is a measure of:

## Cardinality Estimation

If I randomly sampled values from o - 999 (no repeats) and told you that the minimum value was 300 , what is your best estimate for the cardinality in the random set?

What if the minimum value was 20 ?

## K-minimum Estimation

Will the k-th minimum give me a better, worse, or the same estimation accuracy as the minimum? Why?

## K-minimum Estimation Equation

Given a range of values $m$ and the $k$-th minimum value, what equation can be used to estimate the cardinality?

Can you modify the equation if we don't assume our range is $[0,1)$ ?

## Set Review

$$
\begin{aligned}
& \mathbf{A}=\{\mathbf{1}, \mathbf{2}, \mathbf{3}, \mathbf{4}\}, \mathrm{B}=\{\mathbf{3}, \mathbf{4}, \mathbf{5}, \mathbf{6}, \mathbf{7}\} \\
& A \cup B=
\end{aligned}
$$

$A \cap B=$

## Jaccard Similarity

What is the equation for the Jaccard similarity? What is the similarity for the above A and B?

## MinHash Sketch

The MinHash sketch is an approximation strategy that reduces a dataset down to an ordered set of integers. What three things does the constructor take as input to do this?
1.
2.

## 3.

The MinHash sketch can be used to estimate two properties about a dataset. What are they?
1.
2.

## MinHash Construction

Describe three ways to build a MinHash sketch. Why would you pick one over another?
1.

## Estimating Similarity

Given the bottom 8 minimum hash values for A and B (below), estimate the similarity of the sets using an approximation of intersection and union.
$\mathrm{A}=\{3,7,8,11,15,17,22,23\}$
$B=\{2,3,6,7,9,11,17,23\}$

Repeat the same calculation, but this time using the inclusionexclusion principle (also known as 'double counting') to estimate the similarity without using the intersection.

