# CS 225 

## Data Structures

## October 20 - Hashing

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## Hashing

Goals:
We want to define a keyspace, a (mathematical) description of the keys for a set of data.
...use a function to map the keyspace into a small set of integers.

## Hashing



## A Hash Table based Dictionary

Client Code:
1 Dictionary<KeyType, ValueType> d; $\mathrm{d}[\mathrm{k}]=\mathrm{v}$;

A Hash Table consists of three things:

1. A hash function, $f(k)$
2. An array
3. Something to handle chaos when it occurs!

## A Perfect Hash Function

(Angrave, CS 241)
(Bailey, CS 465)
(Challen, CS 124)
(Davis, CS 101)
(Evans, CS 225)
(Fagen-Ulmschneider, CS 240)
(Gunter, CS 464)
(Herman, CS 233)

## A Perfect Hash Function

| Key | Value |
| :--- | :--- |
| 0 |  |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| 6 |  |
| 7 |  |
| 8 |  |
| 9 |  |
| 10 |  |
| 11 |  |
| 12 |  |
| 13 |  |
| 14 |  |
| 15 |  |

## Hash Function

Our hash function consists of two parts:

- A hash:
- A compression:

Choosing a good hash function is tricky...

- Don't create your own (yet*)
- Very smart people have created very bad hash functions


## Hash Function

Characteristics of a good hash function:

1. Computation Time:
2. Deterministic:
3. Satisfy the SUHA:

## General Purpose Hash Function

Keyspaces


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Keyspaces


Easy to create if: |KeySpace| ~ N

## General Purpose Hash Function

Keyspaces


Easy to create if: |KeySpace| ~ N






## Hash Function

Given: Easy to create a hash function of strings of length 8.

## Idea: Map 40 character things to length 8:

```
Alice was beginning to get very tired of
    sitting by her sister on the bank, and
of having nothing to do: once or twice s
he had peeped into the book her sister w
as reading, but it had no pictures or co
nversations in it, 'and what is the use
of a book,' thought Alice 'without pictu
res or conversations?' So she was consi
dering in her own mind (as well as she c
ould, for the hot day made her feel very
    sleepy and stupid), whether the pleasur
e of making a daisy-chain would be worth
    the trouble of getting up and picking t
he daisies, when suddenly a White Rabbit
    with pink eyes ran close by her. There
    was nothing so very remarkable in that;
    nor did Alice think it so very much out
    of the way to hear the Rabbit say to it
self, 'Oh dear! Oh dear! I shall be late
!' (when she thought it over afterwards,
    it occurred to her that she ought to ha
```


## Idea: Map 40 character things to length 8:

```
https://en.wikipedia.org/wiki/Main_Page
https://en.wikipedia.org/wiki/Battle of
https://en.wikipedia.org/wiki/Vector_Gen
https://en.wikipedia.org/wiki/2017_Austr
https://en.wikipedia.org/wiki/19th_Natio
https://en.wikipedia.org/wiki/Japanese_g
```


## Hash Function

In CS 225, we focus on general purpose hash functions.

Other hash functions exists with different properties (eg: cryptographic hash functions)

Collision Handling: Separate Chaining

$$
\begin{array}{ll}
S=\{16,8,4,13,29,11,22\} & |S|=n \\
h(k)=k \% 7 & |A r r a y|=N
\end{array}
$$

Collision Handling: Probe-based Hashing
$S=\{16,8,4,13,29,11,22\}$
|S| = n
$h(k)=k \% 7$
|Array| = N


Try h(k) = (k + 0) \% 7, if full...
Try $h(k)=(k+1) \% 7$, if full...
Try $h(k)=(k+2) \% 7$, if full...

