# CS 225 

## Data Structures

## October 6-BST Balance

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BST Analysis
Therefore, for all BST:
Lower bound: $h>=\mathbf{O}(\lg (n)$ )
Upper bound: $\mathrm{h}<=\mathbf{O}(\mathrm{n})$

## BST Analysis

The height of a BST depends on the order in which the data is inserted into it.

$$
\text { ex: } 1324576 \text { vs. } 4236715
$$

Q: How many different ways are there to insert keys into a BST?

Q: What is the average height of all the arrangements?

## BST Analysis - Running Time

| Operation | BST <br> Average case | BST <br> Worst case | Sorted array | Sorted List |
| :---: | :---: | :---: | :---: | :---: |
| find |  |  |  |  |
| insert |  |  |  |  |
| delete |  |  |  |  |
| traverse |  |  |  |  |

## Height-Balanced Tree

What tree makes you happier?


Height balance: $b=\operatorname{height}\left(T_{R}\right)-\operatorname{height}\left(T_{L}\right)$

A tree is height balanced if:


## BST Rotation

We will perform a rotation that maintains two properties:
1.
2.







## BST Rotation Summary

- Four kinds of rotations (L, R, LR, RL)
- All rotations are local (subtrees are not impacted)
- All rotations are constant time: O(1)
- BST property maintained

GOAL:

We call these trees:

## AVL Trees

Three issues for consideration:

- Rotations
- Maintaining Height
- Detecting Imbalance

