# CS 225

#### **Data Structures**

Oct. 7 – BST Balance G Carl Evans

#### **BST** Analysis

Therefore, for all BST: Lower bound: h >= O( lg(n) )

Upper bound:  $h \le O(n)$ 

#### **BST** Analysis

The height of a BST depends on the order in which the data is inserted into it.

ex: 1324576 vs. 4236715

**Q:** How many different ways are there to insert keys into a BST?

**Q:** What is the average height of all the arrangements?

#### **BST** Analysis

**Q:** How many different ways are there to insert keys into a BST?

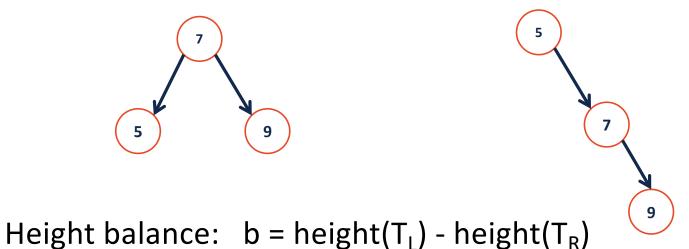
**Q:** What is the average height of all the arrangements?

## BST Analysis – Running Time

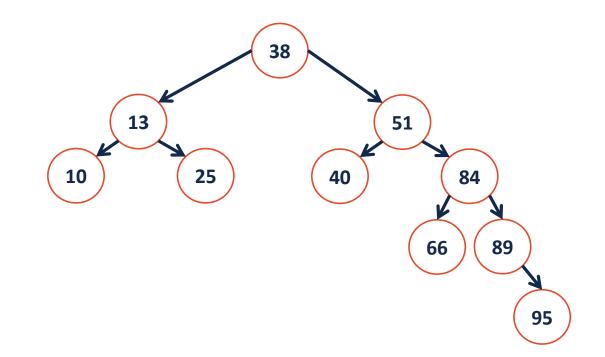
Operation	BST Average case	BST Worst case	Sorted array	Sorted List
find				
insert				
delete				
traverse				

#### Height-Balanced Tree

What tree makes you happier?



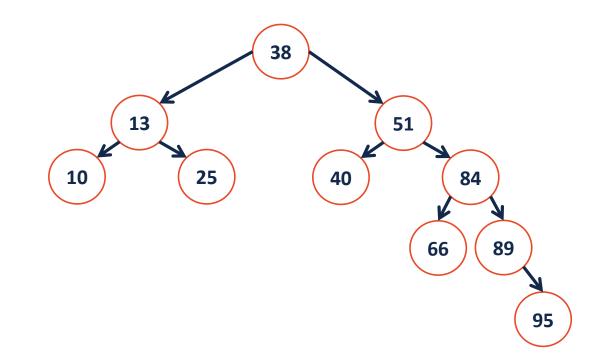
A tree is height balanced if:

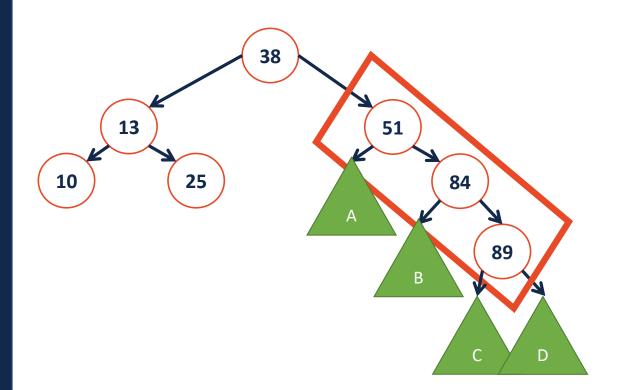


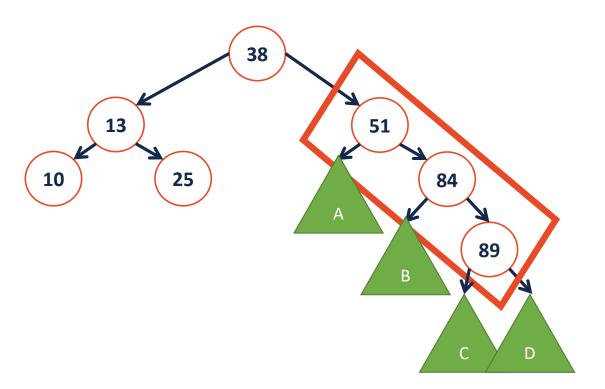
#### **BST** Rotation

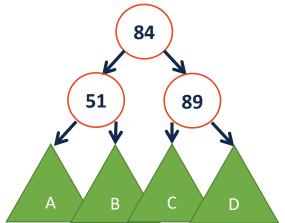
We will perform a rotation that maintains two properties: **1**.

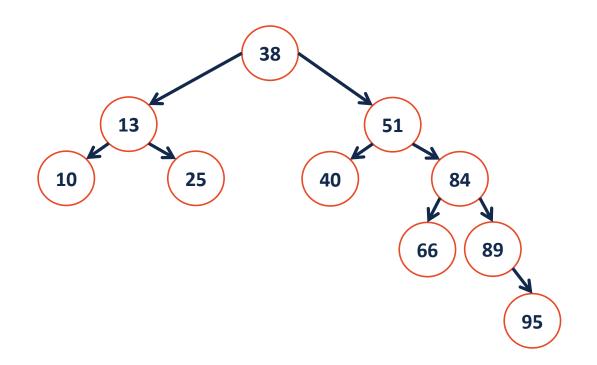
2.

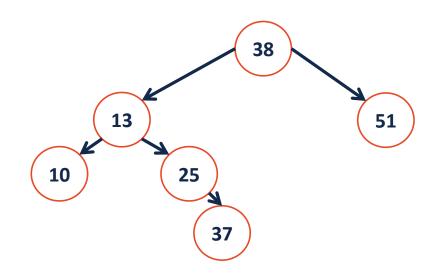


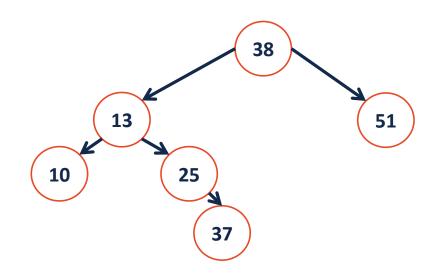












### **BST Rotation Summary**

- Four kinds of rotations (L, R, LR, RL)
- All rotations are local (subtrees are not impacted)
- All rotations are constant time: O(1)
- BST property maintained

#### GOAL:

We call these trees:

## **AVL Trees**

Three issues for consideration:

- Rotations
- Maintaining Height
- Detecting Imbalance