Every hash table contains three pieces:

1. A hash function, $\mathbf{f}(\mathbf{k})$. The hash function transforms a key from the keyspace into a small integer.
2. An array.
3. A third element that handles chaos when it occurs.

## A Perfect Hash Function


...characteristics of this function?

## A Second Hash Function


...characteristics of this function?

All hash functions will consist of two parts:

- A hash:
- A compression:

Characteristics of a good hash function:

1. Computation Time:
2. Deterministic:
3. SUHA:

## Towards a general-purpose hashing function:

It is easy to create a general-purpose hashing function when the keyspace is proportional to the table size:

- Ex: Professors at CS@Illinois
- Ex: Anything you can reason about every possible value

It is difficult to create a general-purpose hashing function when the keyspace is large:


## My 40-character strategy:

$$
\begin{aligned}
& \text { Alice was beginning to get very tired of } \\
& \text { sitting by her sister on the bank, and } \\
& \text { of having nothing to do: once or twice s } \\
& \text { he had peeped into the book her sister } \\
& \text { as reading, but it had no pictures or co } \\
& \text { nversations in it, 'and what is the use } \\
& \text { of a book,' thought Alice 'without pictu } \\
& \text { res or conversations?' So she was consi } \\
& \text { dering in her own mind (as well as she c } \\
& \text { ould, for the hot day made her feel very } \\
& \text { sleepy and stupid), whether the pleasur } \\
& \text { e of making a daisy-chain would be worth } \\
& \text { the trouble of getting up and picking t } \\
& \text { he daisies, when suddenly a White Rabbit } \\
& \text { with pink eyes ran close by her. There } \\
& \text { was nothing so very remarkable in that; } \\
& \text { nor did Alice think it so very much out } \\
& \text { of the way to hear the Rabbit say to it } \\
& \text { self, 'Oh dear! Oh dear! I shall be late } \\
& \text { !' (when she thought it over afterwards, } \\
& \text { it occurred to her that she ought to ha }
\end{aligned}
$$

...what is a naïve hashing strategy for this input?
...characteristics of this function?

What is an example of bad input data on this hash function?

## Reflections on Hashing

We are starting the study of general-purpose hash functions. There are many other types of hashes for specific uses (ex: cryptographic hash functions).

Even if we build a good hash function, it is not perfect. What happens when the function isn't always a bijection?

## Collision Handling Strategy \#1: Separate Chaining

Example: $\mathbf{S}=\{\mathbf{1 6}, \mathbf{8}, \mathbf{4}, \mathbf{1 3}, \mathbf{2 9}, \mathbf{1 1}, 22\},|\mathbf{S}|=\mathbf{n}$

$$
\mathbf{h}(\mathbf{k})=\mathbf{k} \% 7
$$

$\mid$ Array $\mid=\mathbf{N}$

| $[0]$ |  |
| ---: | ---: |
| $[1]$ |  |
| $[2]$ |  |
| $[3]$ |  |
| $[4]$ |  |
| $[5]$ |  |
| $[6]$ |  |
| $[7]$ |  |

## Load Factor:

Running time of Separate Chaining:

|  | Worst Case | SUHA |
| :--- | :--- | :--- |
| Insert |  |  |
| Remove/Find |  |  |

## CS 225 - Things To Be Doing:

1. Programming Exam B starts tomorrow
2. $\mathrm{MP}_{5}$ has been released; $\mathrm{EC}^{+7}$ deadline is Monday
3. lab_btree released today
4. Daily POTDs are ongoing!
