



CS 225

Data Structures

Oct. 23 – BTree

B-Trees

Q: Can we always fit our data in main memory?

Q: Where else can we keep our data?

However, big-O assumes uniform time for all operations.

Vast Differences in Time

A **3GHz** CPU performs 3m operations in _____.

Old Argument: “Disk Storage is Slow”

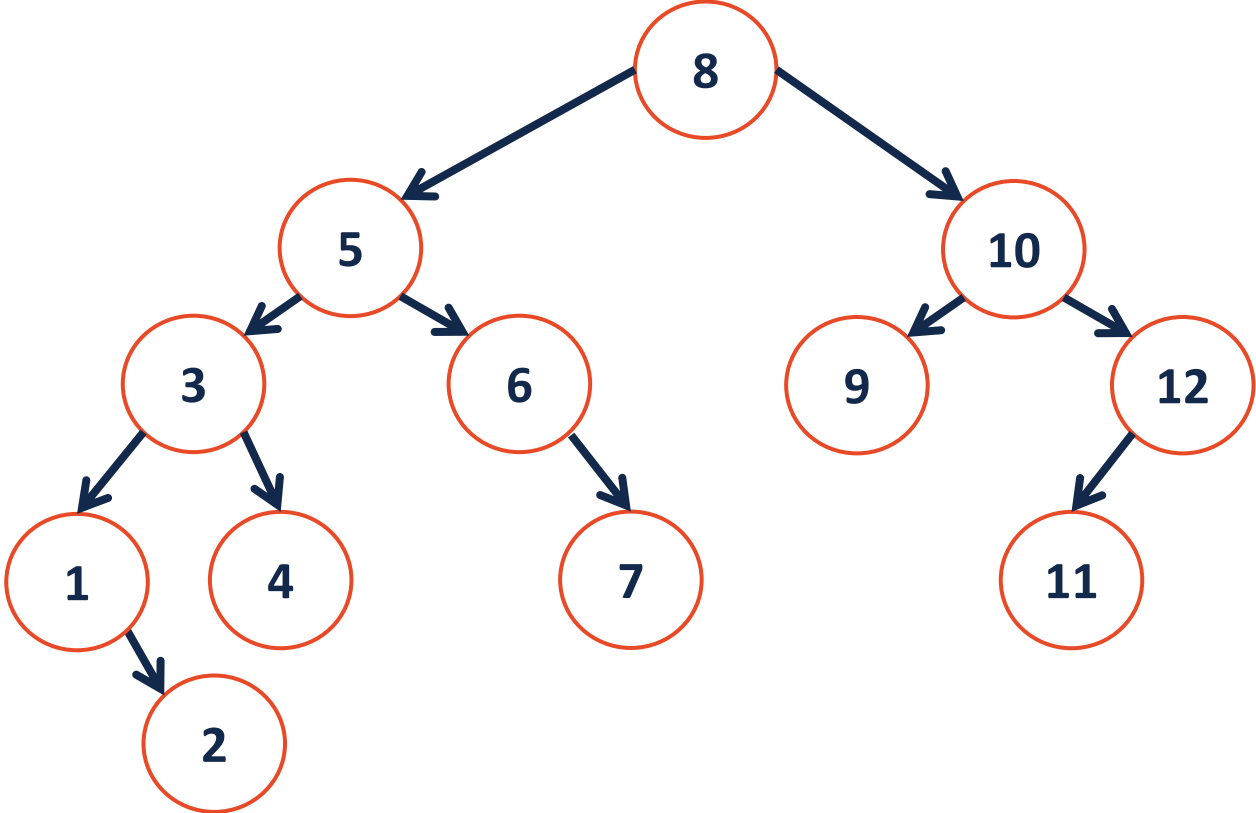
- Bleeding-edge storage is pretty fast:

NVMe (M.2, PCIe 3.0 x4):

- Large Disks (10 TB+) still have slow throughput:

New Argument: “The Cloud is Slow!”

AVLs on Disk



Real Application

Imagine storing driving records for everyone in the US:

How many records?

How much data in total?

How deep is the AVL tree?

Exams

Exam 7 (Theory Exam)

- Live right now!

Exam 8 (Programming Exam)

- Review Assignments: MP4, lab_avl
- Topics: AVL trees, iterators

Share Your #cs225animation

On Facebook/Twitter/Instagram:

#cs225animation

...I'll search this tag every few days and like/heart your work!

On Piazza:

See pinned post: "MP4: Animation Sharing"

BTree Motivations

Knowing that we have large seek times for data, we want to:

BTree (of order m)

-3	8	23	25	31	42	43	55
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m=9

Goal: Minimize the number of reads!

Build a tree that uses _____ / node
[1 network packet]
[1 disk block]

BTree Insertion

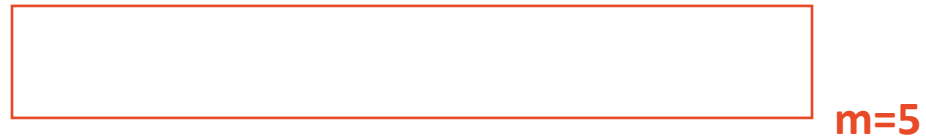
A **BTree** of order **m** is an m-way tree:

- All keys within a node are ordered
- All leaves contain hold no more than **m-1** nodes.

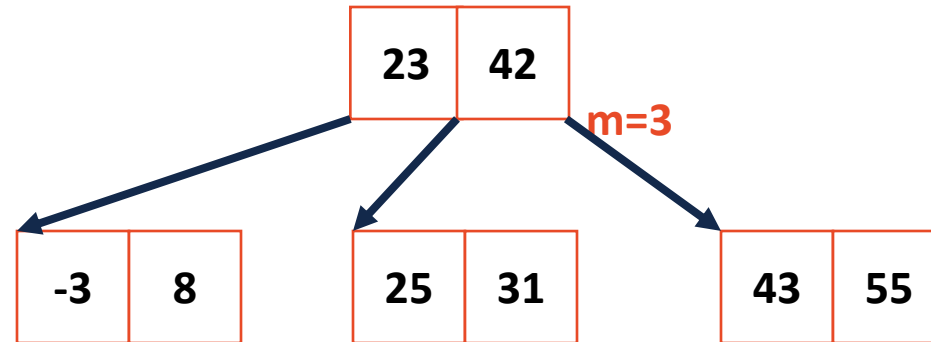


BTree Insertion

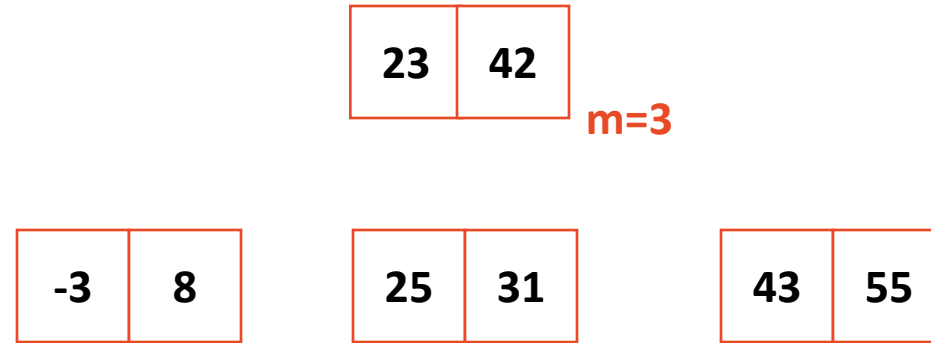
When a BTree node reaches **m** keys:



BTree Recursive Insert



BTree Recursive Insert



BTree Visualization/Tool

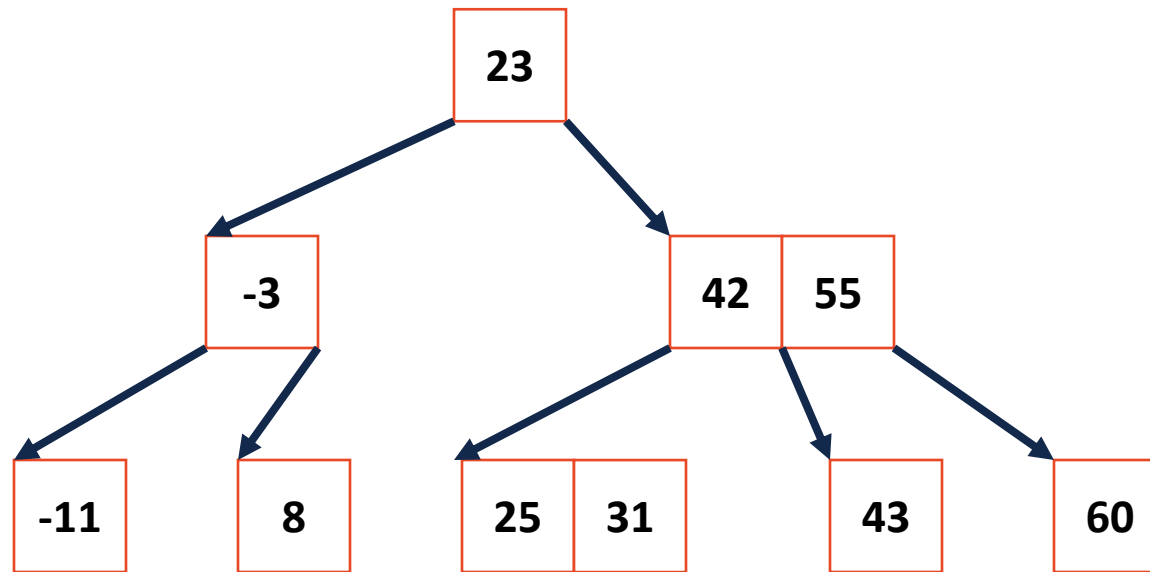
<https://www.cs.usfca.edu/~galles/visualization/BTree.html>

Btree Properties

A **BTree** of order **m** is an m-way tree:

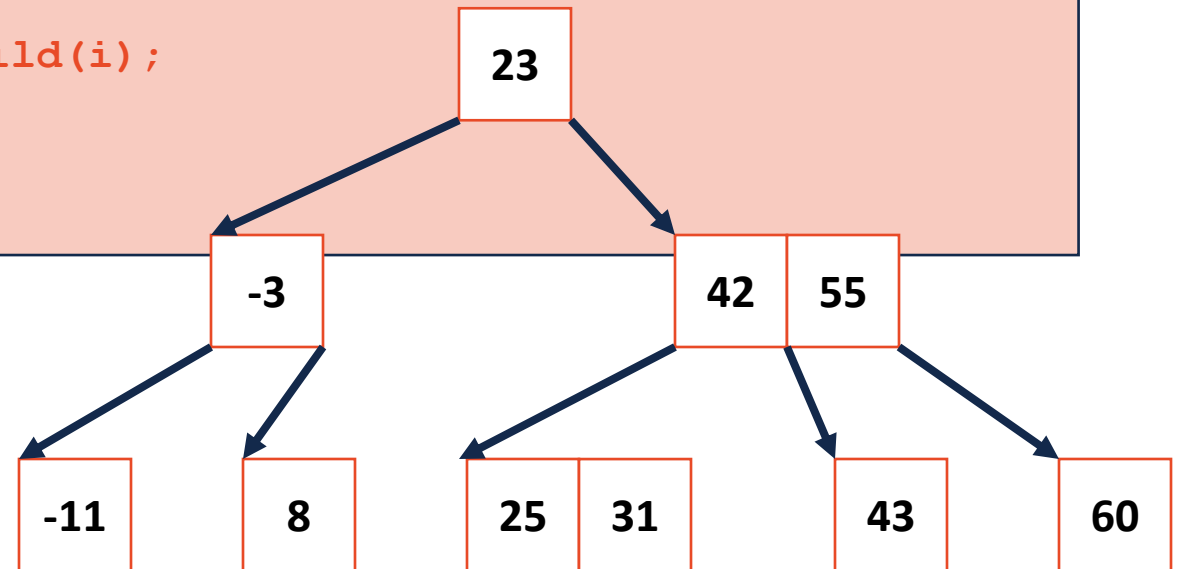
- All keys within a node are ordered
- All leaves contain hold no more than **m-1** nodes.
- All internal nodes have exactly **one more key than children**
- Root nodes can be a leaf or have **[2, m]** children.
- All non-root, internal nodes have **[ceil(m/2), m]** children.
- All leaves are on the same level

BTree Search



BTree Search

```
1 bool Btree::_exists(BTreeNode & node, const K & key) {
2
3     unsigned i;
4     for ( i = 0; i < node.keys_ct_ && key < node.keys_[i]; i++) { }
5
6     if ( i < node.keys_ct_ && key == node.keys_[i] ) {
7         return true;
8     }
9
10    if ( node.isLeaf() ) {
11        return false;
12    } else {
13        BTreeNode nextChild = node._fetchChild(i);
14        return _exists(nextChild, key);
15    }
16 }
```



BTree Analysis

The height of the BTree determines maximum number of _____ possible in search data.

...and the height of the structure is: _____.

Therefore: The number of seeks is no more than _____.

...suppose we want to prove this!

BTree Analysis

In our AVL Analysis, we saw finding an upper bound on the height (given n) is the same as finding a lower bound on the nodes (given h).

We want to find a relationship for BTrees between the number of keys (n) and the height (h).

CS 225 – Things To Be Doing

Exam 7 (theory) starts Monday!

Review Document: On Piazza

Review Session: 7pm, 1404 SC

More Info: <https://courses.engr.illinois.edu/cs225/fa2017/exams/>

MP4: Due Monday

Due: Monday, Oct. 23 at 11:59pm

Lab: lab_avl

Due Sunday, Oct. 22 at 11:59pm

POTD

Every Monday-Friday – *Worth +1 Extra Credit /problem (up to +40 total)*