

L<sub>1</sub>: So it's gonna be forever  
 L<sub>2</sub>: Or it's gonna go down in flames  
 L<sub>3</sub>: You can tell me when it's over

- Taylor Swift, Blank Space

### Text Similarity

**tf-idf** is a classical measure of text similarity, allowing us to establish a base similarity metric between similar regions of text.

**tf**, term frequency asks “how often does the word appear?”

**idf**, inverse document frequency asks “how rare is the word?”

### Calculating tf-idf

**First**, we calculate the tf-idf for every word in every line:

- (a): How many regions does our document have?      #regions:  
 (b): How many regions does [it's] appear?      #(it's)<sub>regions</sub>:  
 (c): How many times does [it's] appear in L<sub>1</sub>?      **tf** = L<sub>1</sub>(it's):  
 (d): Calculate the idf of [it's] on L<sub>1</sub>:      **idf** = log( (a) / (b) ):  
 (e): Calculate tf-idf of [it's] on L<sub>1</sub>:      **tf-idf** = (c) \* (d):

Second, we calculate the **cosine similarity** of each tf-idf:

$$\text{similarity} = \cos(\theta) = \frac{A \cdot B}{\|A\| \|B\|} = \frac{\sum_{i=1}^n A_i \times B_i}{\sqrt{\sum_{i=1}^n (A_i)^2} \times \sqrt{\sum_{i=1}^n (B_i)^2}}$$

How often does [it's] appear in L<sub>1</sub>?

			tf			idf			tf-idf		
	#regions	#regions(word)	L <sub>1</sub>	L <sub>2</sub>	L <sub>3</sub>	L <sub>1</sub>	L <sub>2</sub>	L <sub>3</sub>	L <sub>1</sub>	L <sub>2</sub>	L <sub>3</sub>
so											
it's											
gonna											
be											
forever											
or											
go											
down											
in											
flames											
you											
can											
tell											
me											
when											
over											

How do we set up a cosine similarity?