

The “AM-HM” Inequality

Prove by induction that $\forall n \geq 1$, if $x_1 \cdots x_n$ are positive reals then $(\sum_{i=1}^n x_i)(\sum_{i=1}^n \frac{1}{x_i}) \geq n^2$.