Special Graphs and Intermediate Definitions

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Learning Objectives

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- Recall definitions related to “moving around” on graphs.

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- a cycle on n vertices?
- a cycle on n vertices, but there's also a hub vertex?
- two separate sets of vertices and every possible edge between?

Walks, Paths, and Cycles

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- G is ***acyclic*** if no cycles as subgraphs
- ***Euler circuit***: closed walk that travels every edge exactly once

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- “islands” called ***connected components***
- ***cut edge***, if removed, would disconnect G

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- The ***diameter*** is the max distance over all pairs of vertices

Recap: Learning Objectives

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