Introduction to Graphs

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Warning

Default assumptions: simple, undirected, at least one vertex, finite

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Theorem (Handshaking Theorem)

Let $G = (V, E)$ be an undirected graph. Then

$$\sum_{v \in V} deg(v) = 2|E|.$$

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