Week 4 Tutorial Problems

1. Constructing a concrete relation

Construct a relation R on the set $\{1,2,3\}$ such that all the following are true:

- 1R2
- \bullet R is symmetric
- \bullet R is transitive
- \bullet R is not an equivalence relation

(You can specify the relation however you want: a diagram with arrows, a table of related pairs, etc.)

2. Discussion manual problems

Do the following problems from the discussion manual:

- 4.2 parts (a) and (b)
- 4.3 part (a), except you do not need to prove the relation is an equivalence relation.
- 4.3 part (b)

3. Abstract relation proof

Let R and S be symmetric relations on some set A. Define a relation \sim on A such that $x \sim y$ if and only if xRy and $\neg(xSy)$. Prove that \sim is symmetric.