

# Observation of Gravitational Waves from a Binary Black Hole Merger

B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration)  
Phys. Rev. Lett. **116**, 061102 – Published 11 February 2016

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# Outline

- Background
  - Einstein Field Equations
  - LIGO/VIRGO Detector
- Results
- Result Analysis
- Citation Analysis

# Black Hole Merger



# Einstein's Field Equation Describes How The Curvature of Spacetime Affects Mass and Energy

$$R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} - g_{\mu\nu} \Lambda = \frac{8\pi G}{c^4} T_{\mu\nu}$$

The diagram shows the Einstein Field Equation with red circles around the terms  $R_{\mu\nu}$ ,  $R$ ,  $g_{\mu\nu}$ ,  $\Lambda$ , and  $T_{\mu\nu}$ . Arrows point from these terms to their respective labels: Ricci Curvature Tensor, Ricci Scalar, Metric Tensor, Cosmological Constant, and Stress-Energy-Momentum Tensor.

[1] A. Einstein, Sitzungsber. K. Preuss. Akad. Wiss. 1, 688 (1916).

## Brief Description of Tensor Terms in the Field Equations

$$R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} - g_{\mu\nu} \Lambda = \frac{8\pi G}{c^4} T_{\mu\nu}$$

### Metric Tensor

- Matrix that encodes all the information regarding distances between points within a specific manifold.
- **Example:** For Euclidean spacetime, the minkowski tensor is given.

$$\eta_{\mu\nu} = \begin{bmatrix} -c^2 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$R_{\alpha\mu\beta\nu} = R_{\beta\nu\alpha\mu}$$

$$g^{\alpha\lambda} R_{\alpha\mu\beta\nu} = g^{\alpha\lambda} R_{\beta\nu\alpha\mu}$$

$$R^{\lambda}_{\mu\beta\nu} = R^{\lambda}_{\beta\nu\mu}$$

$$R_{\mu\nu} = R_{\nu\mu}$$

$$R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} - g_{\mu\nu} \Lambda = \frac{8\pi G}{c^4} T_{\mu\nu}$$

### Ricci Curvature Tensor

- Physically, it measures how much a volume changes in curved space compared to flat space.

### Ricci Curvature Scalar

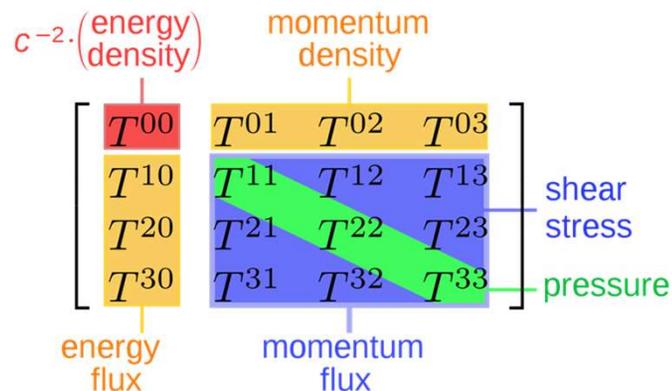
- Scalar that describes curvature.
- Contract the Ricci Tensor

$$R = g^{\mu\nu} R_{\mu\nu} = R^{\mu}_{\mu} = R$$

$$R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} - g_{\mu\nu}\Lambda = \frac{8\pi G}{c^4} T_{\mu\nu}$$

### Stress-Energy Tensor

- Describes the density and flux of energy and momentum in spacetime.

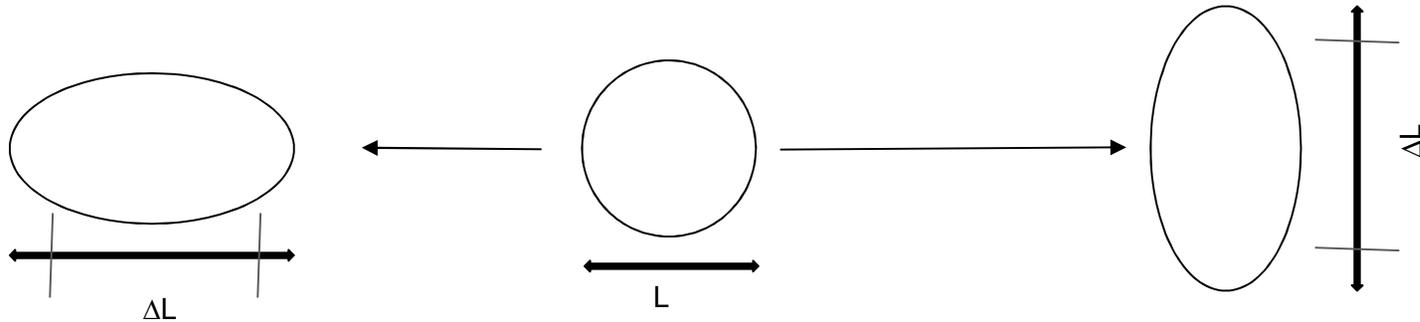


### How to get gravitational waves?

- Linearize the field equation using a minkowski-like metric.

$$g_{\mu\nu} = \eta_{\mu\nu} + \epsilon h_{\mu\nu}$$

## Gravitational Waves Stretch and Squeeze The Distance Between Objects.



- Strain is defined as the change in length over the length and it is a measure of the strength of the gravitational wave.

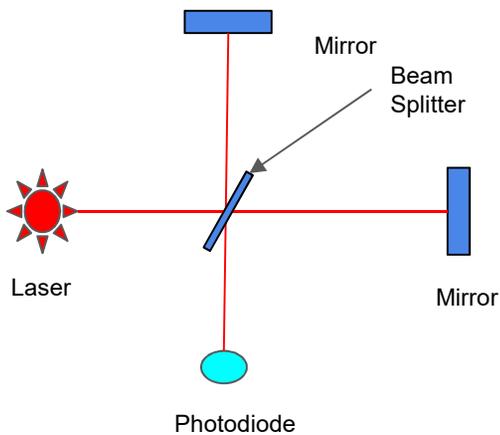
$$h(t) = \frac{\Delta L}{L}$$

- Typical strain value for astrophysical events is of the order  $10^{-21}$ .

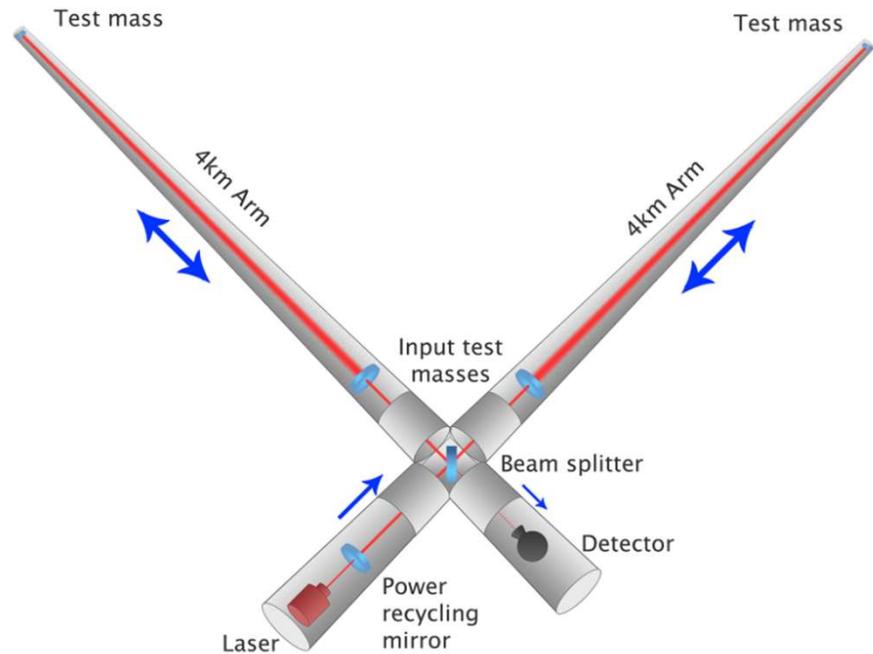
$$h \sim 10^{-21}$$

# LIGO/VIRGO Detector

Michelson Interferometer



Scale it up! →



Laser Wavelength  $\sim 1 \mu\text{m}$

# Previous Discoveries

- Theoretical predictions of gravitational waves and black holes ([1],[2])
- Indirect evidences
  - observation of binary pulsar system PSR B1913p16 by Hulse and Taylor [3].
  - Subsequent observations of energy loss[4].
- Black hole mergers had not been observed before

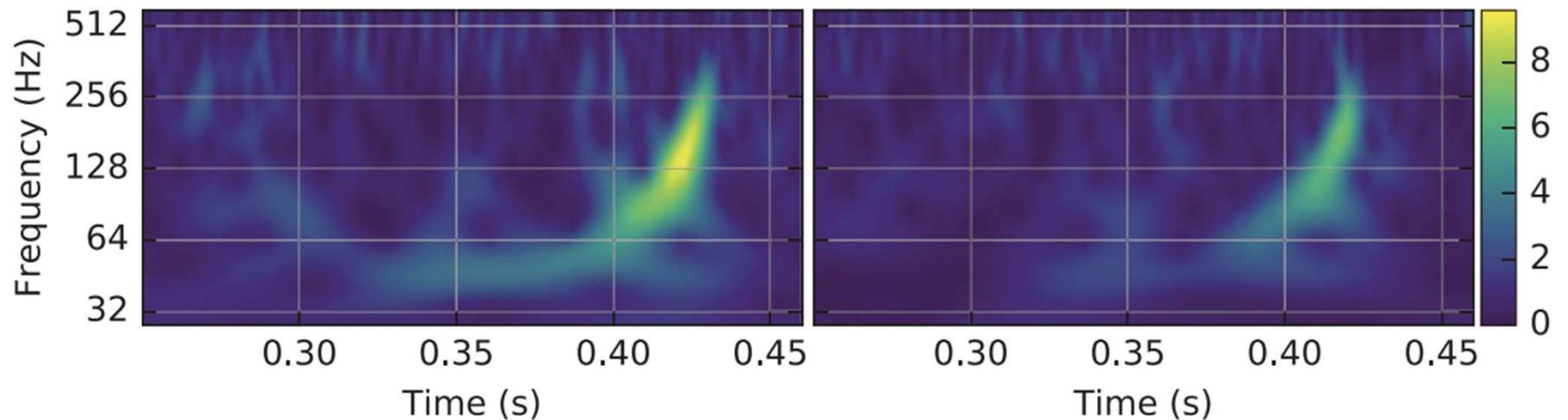
[1] A. Einstein, Sitzungsber. K. Preuss. Akad. Wiss. 1, 688 (1916).

[2] A. Einstein, Sitzungsber. K. Preuss. Akad. Wiss. 1, 154 (1918).

[3] K. Schwarzschild, Sitzungsber. K. Preuss. Akad. Wiss. 1, 189 (1916)

[4] J. H. Taylor and J. M. Weisberg, Astrophys. J. 253, 908 (1982).

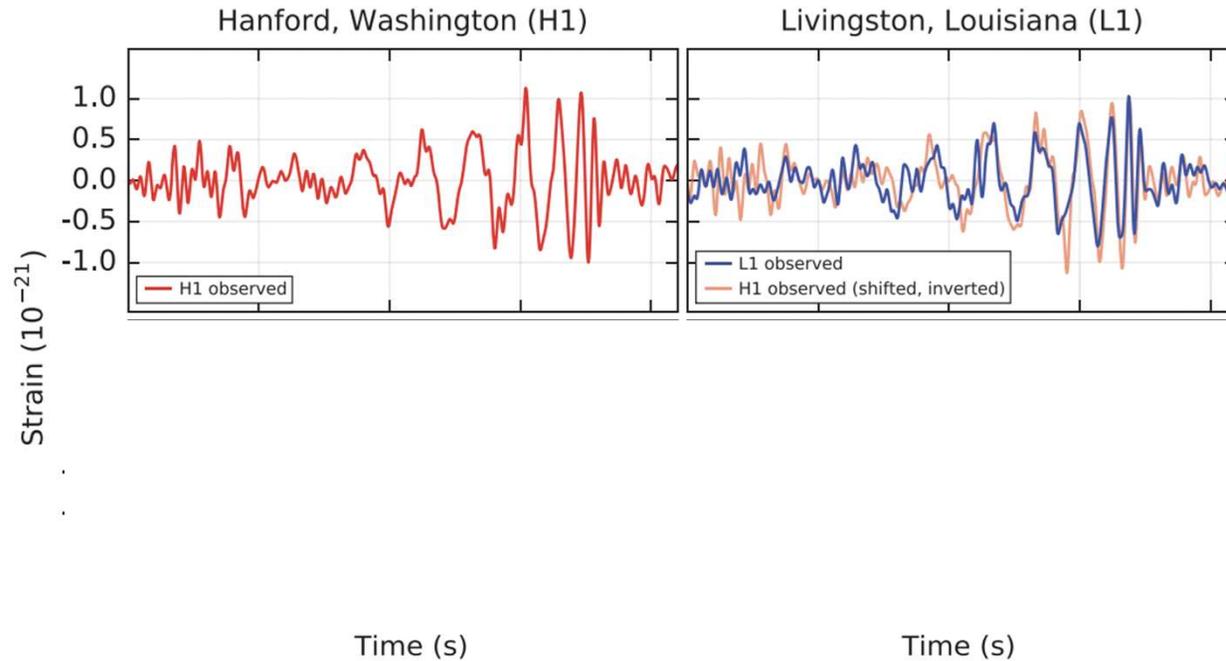
## Initial Observation of Gravitational Waves



By B. P. Abbott et al., 2016, Phys. Rev. Lett. 116.0611

- Confirms the propagation speed of gravitational waves - speed of light
- Only run through a digital filter - very minimal
- Both frequency and amplitude increase - chirp signal of two compact objects and then ring down to a final object at the end

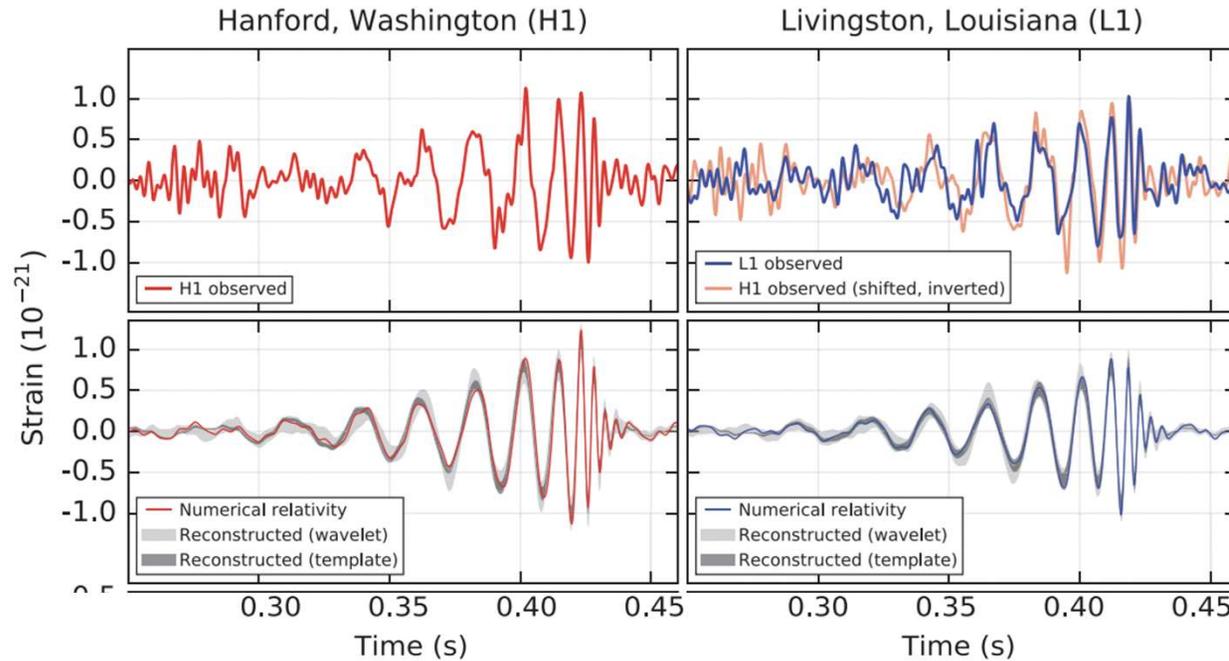
# Processing and Validation of Signal GW150914



By B. P. Abbott et al., 2016, Phys. Rev. Lett. 116.061102

- Coincident chirp inspiral merger ring down signal.
- Second row: Gravitational-wave strain projected onto each detector in the 35–350 Hz band.

# Processing and Validation of Signal GW150914



By B. P. Abbott et al., 2016, Phys. Rev. Lett. 116.061102

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## What does the signal tell us?

- Over 2 secs, frequency increases in 8 cycles from 35 Hz to 150 HZ.
- Then we can measure Chirp mass from  $f$ , observed frequency, and its time derivative

$$\mathcal{M} = \frac{(m_1 m_2)^{3/5}}{(m_1 + m_2)^{1/5}} = \frac{c^3}{G} \left[ \frac{5}{96} \pi^{-8/3} f^{-11/3} \dot{f} \right]^{3/5}$$

- Chirp mass  $M \simeq 30M_\odot$ , Total mass  $\gtrsim 70M_\odot$
- To obtain an orbital frequency of 75 Hz, the two objects must be very close and compact
- Only black holes compact enough to reach this frequency

# Analysis Overview

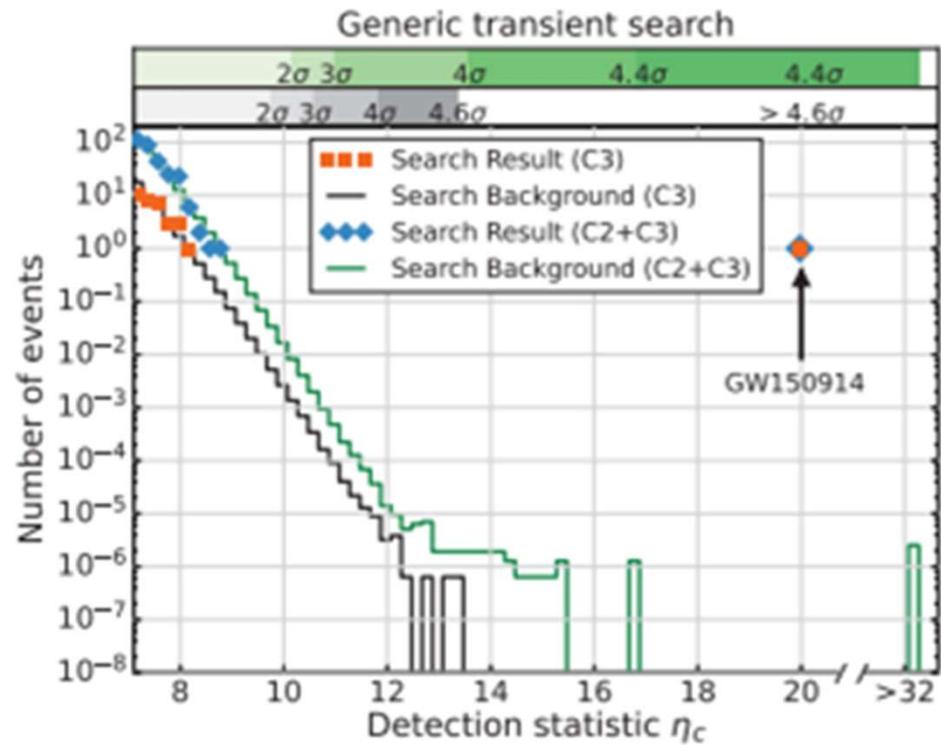
- Two different searches
  - Generic transient search
  - Binary coalescence search
  
- 16 days of data
  - September 12 to October 20, 2015
  - GW150914
  
- Background is estimated
  - Time-shifted data for each method
  - Determines likelihood of event

# Generic Transient Search

- No waveform model is used to compare events
- Excess power
  - Time frequency data of the detector strain data
  - $\eta_c = \sqrt{2E_c/(1 + E_n/E_c)}$  where  $E_c$  = cross-correlation and  $E_n$  = residual noise
- Morphology of data is used to class possible events
  - C1: Known events with morphology of noise transients
  - C2: Remaining events
  - C3: Events with increasing frequency

# Generic Transient Search Results GW150914

- $\eta_c = 20$
- $4.6 \sigma$
- Search was between C1 and a combined (C2 and C3)

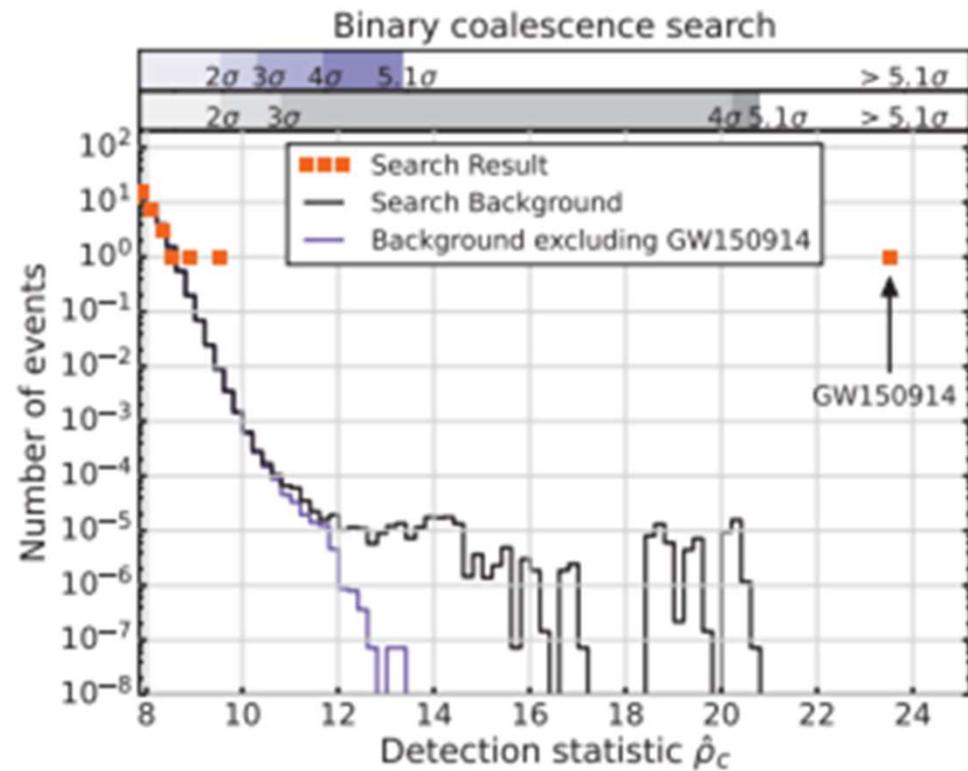


## Binary Coalescence Search

- Model of systems used
- Signal to noise ratio for each model  $p(t)$ 
  - Compared using a  $\chi^2$  statistic
  - Compares events pairs in a 15ms range

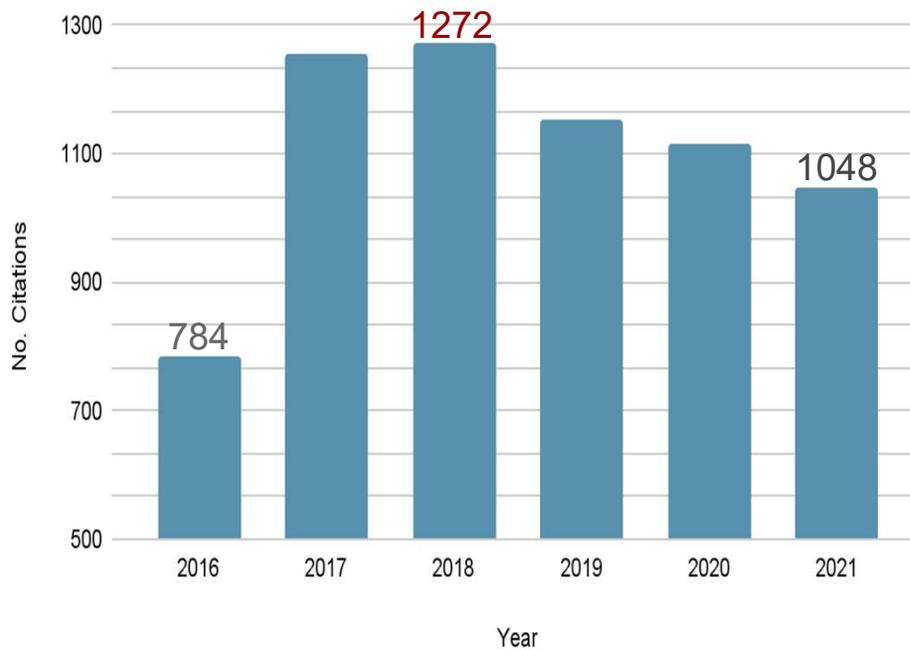
# Binary Coalescence Results GW150914

- $5.1\sigma$
- Signal to noise ratio  
 $P_c = 23.6$



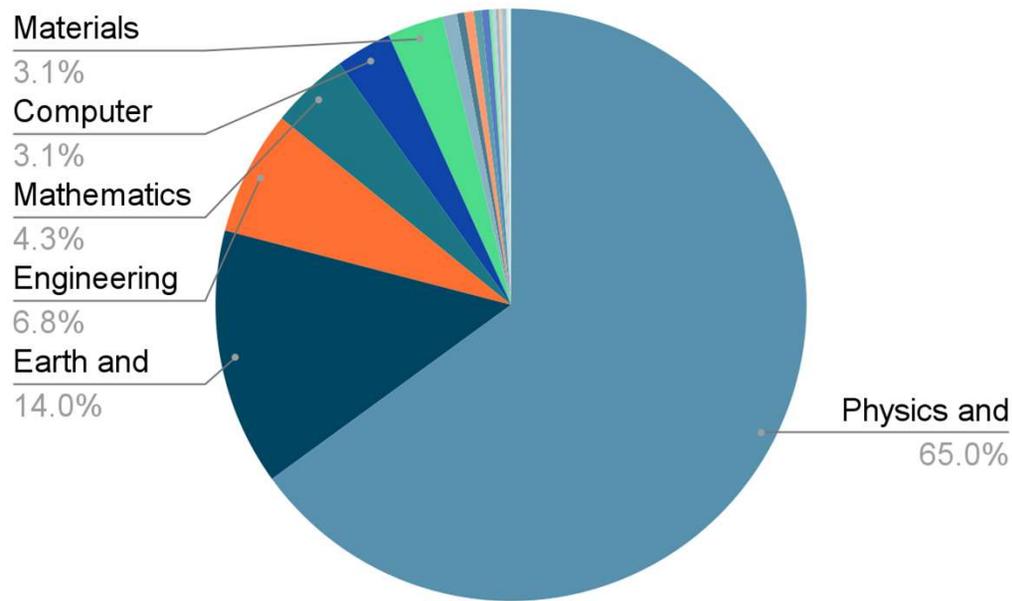
# Citation Analysis

Citations per Year since Publication



- As of 11/25/2021, Cited by 6629 documents since publication in 2016
- Least cited in 2016, 784 times
- Cited most in 2018, 1272 times
- This year (2021), cited 1048 times

# Categories of Works that Cited



- A vast majority of documents that cite this paper are STEM related (~99%)
- ~0.45% are Arts and Humanities and Social Sciences

● Physics and Astronomy ● Earth and Planetary Sciences  
● Engineering ● Mathematics ● Computer Science  
● Materials Science ● Chemistry ● Social Sciences 15 more

\*NOTE: this pie chart doesn't account for genre overlap

# Impact in Astrophysics

Document title	Authors	Year	Source
GW170817: Observation of <u>Gravitational Waves</u> from a Binary <u>Neutron Star</u> Inspiral <i>Open Access</i>	Abbott, B.P., Abbott, R., Abbott, T.D., (...), Zucker, M.E., Zweizig, J.	2017	Physical Review Letters 119(16),161101

- Observation of gravitational waves on 08/17/2017 from Binary Neutron Star Merger
- Used an additional detector (Fermi-GBM) to record Gamma burst data  
-> Neutron Star
- Were able to locate the sky region of the event with a 90% probability!

DOI: <https://doi.org/10.1103/PhysRevLett.119.161101>

# Impact in Particle Physics

Document title	Authors	Year	Source
Primordial black holes as a <u>dark matter candidate</u> <i>Open Access</i>	Green, A.M., Kavanagh, B.J.	2021	Journal of Physics G: Nuclear and Particle Physics 48(4),043001

- What if dark matter was just less-massive black holes formed just after the Big Bang?
  - Primordial black hole, PBH
- This paper goes into detail on current criteria for PBHs to be a dark matter candidate
- Proposition that the black holes involved in GW150914 merger were PBH
- Merging rate of the black holes consistent with scenario of all dark matter being made of PBHs

DOI: [10.1088/1361-6471/abc534](https://doi.org/10.1088/1361-6471/abc534)

# Impact in Biomedical Engineering

Document title	Authors	Year	Source
Stimulation of <u>3D osteogenesis</u> by mesenchymal stem cells using a nanovibrational bioreactor <i>Open Access</i>	Tsimbouri, P.M., Childs, P.G., Pemberton, G.D., (...), Reid, S., Dalby, M.J.	2017	Nature Biomedical Engineering 1(9), pp. 758-770

- Aim is to develop a way to grow bones in 3D that can be used in grafting procedures
- Similar laser interferometry techniques were used to measure the vibrational amplitude in their bioreactor!

DOI: [10.1038/s41551-017-0127-4](https://doi.org/10.1038/s41551-017-0127-4)

## Citation Analysis, Summary

- Important enough to be included in review papers
- Techniques described in the paper have use outside the field of physics
- Within the Physics community, has inspired scientists to take more and better data of gravitational waves
  - increase in number of detectors, detector quality, analysis techniques
- Has introduced new questions into the fields of astrophysics and particle physics

Thank you!

