

Physic 102 formula sheet (FA2016)

**Kinematics and mechanics**

$$x = x_0 + v_0 t + \frac{1}{2} a t^2 \quad v = v_0 + a t \quad v^2 = v_0^2 + 2a \Delta x$$

$$F = m a \quad a_c = \frac{v^2}{r}$$

$$E_{\text{tot}} = K + U \quad K = \frac{1}{2} m v^2 = \frac{p^2}{2m} \quad p = m v \quad W_F = F d \cos \theta \quad P = F v \cos \theta$$

**Electrostatics**

$$F_{12} = k \frac{q_1 q_2}{r^2} \quad E = \frac{F}{q_0} \quad U_{12} = k \frac{q_1 q_2}{r} \quad V \equiv \frac{U}{q_0} \quad W_E = -\Delta U = -W_{\text{you}}$$

$$\text{Point charge} \quad E = k \frac{q}{r^2} \quad V = k \frac{q}{r}$$

$$\text{Electric dipole} \quad p = q d \quad \tau_{\text{dip}} = p E \sin \theta \quad U_{\text{dip}} = -p E \cos \theta$$

**Resistance**

$$R = \frac{V}{I} \quad I = \frac{\Delta q}{\Delta t} \quad \text{Physical resistance: } R = \rho \frac{L}{A}$$

$$P = I V = I^2 R = \frac{V^2}{R} \quad R_S = R_1 + R_2 + \dots \quad \frac{1}{R_P} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$$

**Capacitance**

$$C = \frac{Q}{V} \quad \text{Parallel plate capacitor: } C = \frac{\kappa \epsilon_0 A}{d} \quad E = \frac{Q}{\epsilon_0 A} \quad V = E d$$

$$U_C = \frac{1}{2} Q V = \frac{1}{2} C V^2 = \frac{1}{2} \frac{Q^2}{C} \quad C_P = C_1 + C_2 + \dots \quad \frac{1}{C_S} = \frac{1}{C_1} + \frac{1}{C_2} + \dots$$

**Circuits**

$$\sum \Delta V = 0 \quad \sum I_{\text{in}} = \sum I_{\text{out}}$$

$$q(t) = q_{\infty} (1 - e^{-t/\tau}) \quad q(t) = q_0 e^{-t/\tau} \quad I(t) = I_0 e^{-t/\tau} \quad \tau = RC$$

**Magnetism**

$$F = q v B \sin \theta \quad r = \frac{m v}{q B} \quad F_{\text{wire}} = I L B \sin \theta \quad \tau_{\text{loop}} = N I A B \sin \varphi$$

$$\text{Magnetic dipole: } \mu = N I A \quad \tau_{\text{dip}} = \mu B \sin \varphi \quad U_{\text{dip}} = -\mu B \cos \varphi$$

$$B_{\text{wire}} = \frac{\mu_0 I}{2 \pi r} \quad B_{\text{sol}} = \mu_0 n I$$

**Electromagnetic induction**

$$\mathcal{E} = -N \frac{\Delta \Phi}{\Delta t} \quad \Phi = B A \cos \varphi$$

$$|\mathcal{E}_{\text{bar}}| = B L v \quad \mathcal{E}_{\text{gen}} = \mathcal{E}_{\text{max}} \sin \omega t = \omega N A B \sin \omega t \quad \omega = 2 \pi f$$

$$V_{\text{rms}} = \frac{V_{\text{max}}}{\sqrt{2}} \quad I_{\text{rms}} = \frac{I_{\text{max}}}{\sqrt{2}} \quad \frac{V_p}{V_s} = \frac{I_s}{I_p} = \frac{N_p}{N_s}$$

**Electromagnetic waves**

$$\lambda = \frac{c}{f} \quad E = c B$$

$$u_E = \frac{1}{2} \epsilon_0 E^2 \quad u_B = \frac{1}{2 \mu_0} B^2 \quad \bar{u} = \frac{1}{2} \epsilon_0 E_{\text{rms}}^2 + \frac{1}{2 \mu_0} B_{\text{rms}}^2 = \epsilon_0 E_{\text{rms}}^2 = \frac{B_{\text{rms}}^2}{\mu_0} \quad S = I = \bar{u} c = \frac{P}{A}$$

$$f_0 = f_e \sqrt{\frac{1 + v_{\text{rel}}/c}{1 - v_{\text{rel}}/c}} \approx f_e \left( 1 + \frac{v_{\text{rel}}}{c} \right) \quad I = I_0 \cos^2 \theta$$

### Reflection and refraction

$$\theta_r = \theta_i \quad \frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f} \quad f = \pm \frac{R}{2} \quad m = \frac{h_i}{h_o} = -\frac{d_i}{d_o}$$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2 \quad v = \frac{c}{n} \quad \sin \theta_c = \frac{n_2}{n_1} \quad M = \frac{\theta'}{\theta} \approx \frac{d_{\text{near}}}{f}$$

$$\text{Compound microscope: } m_{\text{obj}} = \frac{L_{\text{tube}}}{f_{\text{obj}}} \quad M_{\text{eye}} = \frac{d_{\text{near}}}{f_{\text{eye}}} \quad M_{\text{tot}} = M_{\text{eye}} m_{\text{obj}}$$

### Interference and diffraction

$$\text{Double-slit interference: } d \sin \theta = m\lambda \quad d \sin \theta = \left(m + \frac{1}{2}\right)\lambda \quad m = 0, \pm 1, \pm 2, \dots$$

$$\text{Single-slit diffraction: } a \sin \theta = m\lambda \quad m = 0, \pm 1, \pm 2, \dots$$

$$\text{Circular aperture: } D \sin \theta \approx 1.22\lambda$$

### Quantum mechanics

$$E = hf = \frac{hc}{\lambda} \quad \lambda = \frac{h}{p} \quad \Delta p_x \Delta x \geq \frac{\hbar}{2} \quad \hbar = \frac{h}{2\pi}$$

$$\text{Bohr atom: } 2\pi r_n = n\lambda \quad n = 1, 2, 3, \dots \quad L_n = m_e v_n r_n = n\hbar$$

$$r_n = \left(\frac{\hbar^2}{m_e k e^2}\right) \frac{n^2}{Z} \approx (5.29 \times 10^{-11} \text{ m}) \frac{n^2}{Z} \quad E_n = -\left(\frac{m_e k^2 e^4}{2\hbar^2}\right) \frac{Z^2}{n^2} \approx -(13.6 \text{ eV}) \frac{Z^2}{n^2}$$

$$\frac{1}{\lambda} \approx (1.097 \times 10^7 \text{ m}^{-1}) Z^2 \left(\frac{1}{n_f^2} - \frac{1}{n_i^2}\right)$$

$$\text{Quantum atom: } L = \sqrt{\ell(\ell+1)}\hbar \quad L_z = m_\ell \hbar \quad S_z = m_s \hbar$$

$$\text{Atomic magnetism: } \mu_{e,z} = -\frac{e}{2m_e} L_z \quad \mu_{s,z} = -\frac{g e}{2m_e} S_z, \quad g \approx 2 \quad \mu_B \equiv \frac{e\hbar}{2m_e} \approx 5.8 \times 10^{-5} \text{ eV/T}$$

### Nuclear physics and radioactive decay

$$A = Z + N \quad r \approx (1.2 \times 10^{-15} \text{ m}) A^{1/3} \quad E_0 = mc^2$$

$$m_{\text{nucleus}} = Zm_{\text{proton}} + Nm_{\text{neutron}} - \frac{|E_{\text{bind}}|}{c^2}$$

$$\frac{\Delta N}{\Delta t} = -\lambda N \quad N(t) = N_0 e^{-\lambda t} = N_0 2^{-t/T_{1/2}} \quad T_{1/2} = \frac{\ln 2}{\lambda} \approx \frac{0.693}{\lambda}$$

### Constants and unit conversion

$$g = 9.8 \text{ m/s}^2 \quad e = 1.60 \times 10^{-19} \text{ C}$$

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{Nm}^2 \quad k \equiv \frac{1}{4\pi\epsilon_0} = 8.99 \times 10^9 \text{ Nm}^2/\text{C}^2 \quad \mu_0 = 4\pi \times 10^{-7} \text{ T} \cdot \text{m/A}$$

$$c = \frac{1}{\sqrt{\epsilon_0 \mu_0}} = 3 \times 10^8 \text{ m/s} \quad h = 6.626 \times 10^{-34} \text{ J} \cdot \text{s} \quad hc = 1240 \text{ eV} \cdot \text{nm}$$

$$1 \text{ eV} = 1.60 \times 10^{-19} \text{ J} \quad m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg} = 511 \text{ keV}/c^2$$

$$m_{\text{proton}} = 1.673 \times 10^{-27} \text{ kg} = 938 \text{ MeV}/c^2 \quad m_{\text{neutron}} = 1.675 \times 10^{-27} \text{ kg} = 939.5 \text{ MeV}/c^2$$

### SI Prefixes

Power	Prefix	Symbol
10 <sup>9</sup>	giga	G
10 <sup>6</sup>	mega	M
10 <sup>3</sup>	kilo	k
10 <sup>0</sup>	—	—
10 <sup>-3</sup>	milli	m
10 <sup>-6</sup>	micro	μ
10 <sup>-9</sup>	nano	n
10 <sup>-12</sup>	pico	p