

# ECE 537 Fundamentals of Speech Processing

## Problem Set 4

UNIVERSITY OF ILLINOIS  
Department of Electrical and Computer Engineering

Assigned: Friday, 9/30/2022; Due: Monday, 10/3/2022  
Reading: Velichko & Zagoruyko, “Automatic Recognition of 200 Words,” 1970

- The five bandpass filters used by Velichko & Zagoruyko have relatively wide bandwidth, compared to the use of a spectrum based on the fast Fourier transform. It turns out that Euclidean distance between spectra is only reasonable if the filters have relatively wide bandwidth. This problem will explore the reasons.

Suppose that you have two utterances of the same vowel,  $s_1[n]$  and  $s_2[n]$ . Suppose that both  $s_1[n]$  and  $s_2[n]$  are examples of the same vowel, with Dudley vocoder amplitudes of  $A_1 = 1$ ,  $A_2 = 10$ ,  $A_3 = 2$ ,  $A_4 = 2$ ,  $A_5 = 0$ ,  $A_6 = 3$ ,  $A_7 = 3$ , and no energy above 2100Hz (remember that, in a Dudley vocoder, spectral amplitude  $A_\ell$  scales frequency components in the range  $300(\ell - 1) < f < 300\ell$ ). The difference between them is that  $s_1[n]$  has a pitch period of  $N_1$  samples, while  $s_2[n]$  has a pitch period of  $N_2$  samples.

- (1 point) Assume an analysis window of length  $N$  samples, where  $N$  is the least common multiple of  $N_1$  and  $N_2$ , and the discrete Fourier transform (DFT) is

$$S_i[k] = \sum_{n=0}^{N-1} s_i[n] e^{-j \frac{2\pi kn}{N}}$$

Assume that the integers  $\frac{N}{N_1}$  and  $\frac{N}{N_2}$  have no common multiple, i.e., none of the harmonics of  $X_1[k]$  are in the same DFT bin as any harmonic of  $X_2[k]$ . Define the following normalized spectra:

$$F_1[k] = \frac{|S_1[k]|}{\sqrt{\sum_{k'=0}^{N-1} |S_1[k']|^2}}, \quad F_2[k] = \frac{|S_2[k]|}{\sqrt{\sum_{k'=0}^{N-1} |S_2[k']|^2}}$$

What is the Euclidean distance between these two normalized spectra? Is this a large number or a small number?

- (1 point) Now, instead of using a DFT, use the spectral energy features defined by Velichko & Zagoruyko. In order to make the calculation easier, assume that  $s_1[n]$  and  $s_2[n]$  each has the same fraction of its harmonics within each of the five V& Z sub-bands. Find  $\rho$ , the Euclidean distance between their log sub-band energies.
- Suppose that you have a word that is two frames long, and a word that is three frames long. The spectral similarities  $a_{i,k}$  are as shown in the following table, where  $i$  is the row index and  $k$  is the column index:

$a_{i,k}$	1	2	3
1	0.484	0.153	0.464
2	0.405	0.624	0.146

What is the best alignment, and what is the average spectral similarity computed along the best alignment?