

$$P(X = \text{comp} + w_n) = b$$

$$= P(X = \text{comp}, R=1) + P(X = \text{comp}, R=0)$$

$$b = ap + (1-a) \frac{1}{m}$$

$$p = \frac{b - (1-a)/m}{a}$$

## 9 OPTIMIZATION

$$W = [w_0, \dots, w_{m-1}] \quad w_i \in \{0, \dots, n-1\}$$

### a) Exhaustive search

$m$  coefficients, each has  $n$  values

$\Rightarrow n^m$  possible  $w$  vectors

$$\Rightarrow \mathcal{O}\{n^m\}$$

### b) Coordinate search w/ random restarts

For each restart:

generate a random starting  $w$

for each iteration:

for each coordinate  $0 \leq i \leq m-1$ :

- find best possible value,  $\hat{w}_i$ , of  $w_i$ ,  
under condition that  $w_j$  fixed.

$$\text{Record } \mathcal{L}_i = \mathcal{L}(w_0, \dots, w_i, \hat{w}_i, w_{i+1}, \dots, w_{m-1})$$

Find  $i^* = \arg \min \mathcal{L}_i$

$$W \leftarrow [w_0, \dots, w_{i^*-1}, \hat{w}_{i^*}, w_{i^*+1}, \dots, w_{m-1}]$$

Restarts:  $p$

Iterations:  $q$

Coordinates:  $m$

Values:  $n$

Total complexity:  $\underline{pqmn}$   $\mathcal{O}\{pqmn\}$

Question: How large does  $p$  have to be

to make

$$\mathcal{O}\{pqmn\} = \mathcal{O}\{n^m\}$$

$$p = \frac{n^m}{qmn} = \frac{n^{m-1}}{qm}$$