

# Introduction to Lighting and Rendering

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# Creating realistic contents is CRUCIAL

**MAY CONTAIN CONTENT  
INAPPROPRIATE FOR CHILDREN**

Visit [esrb.org](https://www.esrb.org) for  
rating information



Video game



AR/VR

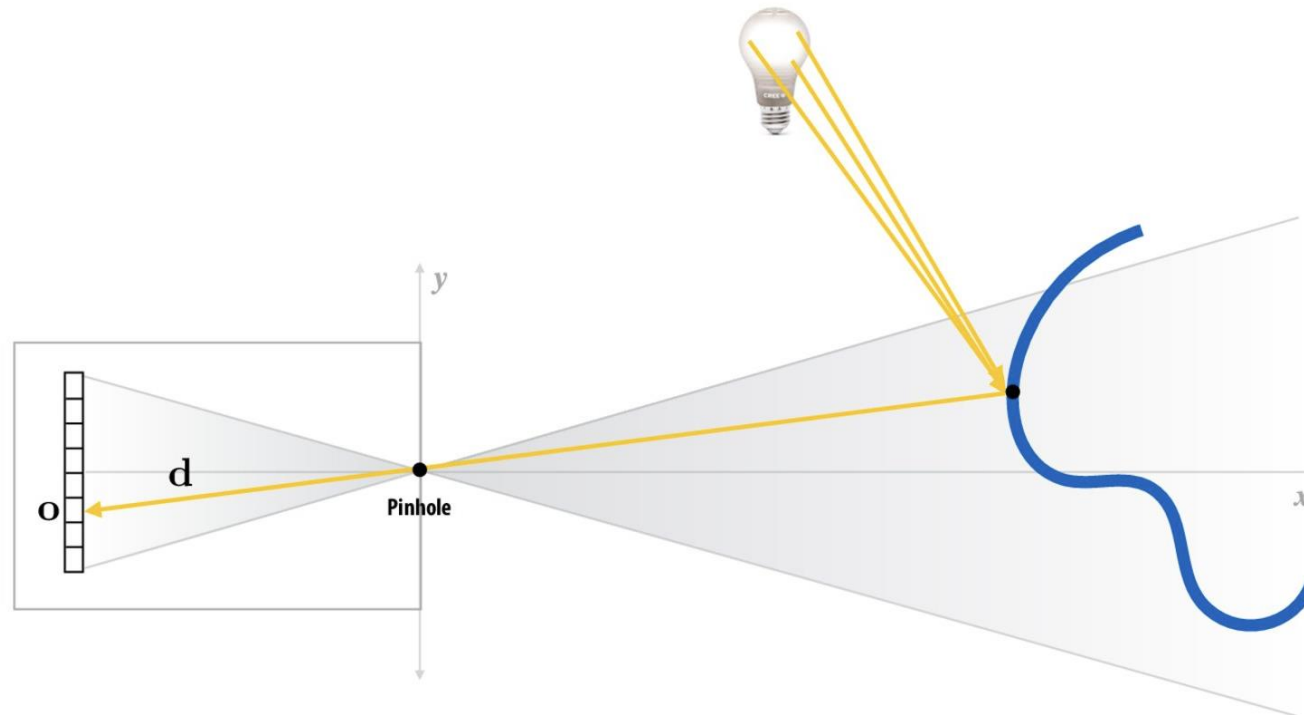


Self-driving  
simulation

<https://www.youtube.com/watch?v=inQelDKULOQ>  
<https://www.youtube.com/watch?v=IY4x85zqoJM>  
<https://www.youtube.com/watch?v=-L9VuPpzVdQ>

# We are going to talk about ...

- What are the basic components of rendering process?
- How to render an image?
- What is inverse rendering? Why is it challenging?



# How to render 2D from 3D?



3D scene

2D images/videos

# Geometry

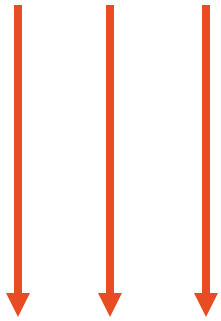
In rendering pipeline, the geometry is usually represented as meshes



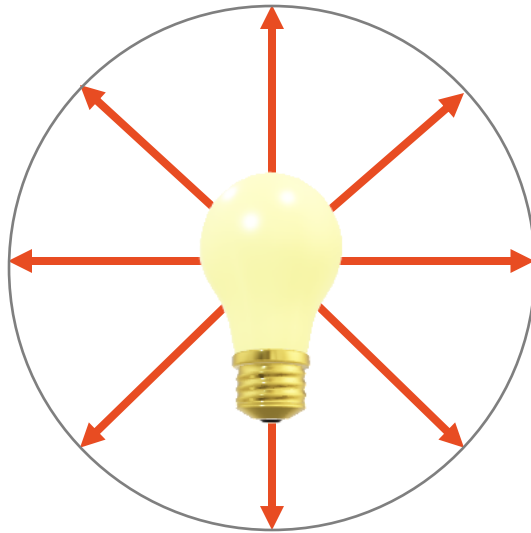
FlexiCubes (ToG, SIGGRAPH 2023)

What papers did we discuss for geometry reconstruction/generation?

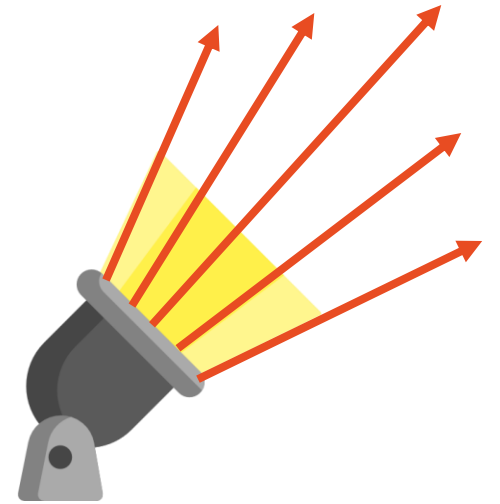
# Light sources



Directional light



Point light

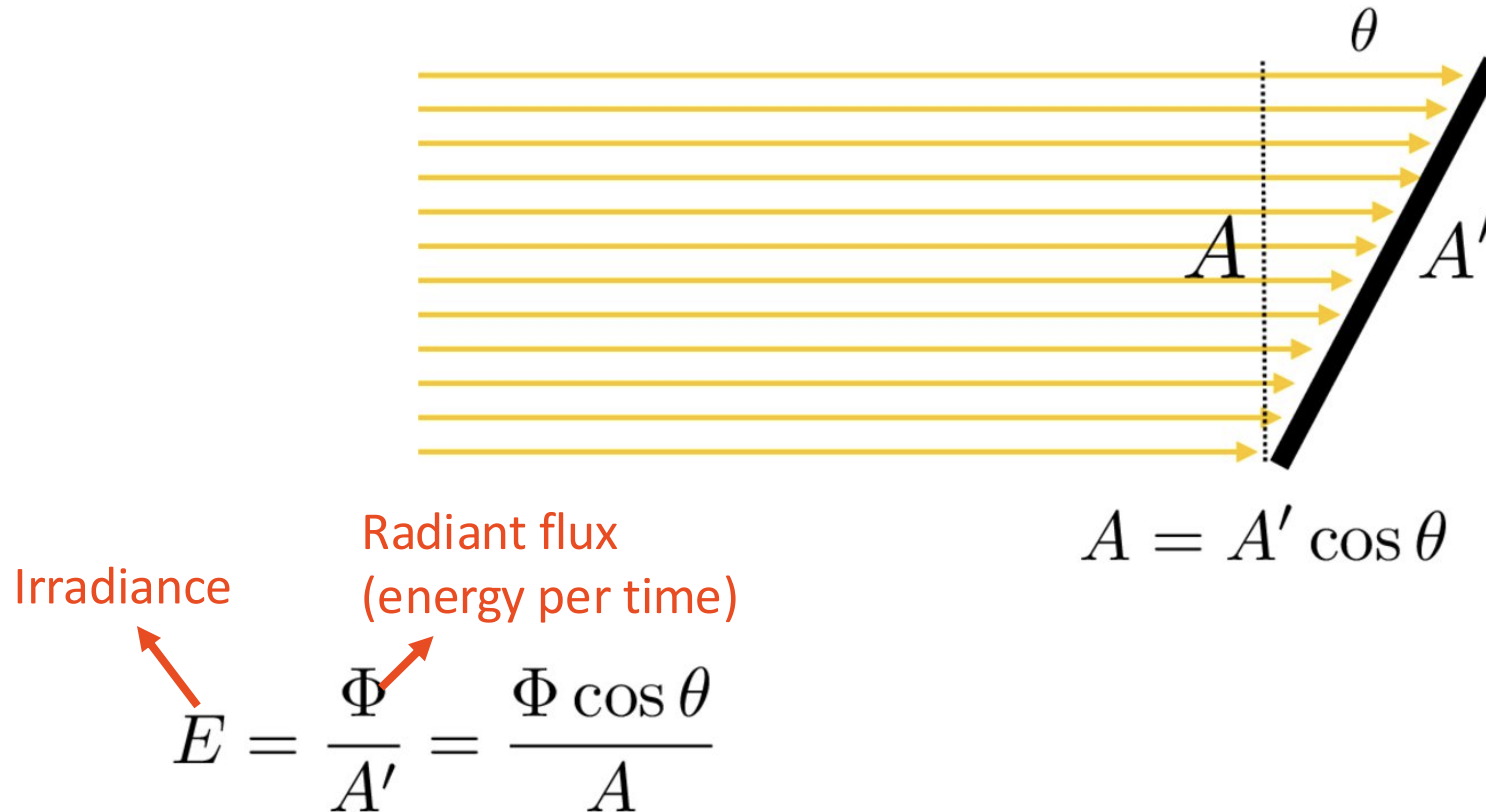


Spotlight

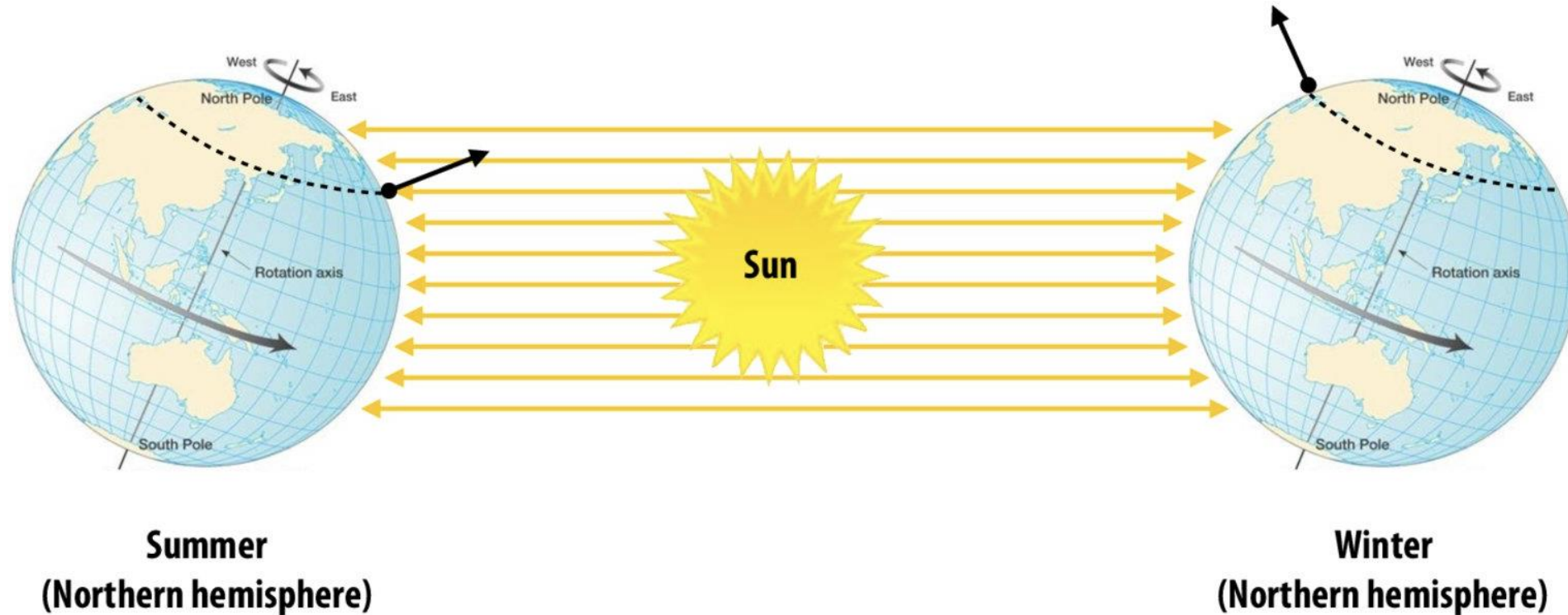
# Light direction

## Lambert's Law

Light intensity at surface is proportional to cosine of angle between light direction and surface normal



# Why do we have seasons?



**Earth's axis of rotation:  $\sim 23.5^\circ$  off axis**



# Material

**Materials: diffuse**



**Materials: gold**



**Materials: mirror**



**Materials: Ford mystic lacquer paint**



**Materials: red semi-gloss paint**



**Materials: plastic**



# Some basic reflection functions

- **Ideal specular**  
Perfect mirror



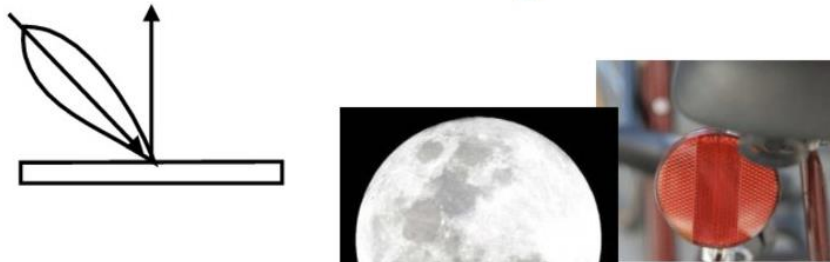
- **Ideal diffuse**  
Uniform reflection in all directions



- **Glossy specular**  
Majority of light distributed in reflection direction



- **Retro-reflective**  
Reflects light back toward source



# BRDF

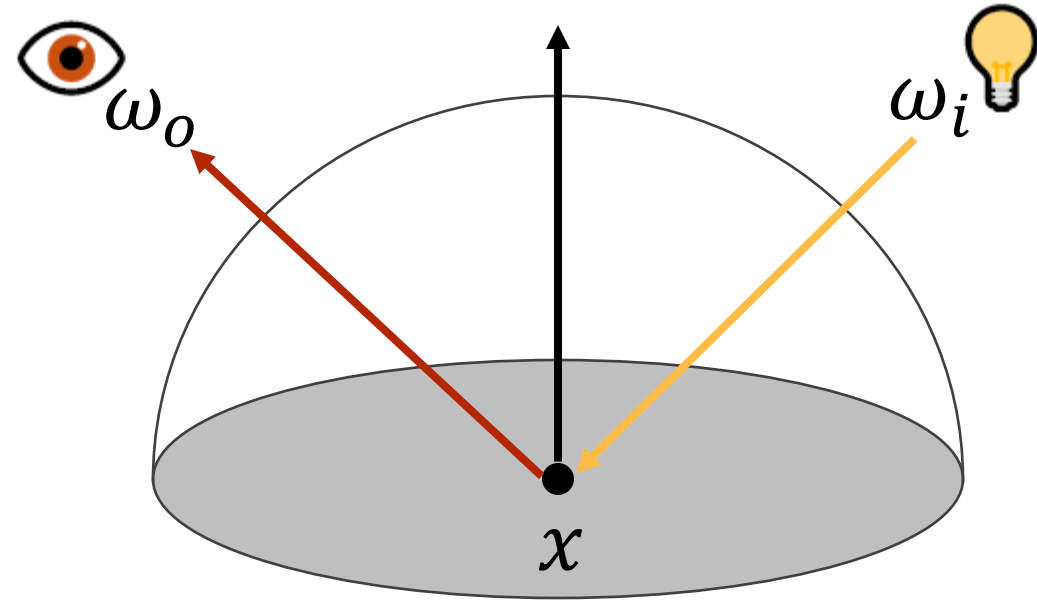
## Bidirectional Reflectance Distribution Function

Encodes behavior of light that **bounces off** surface

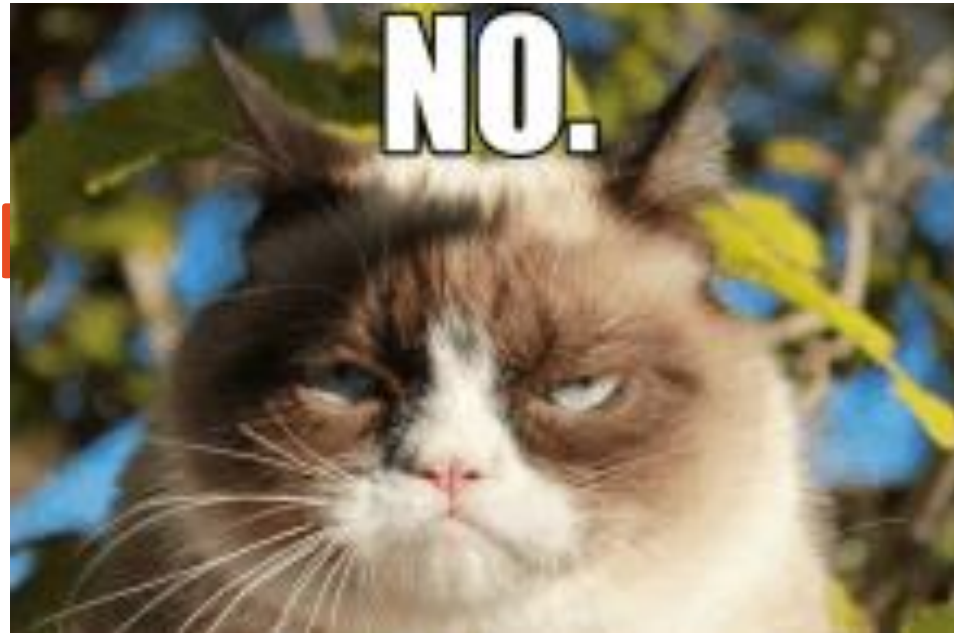
$$f(\omega_i, \omega_o) = \frac{L_o(\omega_o)}{L_i(\omega_i)}$$
$$= \frac{\text{Outgoing light in direction } \omega_o}{\text{Incoming light in direction } \omega_i}$$

Helmholtz reciprocity:  $f(\omega_1, \omega_2) = f(\omega_2, \omega_1)$

$$f(\omega_i, \omega_o) \geq 0$$



Can BRD be associated with these behaviors?



# More light & material behaviors

In addition to reflecting off surfaces, light may be transmitted through surfaces

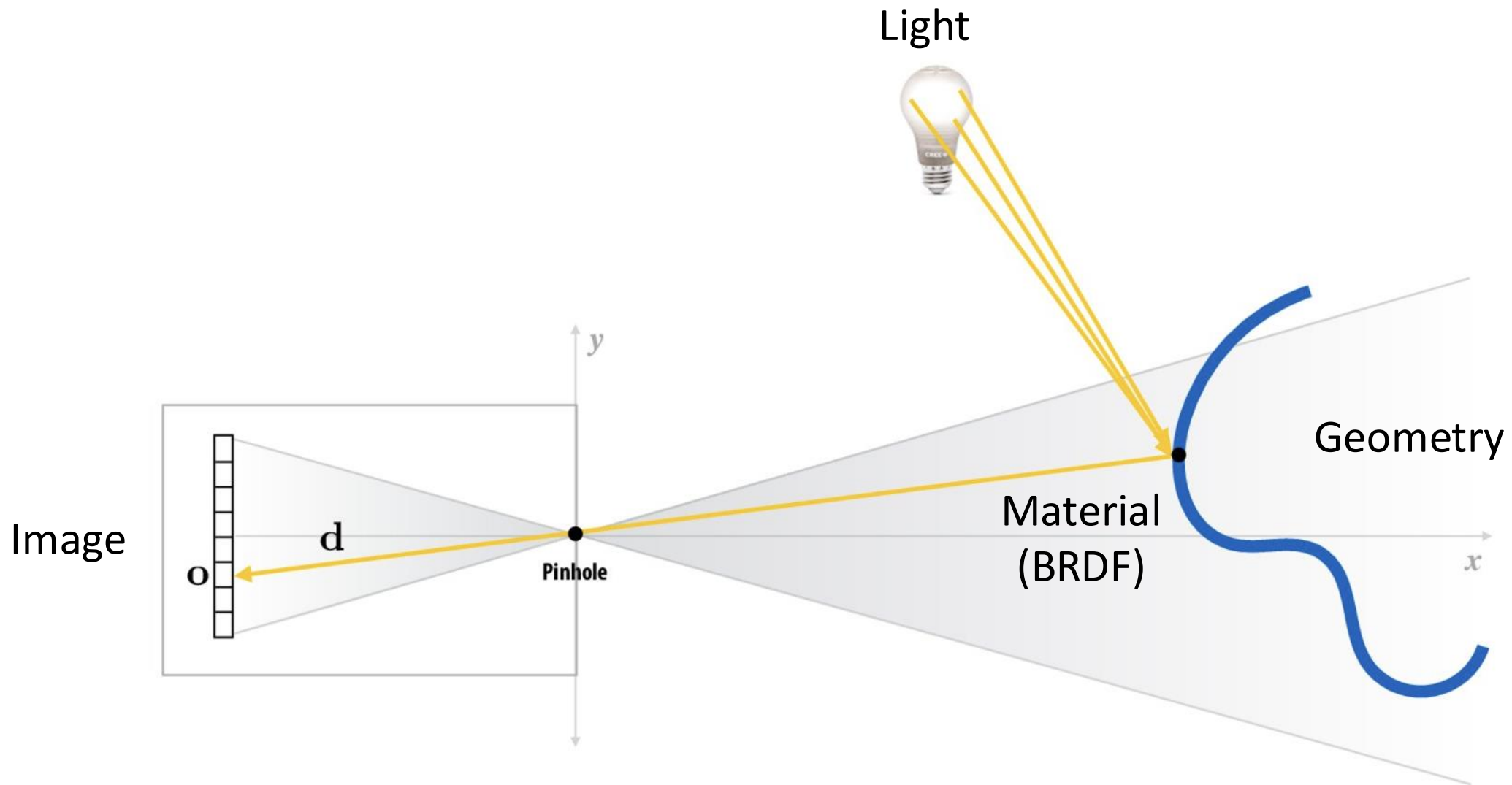
We didn't cover:

- Refraction
- Fresnel reflection
- Subsurface scattering
  
- BSDF



[Donner et al 2008]

# How to render a pixel?

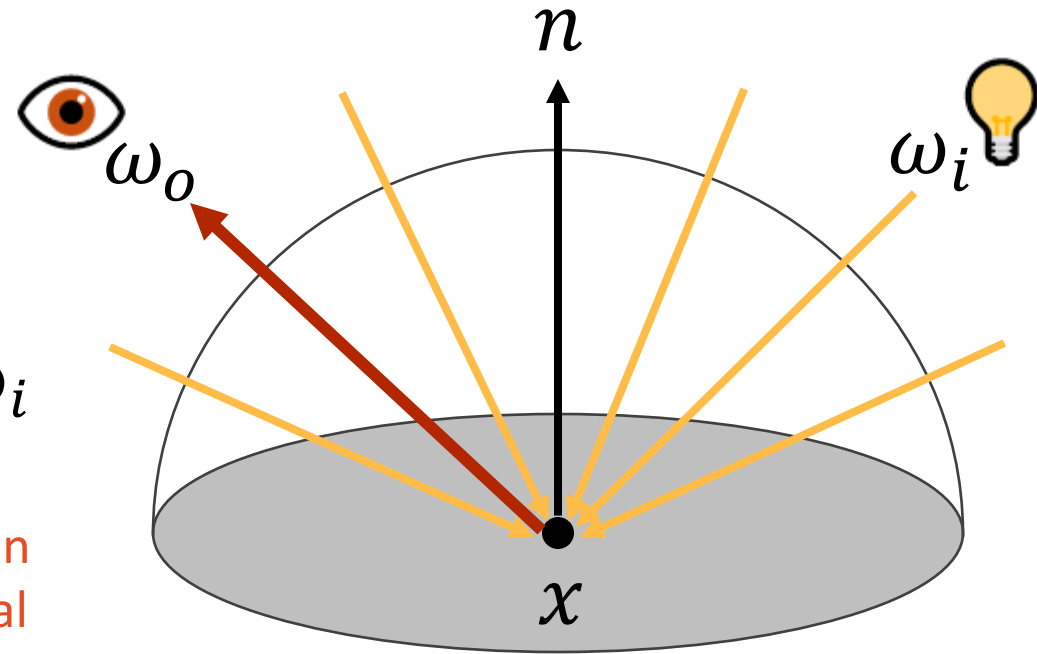


# Rendering equation

Observed radiance  $L_o(x, \omega_o)$  = Emitted radiance  $L_e(x, \omega_o)$  +

$$\int_{\Omega} f(x, \omega_i, \omega_o) L_i(x, \omega_i) (\omega_i \cdot n) d\omega_i$$

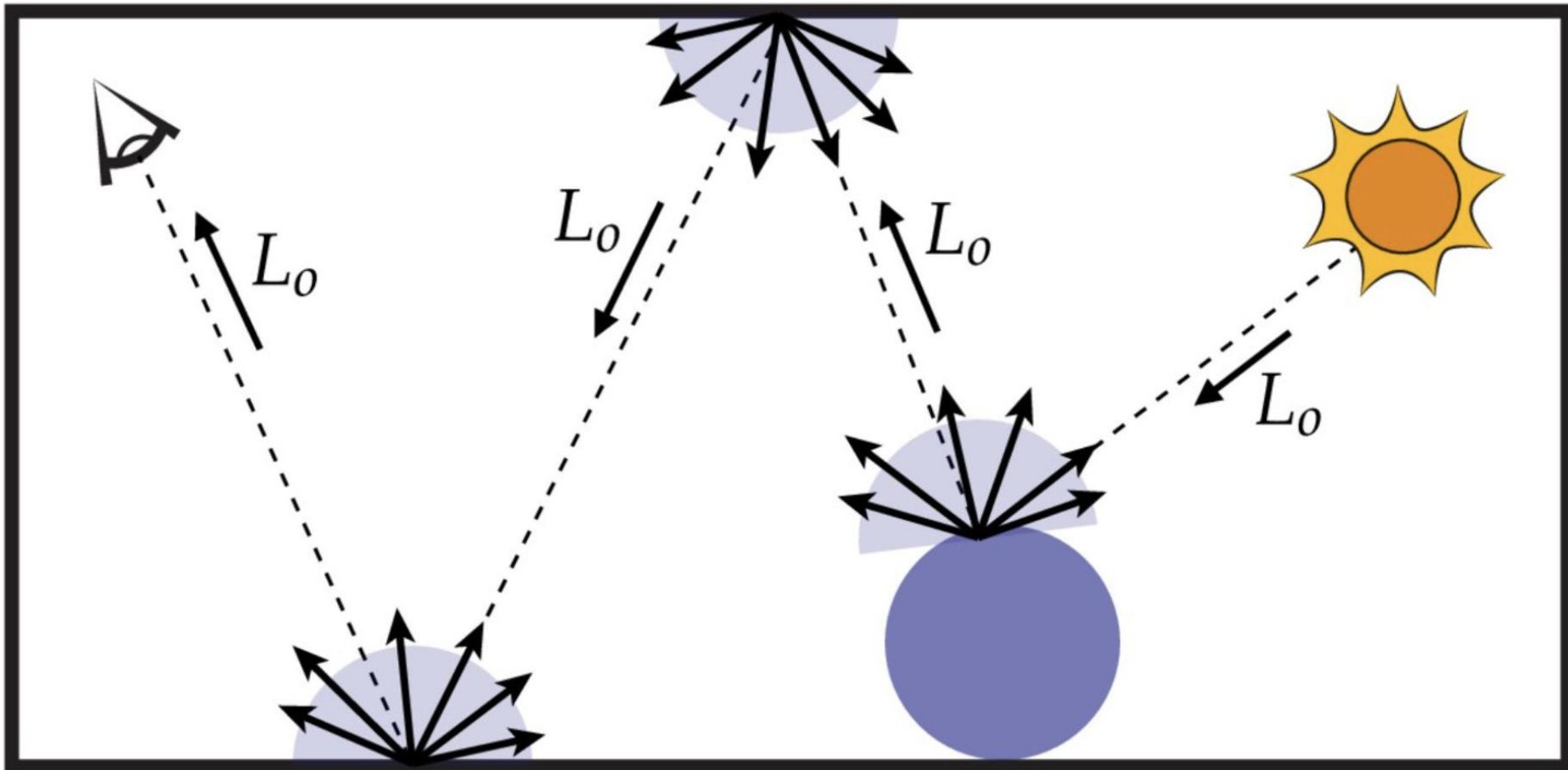
Scattering function (e.g. BRDF)      Incoming radiance  $L_i(x, \omega_i)$       Angle between Light & normal  $(\omega_i \cdot n)$



Rendering equation is recursive!

# Ray Tracing

- Basic strategy: trace the ray from sensors to light sources!

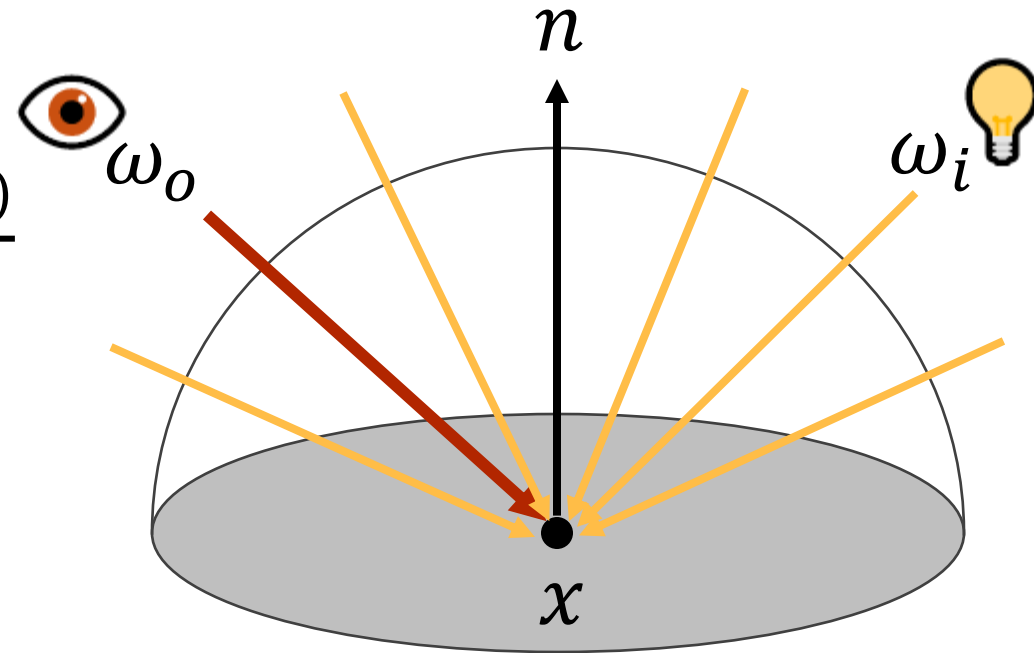




# Ray Tracing

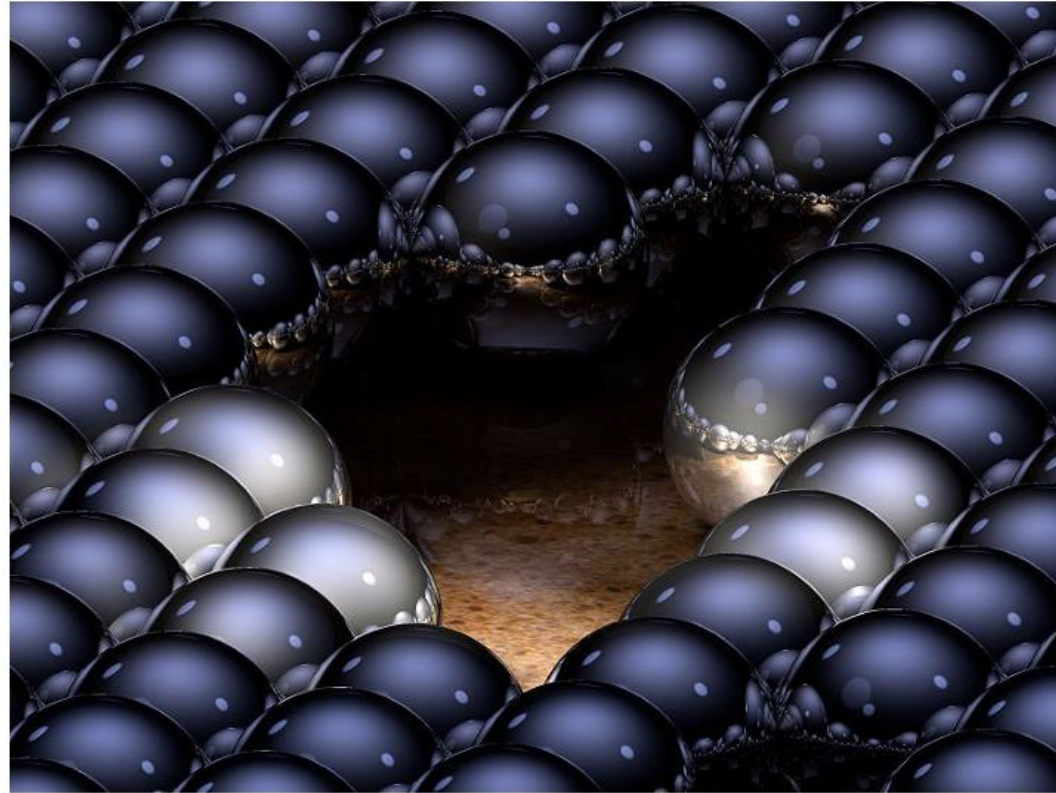
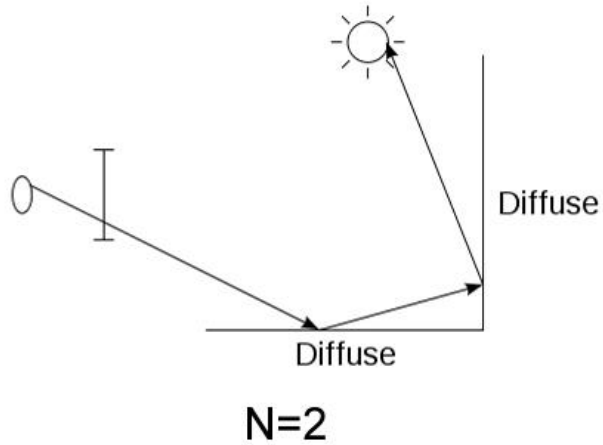
- March the ray until it hits surface
- Sample ray from specific distribution  $p(\omega)$  (e.g. BRDF)
- Approximate the integral with Monte Carlo integration

$$L_o(x, \omega_o) = \frac{1}{N} \sum_{i=1}^N \frac{f(x, \omega_i, \omega_o) L_i(x, \omega_i) (\omega_i \cdot n)}{p(\omega_i)}$$



# Interreflections

- Reflect light  $N$  times before heading to light source

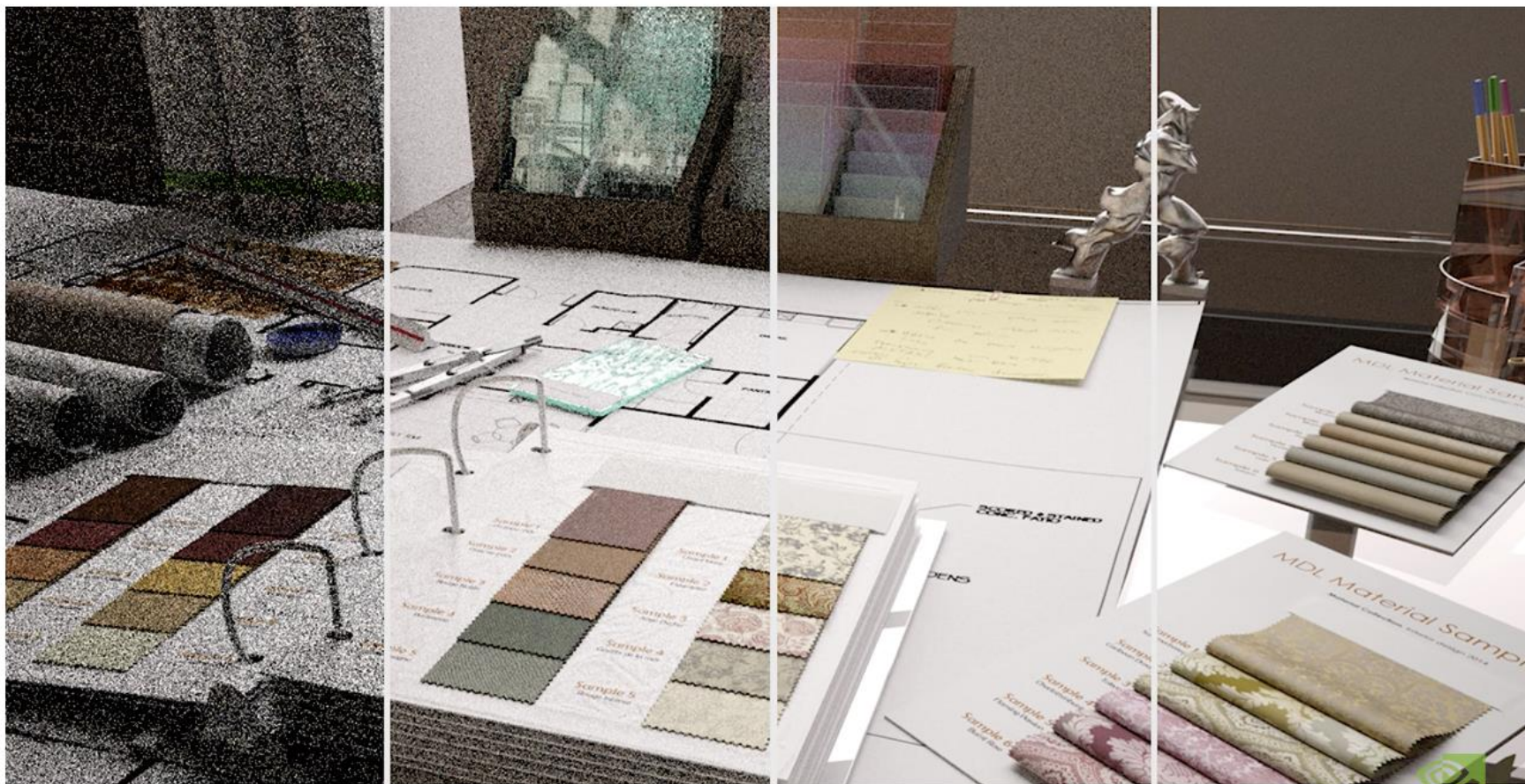


N=16

[http://en.wikipedia.org/wiki/Ray\\_tracing\\_\(graphics\)#mediaviewer/File:Ray-traced\\_steel\\_balls.jpg](http://en.wikipedia.org/wiki/Ray_tracing_(graphics)#mediaviewer/File:Ray-traced_steel_balls.jpg)

# Denoising

- Few ray samples lead to noisy images



5 samples/pixel (spp)

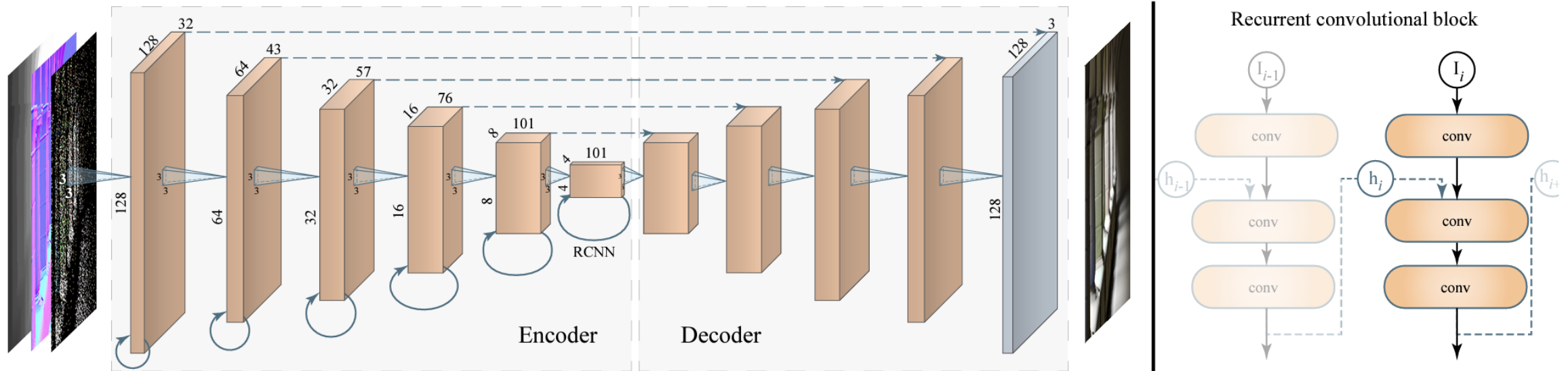
50 spp

500 spp

5,000 spp

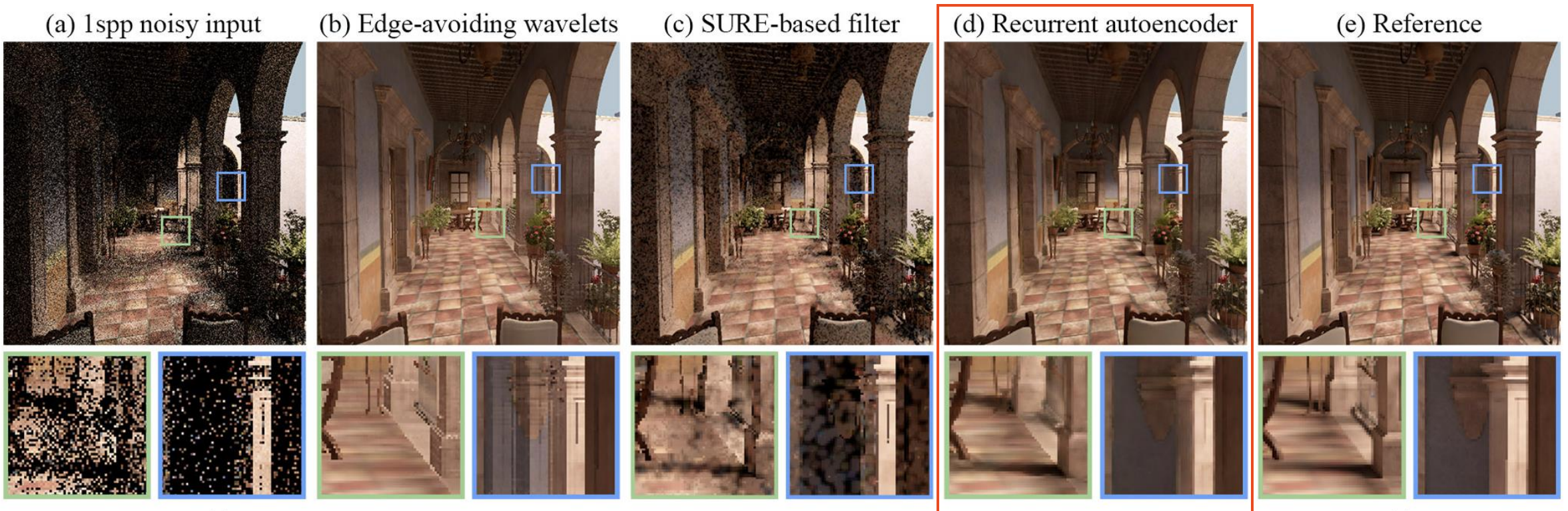
# Denoising

- Based on the information of neighboring pixels, fill in the missing ones
- Deep learning could be used for image denoising



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- Deep learning could be used for image denoising

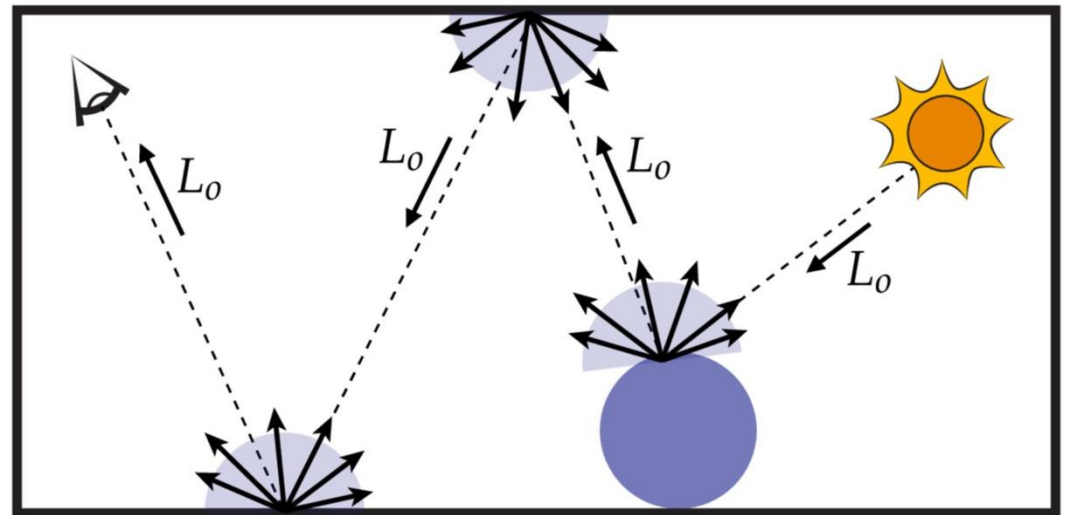


# Ray tracing

- Conceptually simple but hard to do fast

Design choices:

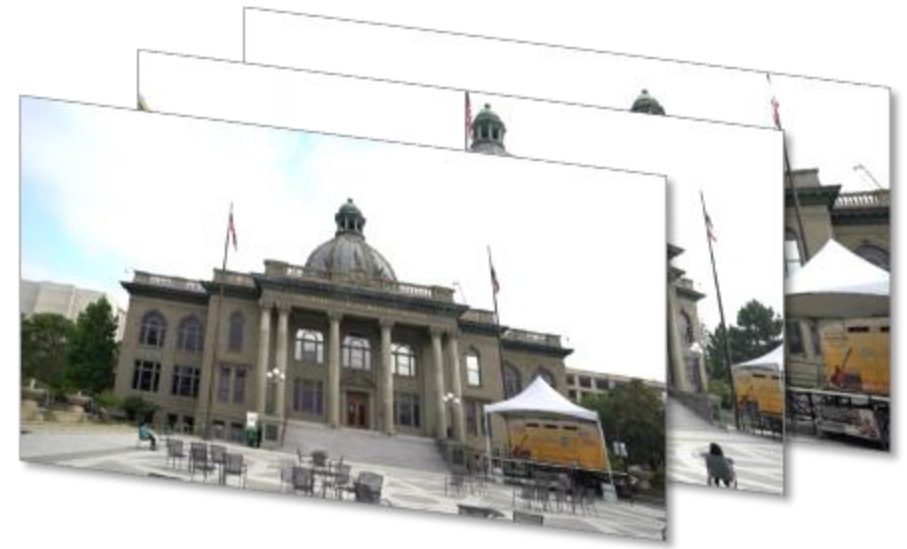
- Ray paths: light  $\rightarrow$  camera vs. camera  $\rightarrow$  light
- How many samples per pixel?
- How to sample the rays?
- When should the rays stop?
- How to denoise the image?
- ...



# How to render 2D from 3D?

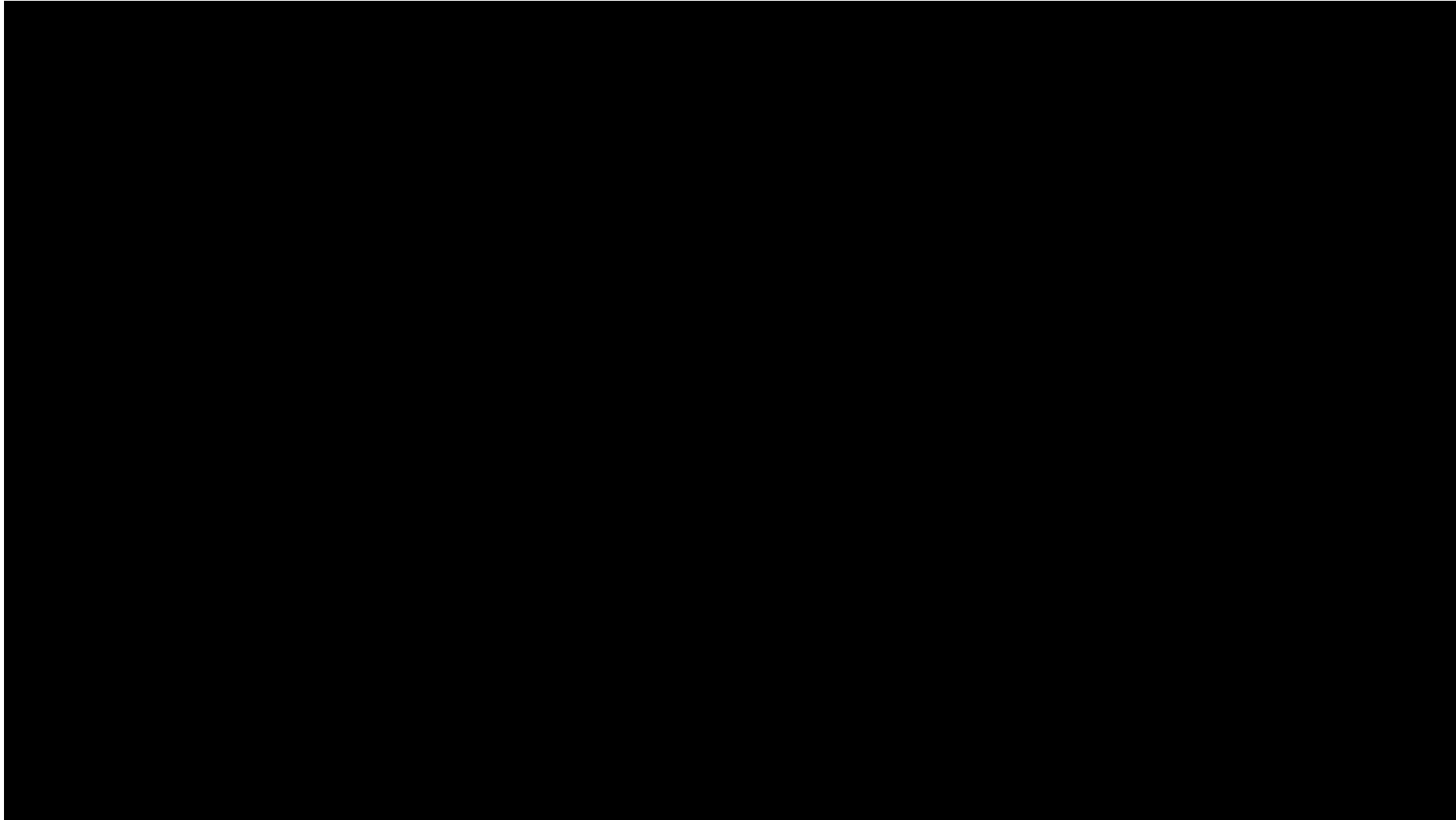


3D scene



2D images/videos

# Creating virtual contents is EXPENSIVE



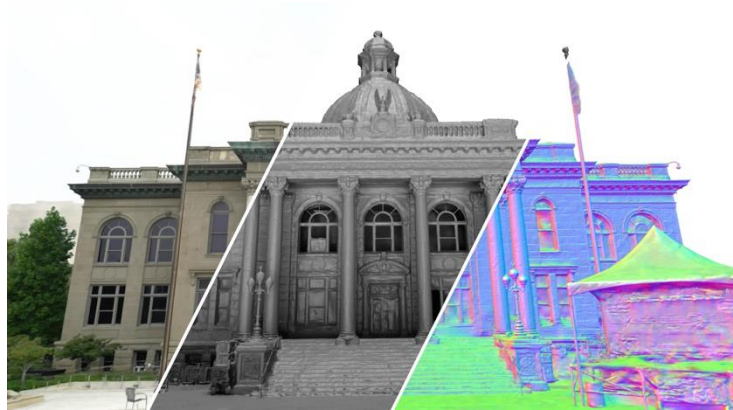
<https://www.youtube.com/watch?v=zaqmn55w4IA>



# Can we reduce the cost?



2D images/videos



3D scene



Applications (AR/VR)

Photo credit:

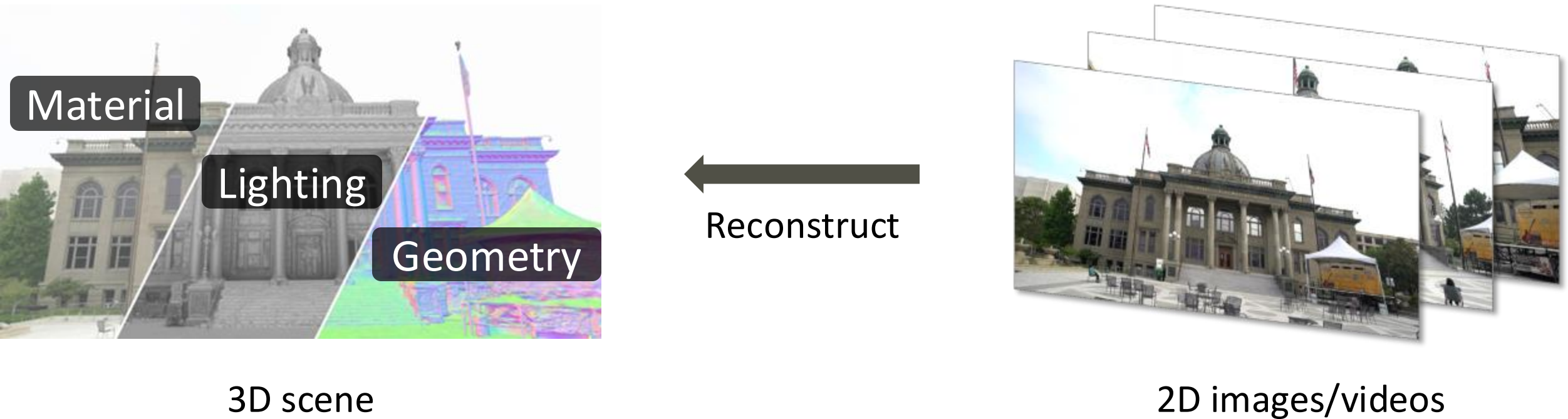
Neuralangelo: High-Fidelity Neural Surface Reconstruction (CVPR'23)

Tanks and Temples (<https://www.tanksandtemples.org/>)

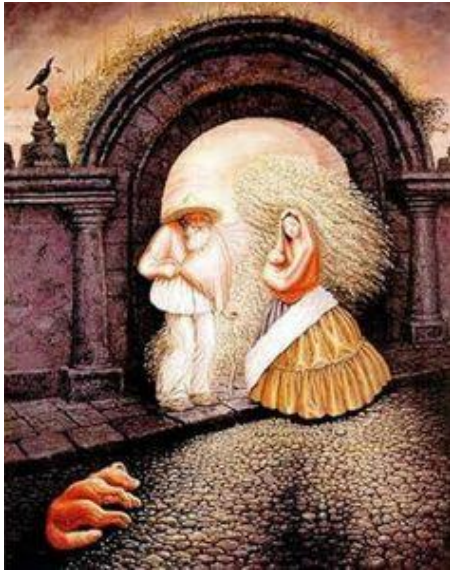
<https://www.youtube.com/watch?v=IY4x85zqoJM>

# Inverse rendering

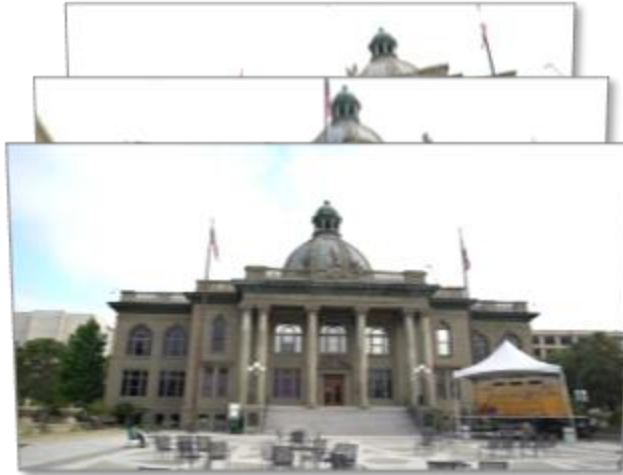
How to reconstruct 3D from 2D?



# Inverse rendering is CHALLENGING



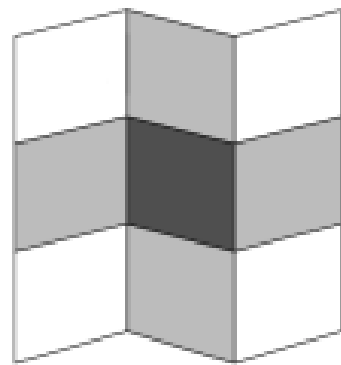
Ill-posed problem



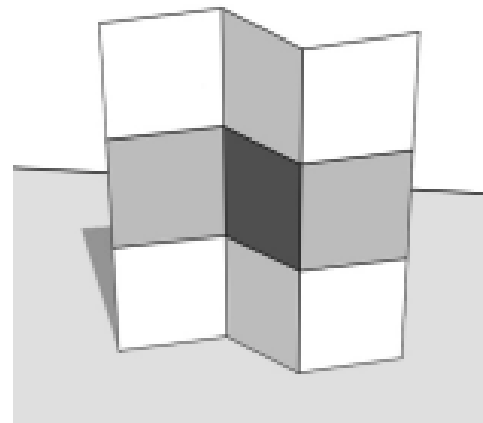
Incomplete observation



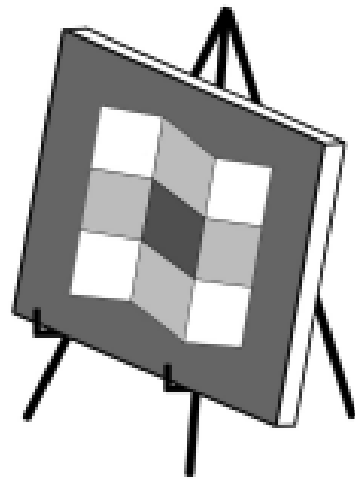
Limited real 3D data  
Noise in real 2D data



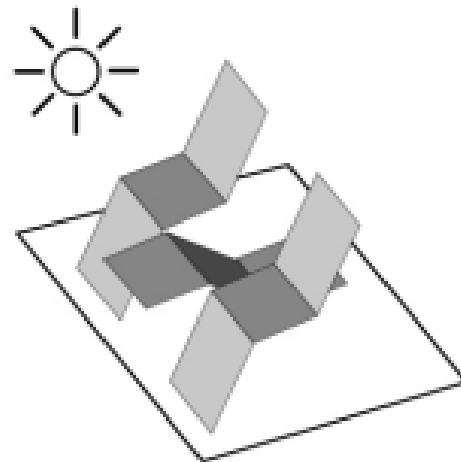
(a) an image



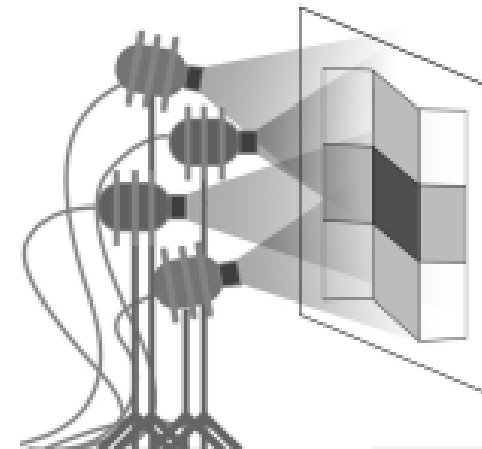
(b) a likely explanation



(c) painter's explanation

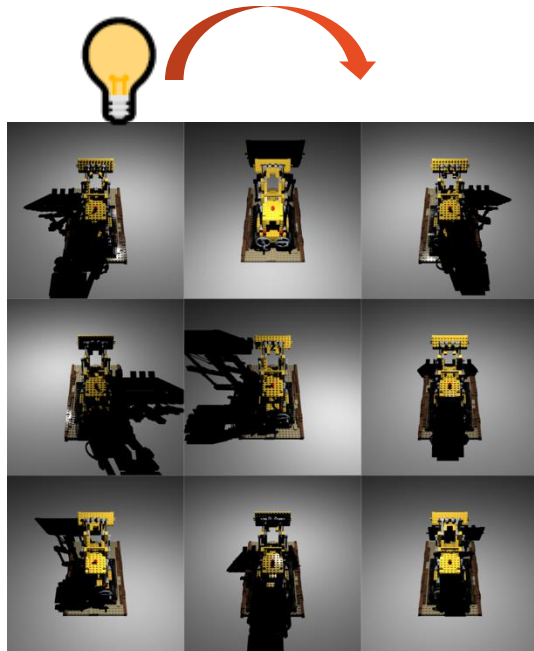


(d) sculptor's explanation

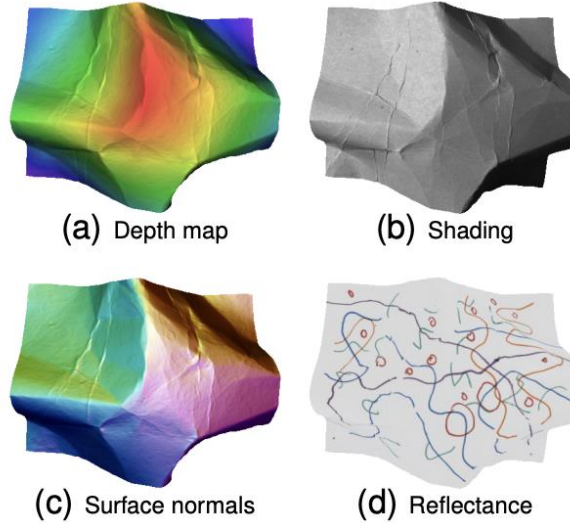


(e) gaffer's explanation

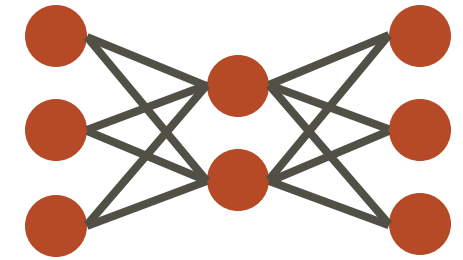
# Strategies



Increase observation



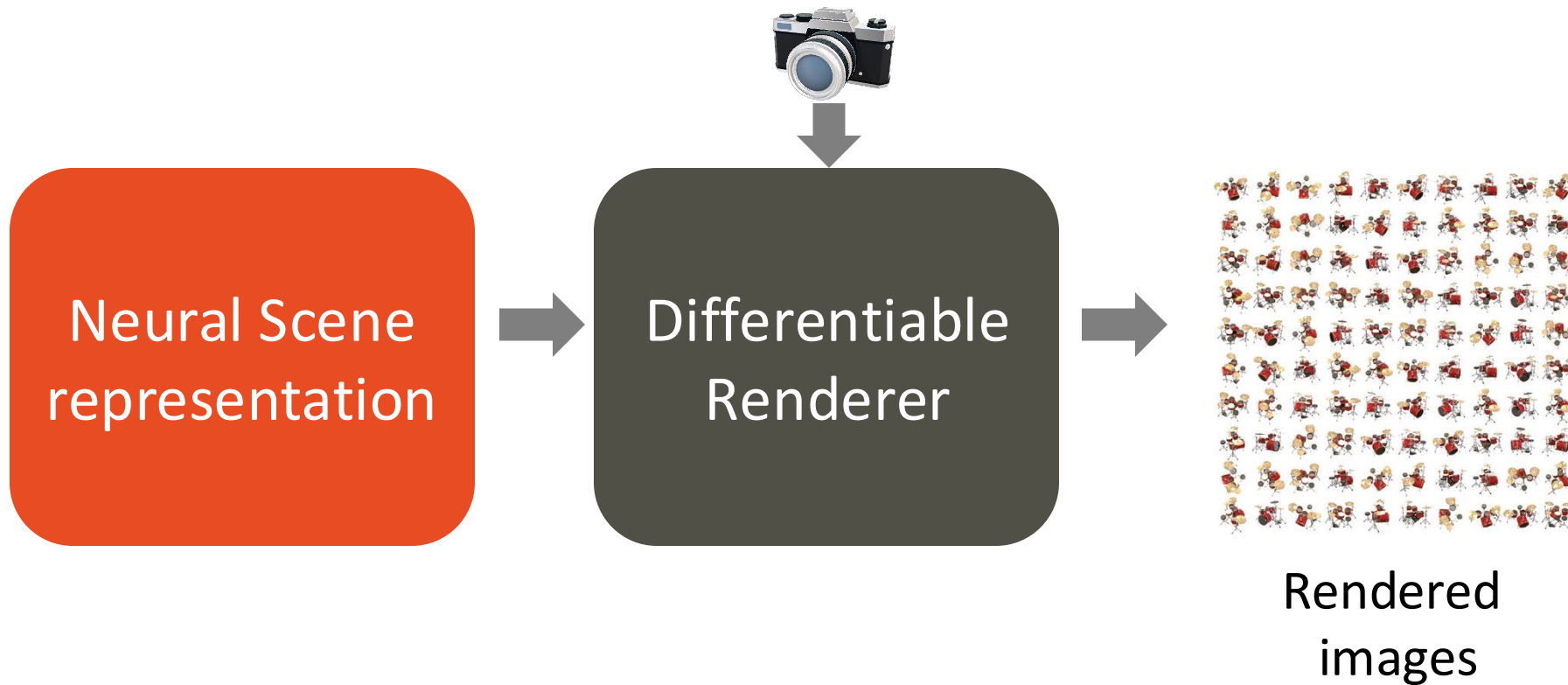
Introduce scene priors



Differentiable rendering

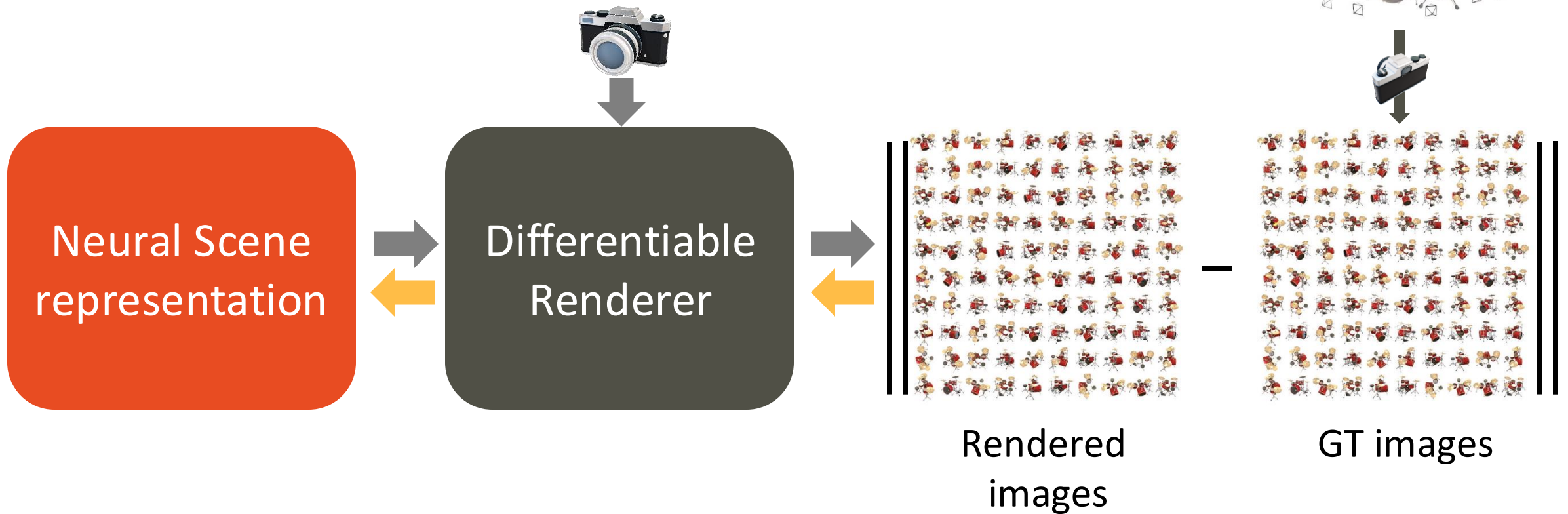
# Differentiable rendering

1. Set the scene as learnable parameters
2. Differentiable forward rendering



# Differentiable rendering

3. Optimize scene parameters with gradient descent!



# Neural Radiance Field (NeRF)



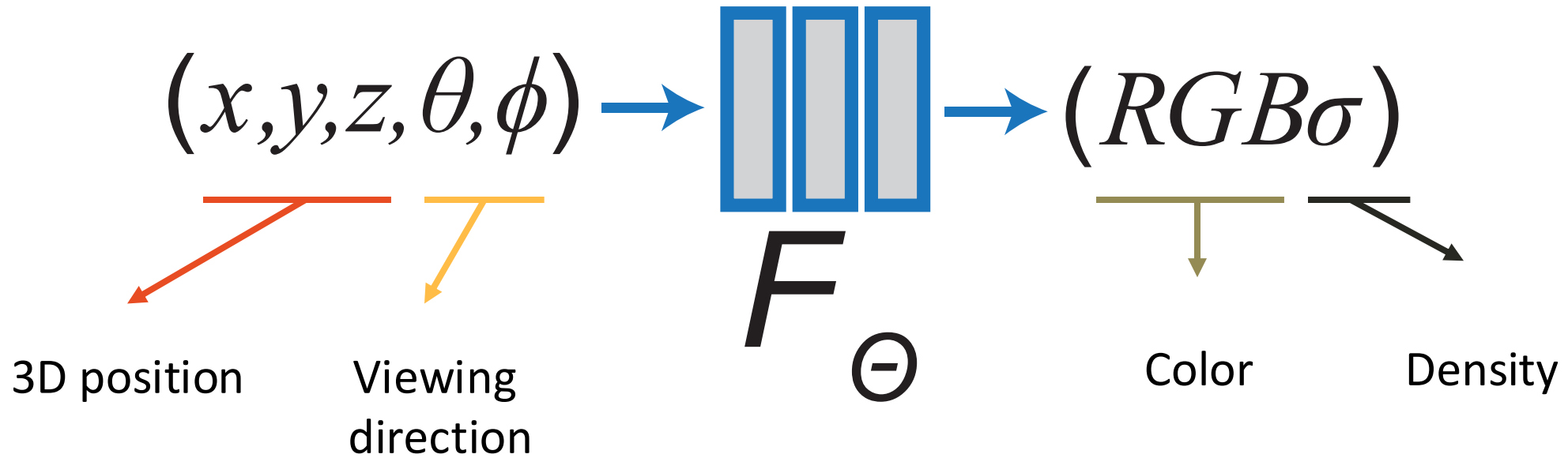
Multi-view images +  
Camera pose



3D scene

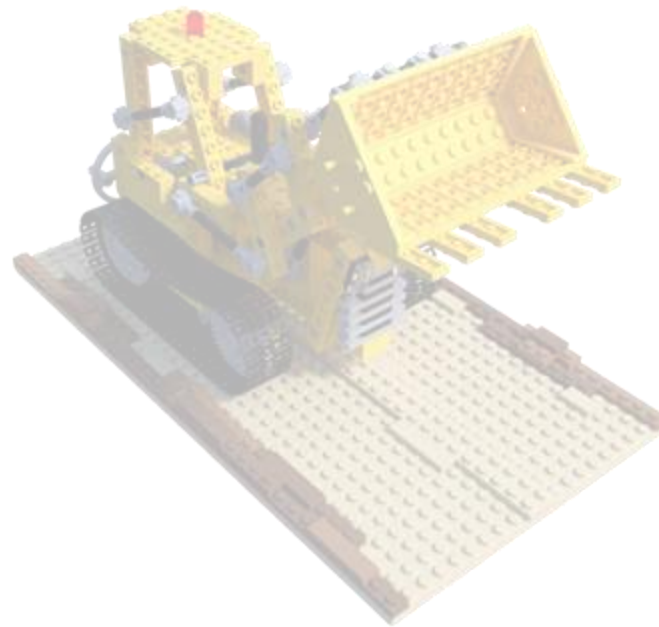
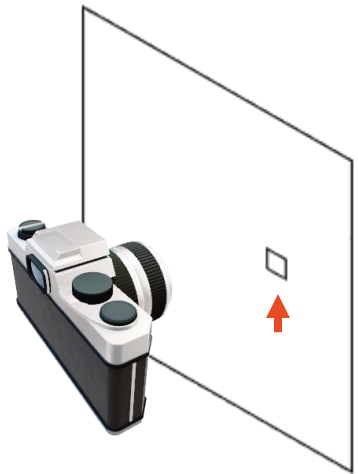


# NeRF: representation



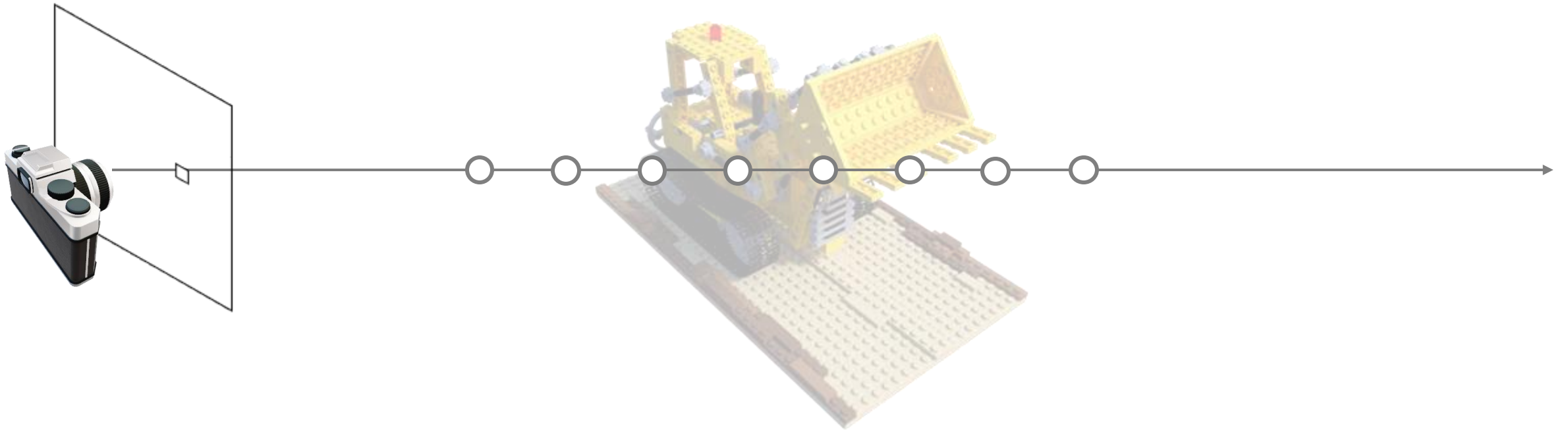
# Volume rendering

How to calculate the color of the pixel?



# Volume rendering

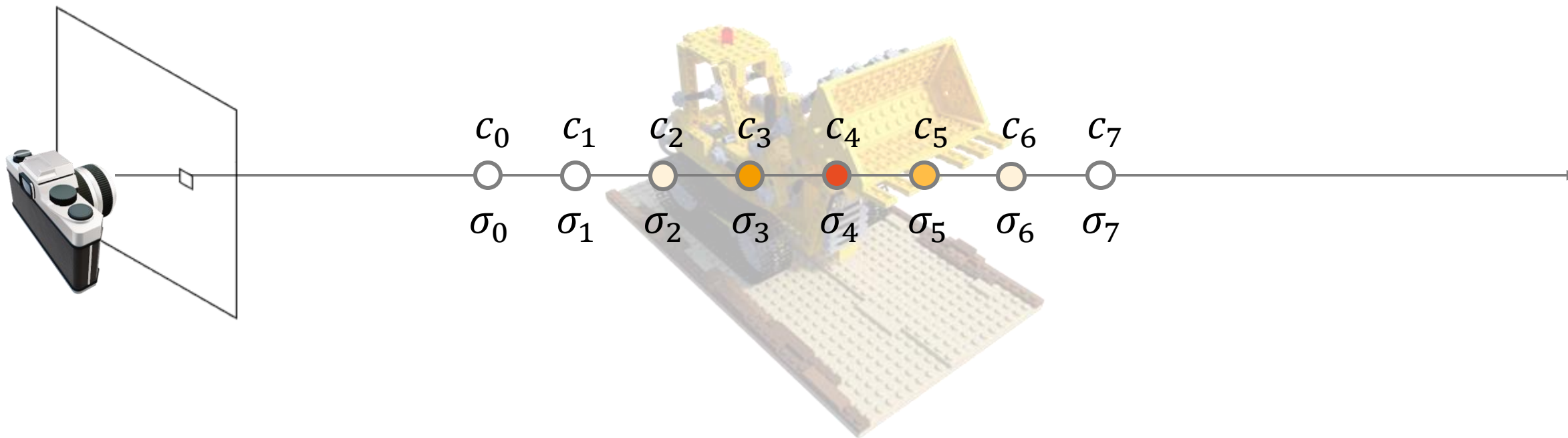
1. Cast a ray from camera to the scene
2. Sample multiple points along the ray



# Volume rendering

3. Predict color, density of each point

$$(x, y, z, \theta, \phi) \rightarrow \begin{matrix} \text{||||} \\ F_{\Theta} \end{matrix} \rightarrow (RGB\sigma)$$



# Volume rendering

Weighted sum of point color

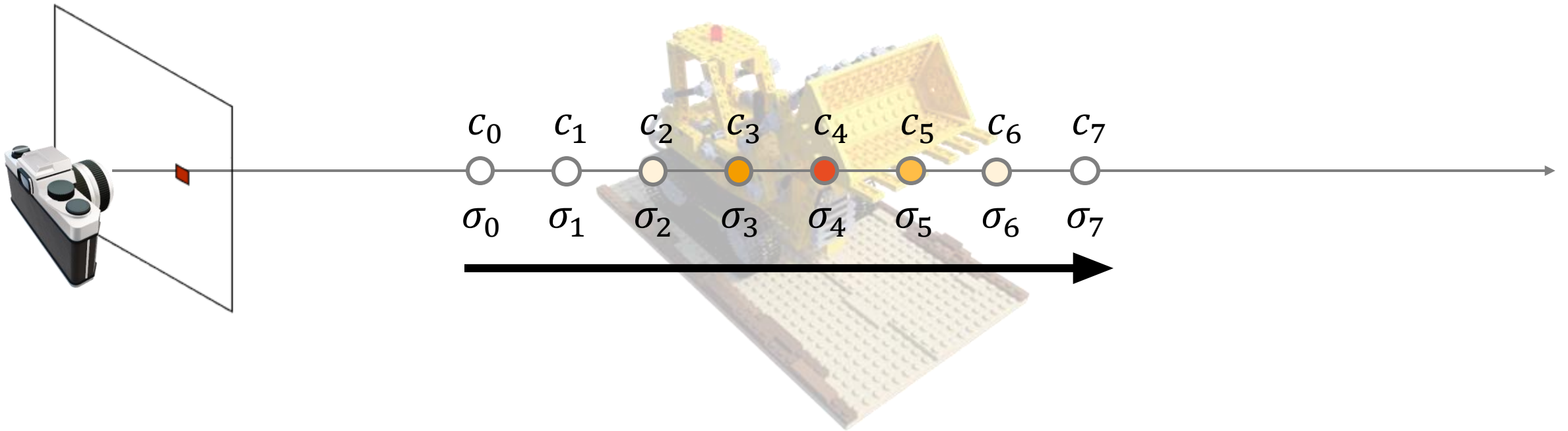
$$C(r) = \sum_{i=1}^N T_i \alpha_i c_i$$

How much light is NOT blocked yet

$$T_i = \exp\left(-\sum_{j=1}^{i-1} \sigma_j \delta_j\right)$$

How much light is blocked by this point

$$\alpha_i = 1 - \exp(-\sigma_i \delta_i)$$



# Volume rendering

Weighted sum of point color

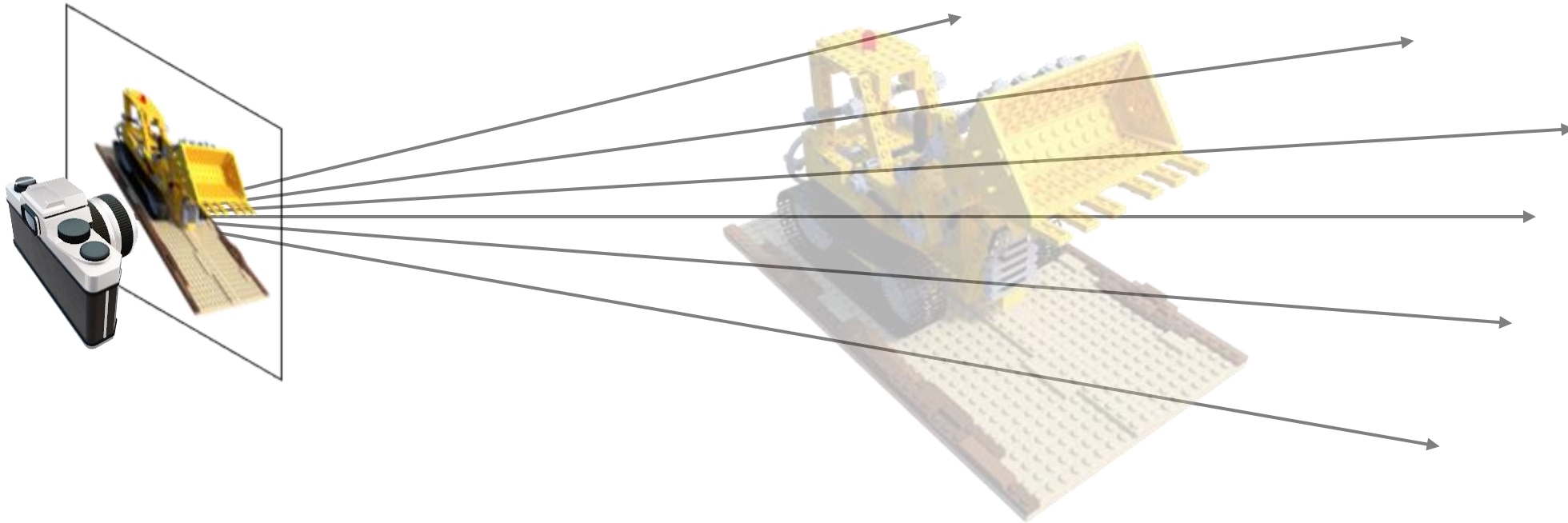
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NOT blocked yet

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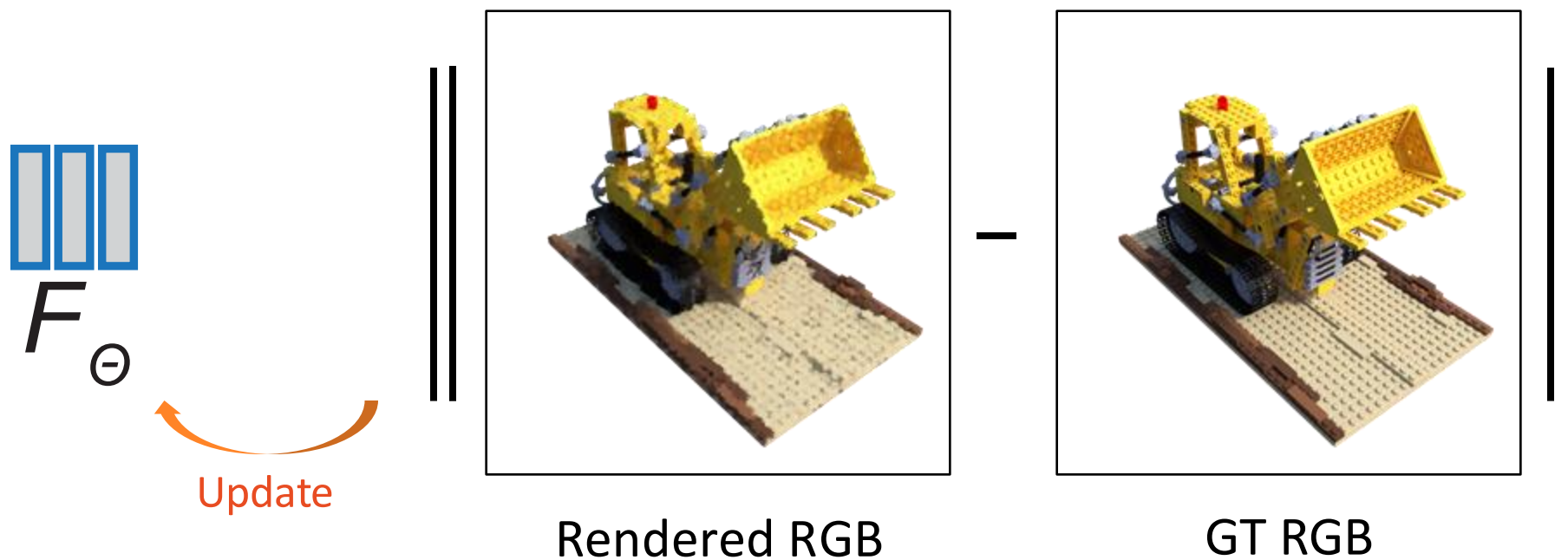
How much light is  
blocked by this point

$$\alpha_i = 1 - \exp(-\sigma_i \delta_i)$$

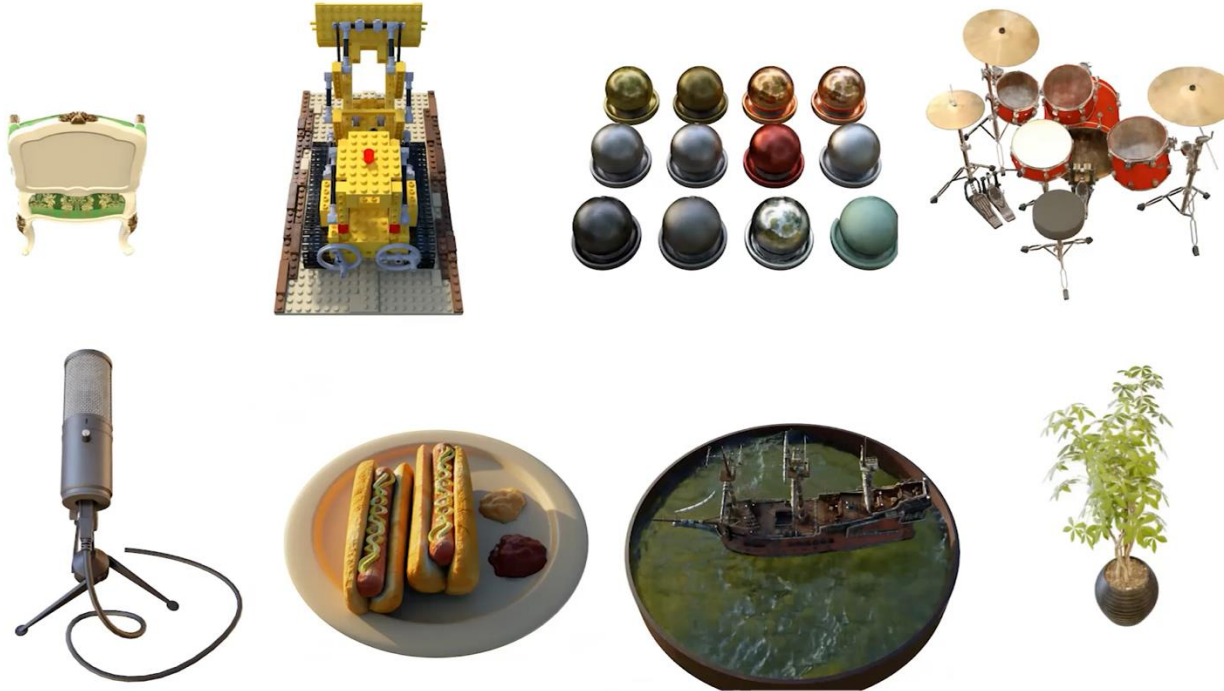


# NeRF: optimization

$$L = \sum_{r \in R} \|\overset{\text{Rendered}}{C(r)} - \overset{\text{GT}}{\hat{C}(r)}\|_2^2$$



# Neural Radiance Field (NeRF)



## Strength

- Realistic novel view synthesis
- GT 3D data is not required

## Weakness

- Limited to small scenes
- No lighting and material decomposition
- Slow optimization & rendering

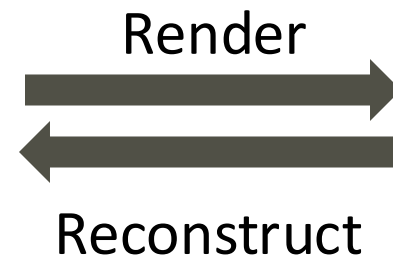


# We have talked about ...

- What are the basic components of rendering process?
  - Geometry, lighting, material, BRDF
- How to render an image?
  - Rendering equation, Ray tracing, denoising
- What is inverse rendering? Why is it challenging?
  - Ill-posed problem, incomplete observation, limited data



3D scene



2D images/videos

# We have NOT talked about ...

- How to parameterize lighting and material (e.g. BRDF)?
- What are other ways to render an image?
  - Rasterization, 3D Gaussian Splatting
- How to estimate smooth surfaces from images?
- How to estimate lighting and material?
- How to insert virtual objects in real-world images/videos?
- Data-driven approaches for inverse rendering
- ...

We will discuss some of the topics in the following lectures!