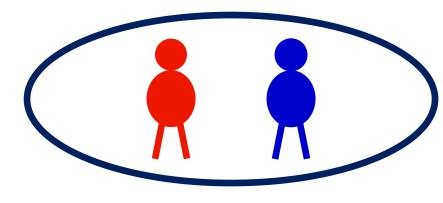
Algorithmic Game Theory

Instructor: Ruta Mehta

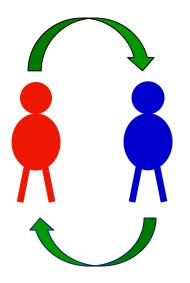
TA: Rucha Kulkarni

Game Theory

Multiple self-interested agents interacting in the same environment

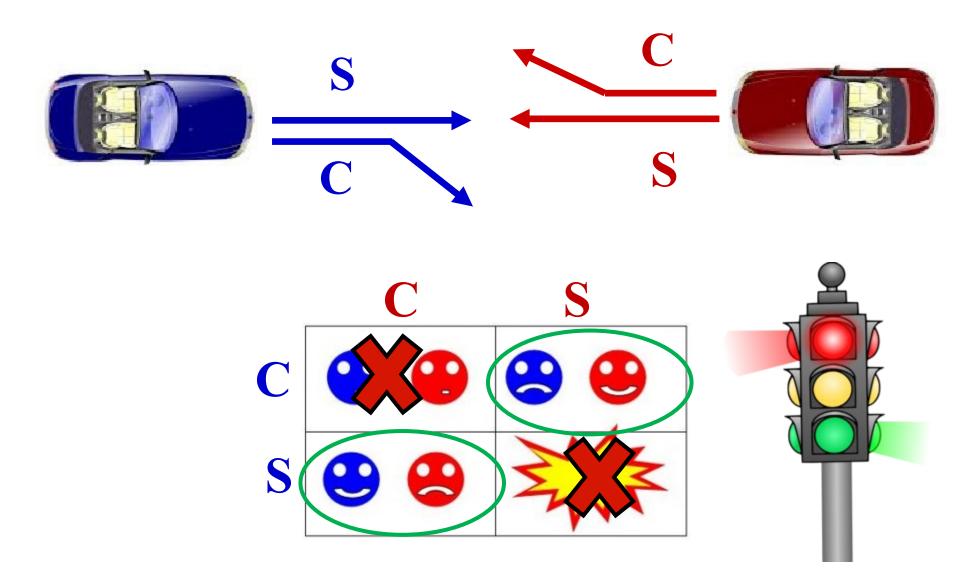


Deciding what to do.



Q: What to expect? How good is it? Can it be controlled?

Game of Chicken (Traffic Light)



Algorithmic Game Theory

AGT, in addition, focuses on designing efficient algorithms to compute solutions necessary to make accurate prediction.

■ What to expect

Research-oriented Course

- □ Exposure to key concepts and proof techniques from AGT
- □ Explore research problems and novel questions

■ What is expected from you

- □ Pre-req: Basic knowledge of linear-algebra, linear programming, probability, algorithms.
- ☐ Energetic participation in class
- □ Research/Survey Project (individually or in a group of two).

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 - Instructor: Ruta Mehta (Me)
 - TA: Rucha Kulkarni
 - Office hours:
 - □ Ruta: Wed 2:30-3:30pm on zoom
 - □ Rucha: Mon 2:30-3:30pm on zoom

For zoom links, see

https://courses.grainger.illinois.edu/cs598rm/fa2020/secure/online.html

(you will need Illinois login to access this page)

- Compass 2g for grades
 - □ https://compass2g.illinois.edu/webapps/login/

Useful links

■ Webpage:

https://courses.engr.illinois.edu/cs598rm/

■ Piazza Page:

piazza.com/illinois/fall2020/cs598rm

Check webpage/piazza at least twice a week for the updates.

HW0 is already posted!

■ Grading:

- \square 4 homeworks 45% (10,10,10,15)
- □ Research/Survey Project 50%
 - Work -25%
 - Presentation 12.5%
 - Report 12.5%
- □ Class participation 5%

HW0 is for self-study and carry no points.

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References

- T. Roughgarden, Twenty Lectures on Algorithmic Game Theory, 2016.
- N. Nisan, T. Roughgarden, E. Tardos, and V. Vazirani (editors), Algorithmic Game Theory, 2007. (Book available online for free.)
- R. Myerson, Game Theory: Analysis of conflict, 1991.

Recent papers, and other lecture notes that we will post on course website.

3 Broad Goals

Goal #1

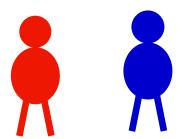
Understand outcomes arising from interaction of intelligent and self-interested agents.

Games and Equilibria

Prisoner's Dilemma

Two thieves caught for burglary.

Two options: {confess, not confess}

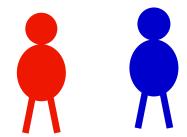


	N	C	
N	-1 -1	-6 0	
C	0 -6	-5 -5	

Prisoner's Dilemma

Two thieves caught for burglary.

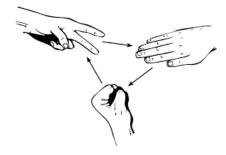
Two options: {confess, not confess}



	N	C	
N	-1 -1	-6 0	
C	0 -6	-5 -5	

Only stable state

Rock-Paper-Scissors



	R	P	S
R	0 0	-1 1	1 -1
P	1 -1	0 0	-1 1
S	-1 1	1 -1	0 0

No pure stable state!

Both playing (1/3,1/3,1/3) is the only NE.

Nash Eq.: No player gains by deviating individually

Why?



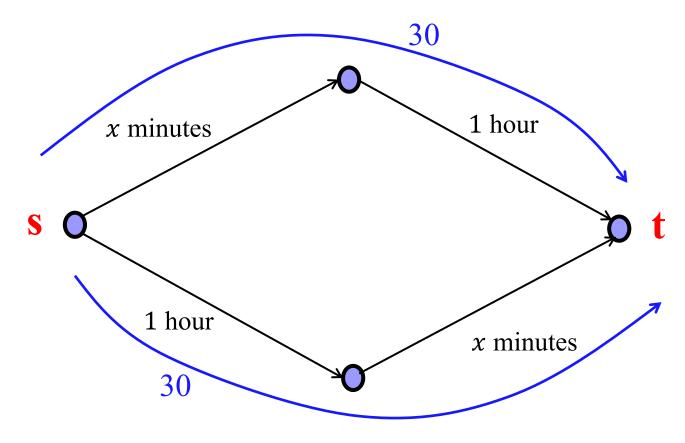
- Normal form games and Nash equilibrium existence
- Computation:
 - □ Zero-sum: minmax theorem,
 - ☐ General: (may be) Lemke-Howson algorithm
- Complexity: PPAD-complete
- Other equilibrium notions markets, security games
- Incomplete information, Bayesian Nash
- Collusion, Core, Nash bargaining

Goal #2

Analyze quality of the outcome arising from strategic interaction, i.e. OPT vs NE.

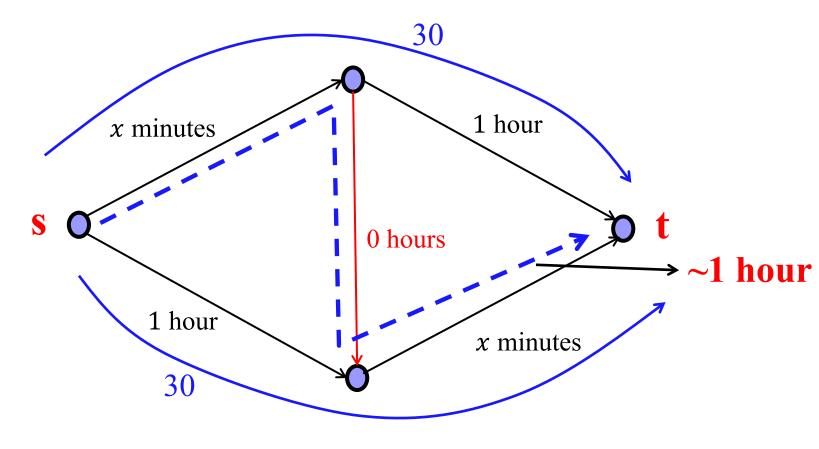
Price of Anarchy

60 commuters



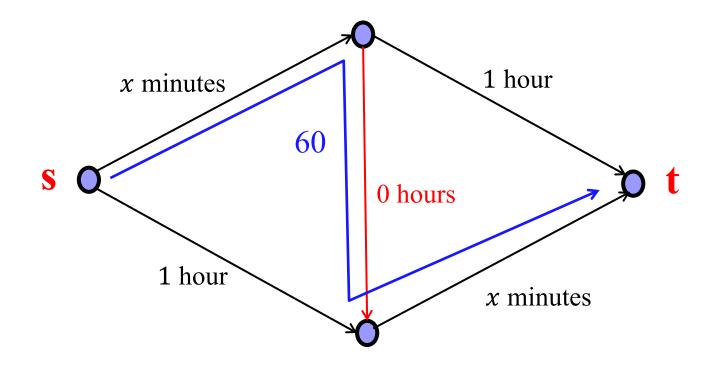
Commute time: 1.5 hours

60 commuters



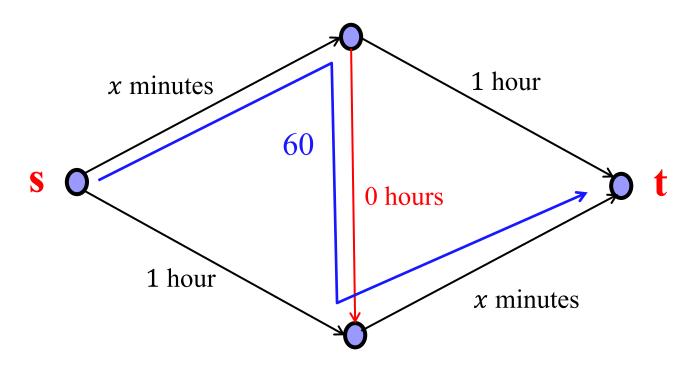
Commute time: 1.5 hours

60 commuters



Commute time: 2 hours

60 commuters



Price of Anarchy (PoA):
$$\frac{worst \, NE}{OPT} = \frac{2}{1.5} = \frac{4}{3}$$

Can not be worse!



- Network routing games
- Congestion (potential) games
- PoA in linear congestion games
 - □ Smoothness framework
- Iterative play and convergence

Goal #3

Designing rules to ensure "good" outcome under strategic interaction among selfish agents.

Mechanism Design

At the core of large industries

Online markets – eBay, Uber/Lyft, TaskRabbit, cloud markets

Spectrum auction – distribution of public good. enables variety of mobile/cable services.

Search auction – primary revenue for google!

Tons of important applications

Fair Division – school/course seats assignment, kidney exchange, air traffic flow management, ...

Voting, review, coupon systems.

So on ...

- 10
 - MD without money
 - ☐ Fair division
 - Divisible items: Competitive equilibrium
 - Indivisible items: EF1, EFX, MMS, Max. Nash Welfare, ...
 - □ stable matching, Arrow's theorem (voting)
 - MD with money
 - ☐ First price auction, second price auction, VCG
 - ☐ Generalized second price auction for search (Google)
 - □ Optimal auctions: Myerson auction and extensions

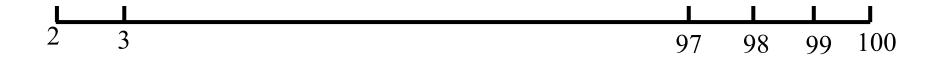
Fun Fact!

Olympics 2012 Scandal Check out Women's doubles badminton tournament

Video of the fist controversial match

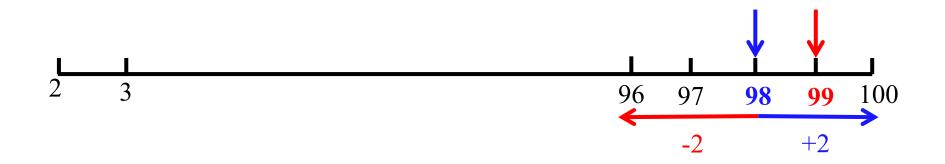
Food for Thought

You and your friend choose a number ...



Food for Thought

You and your friend choose a number ...



What will you choose?

What if \pm 50?

What are Nash equilibria?