

# Computational Approaches to Cameras

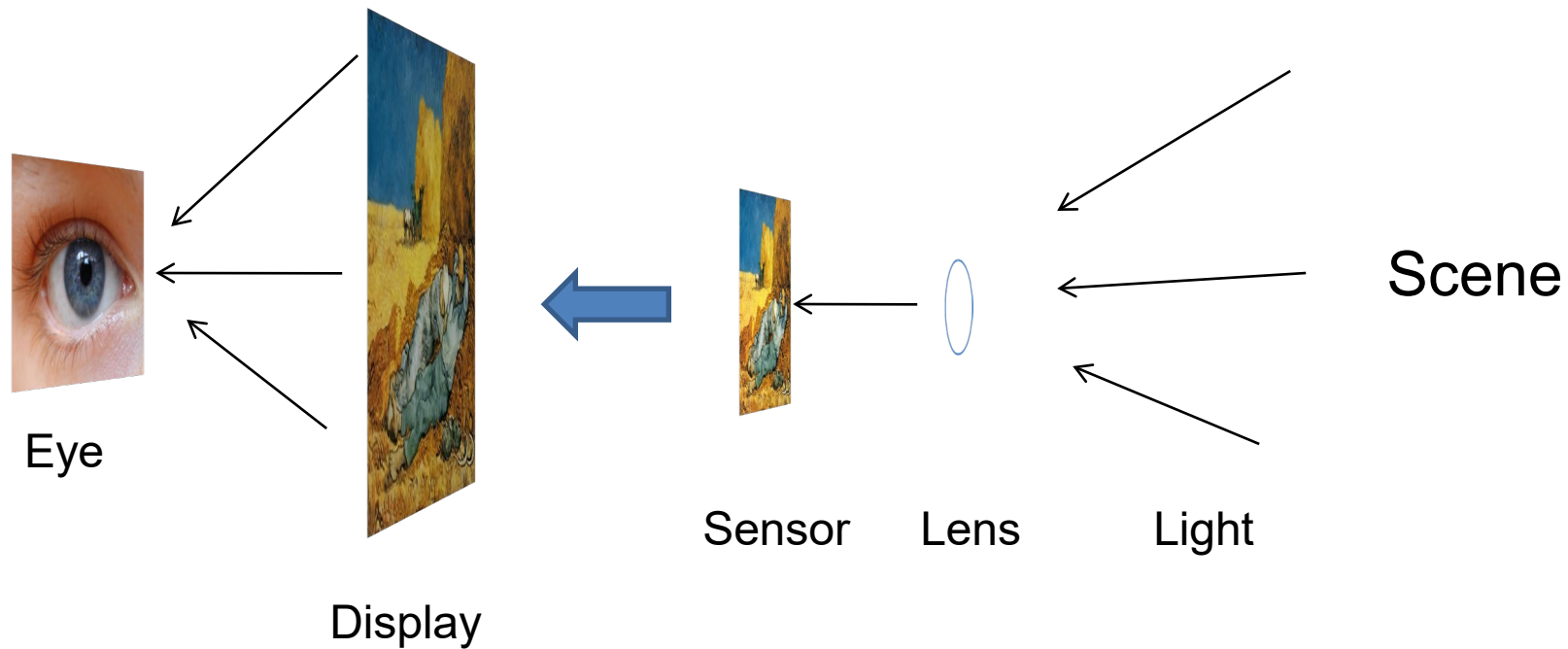


Magritte , *The False Mirror* (1935)

Computational Photography  
Derek Hoiem, University of Illinois

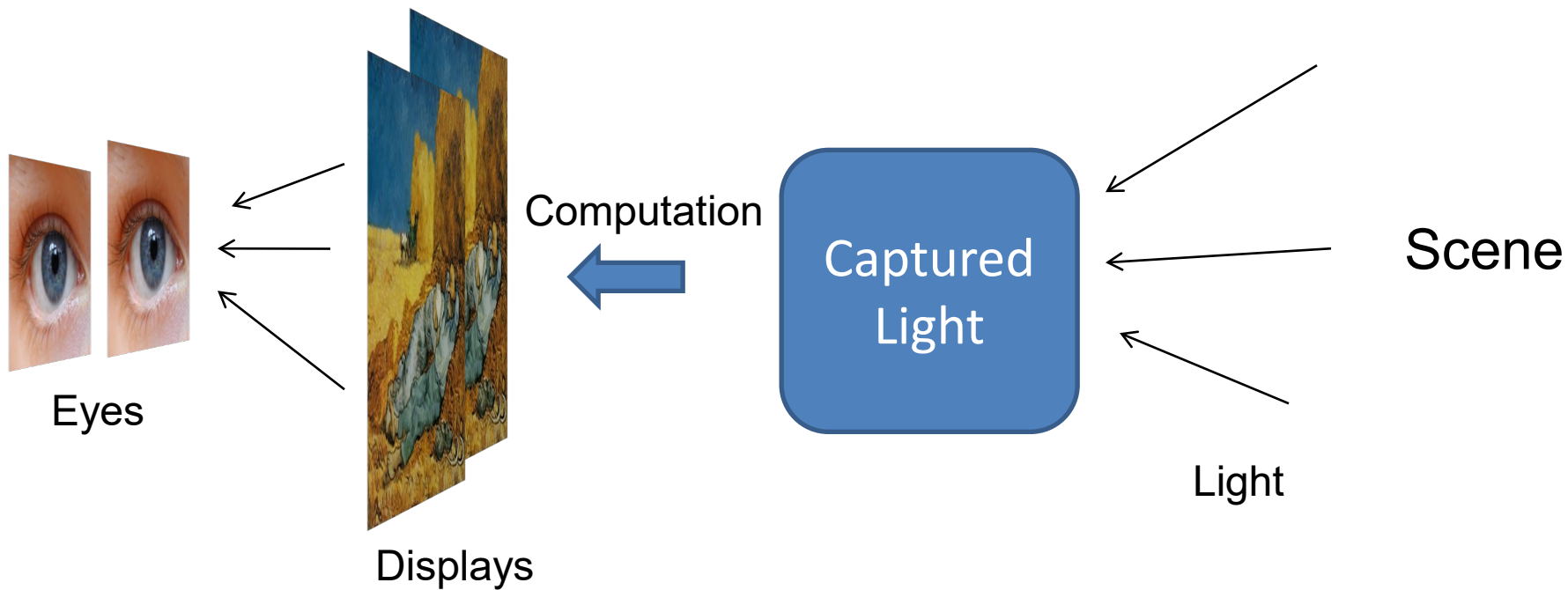
# Conventional cameras

Conventional cameras are designed to capture light in a medium that is directly viewable



# Computational cameras

With a computational approach, we can capture light and then figure out what to do with it



# Questions for today

- How can we represent all of the information contained in light?
- What are the fundamental limitations of cameras?
- What sacrifices have we made in conventional cameras? For what benefits?
- How else can we design cameras for better focus, deblurring, multiple views, depth, etc.?

# Representing Light: The Plenoptic Function



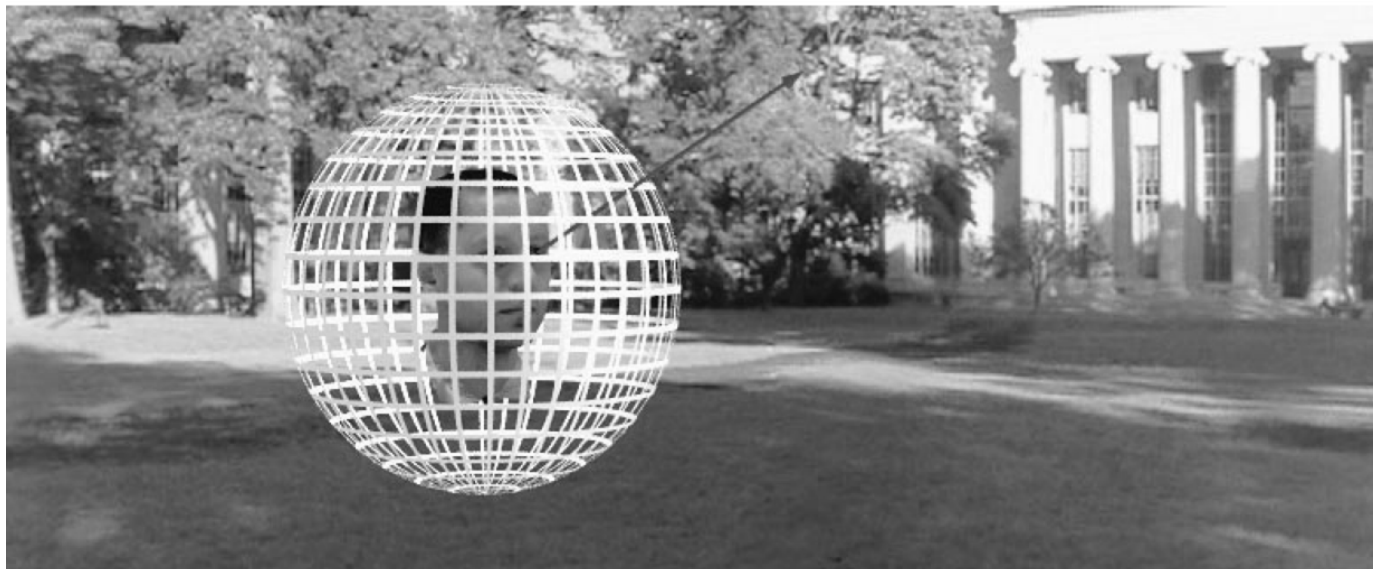
Figure by Leonard McMillan

Q: What is the set of all things that we can ever see?

A: The Plenoptic Function (Adelson & Bergen)

Let's start with a stationary person and try to parameterize everything that he can see...

# Grayscale snapshot



$$P(\theta, \phi)$$

is intensity of light

- Seen from a single view point
- At a single time
- Averaged over the wavelengths of the visible spectrum

(can also do  $P(x,y)$ , but spherical coordinate are nicer)

# Color snapshot



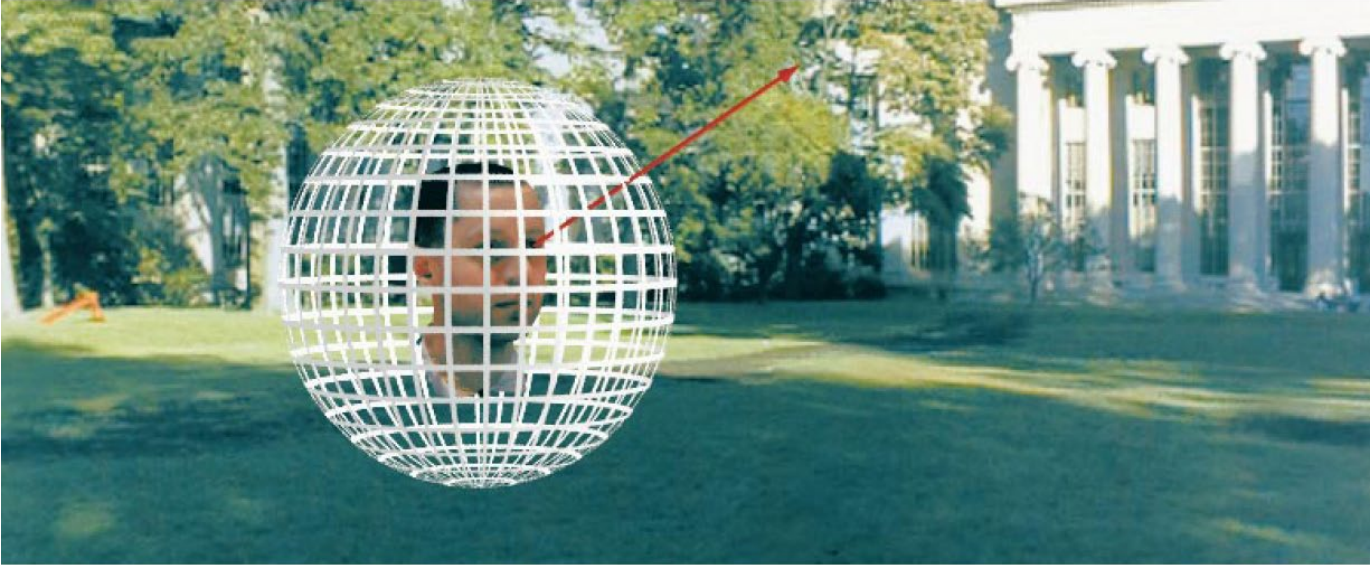
$$P(\theta, \phi, \lambda)$$

is intensity of light

- Seen from a single view point
- At a single time
- As a function of wavelength



# A movie



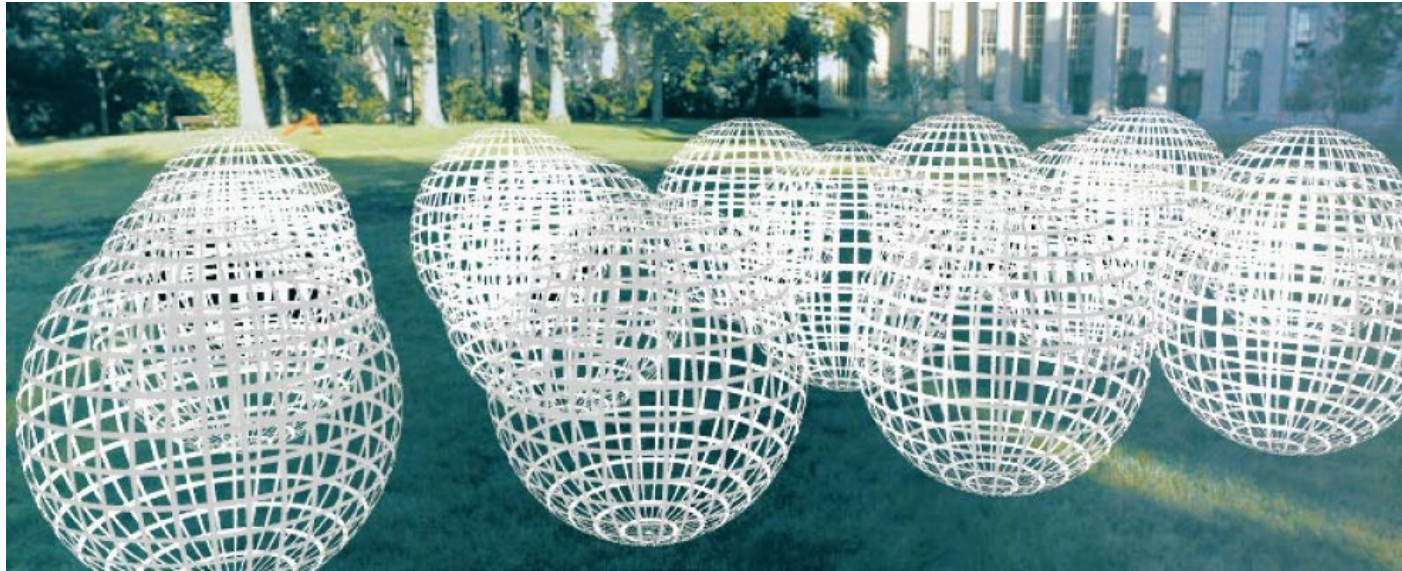
$$P(\theta, \phi, \lambda, t)$$

is intensity of light

- Seen from a single view point
- Over time
- As a function of wavelength



# Holographic movie (or VR)

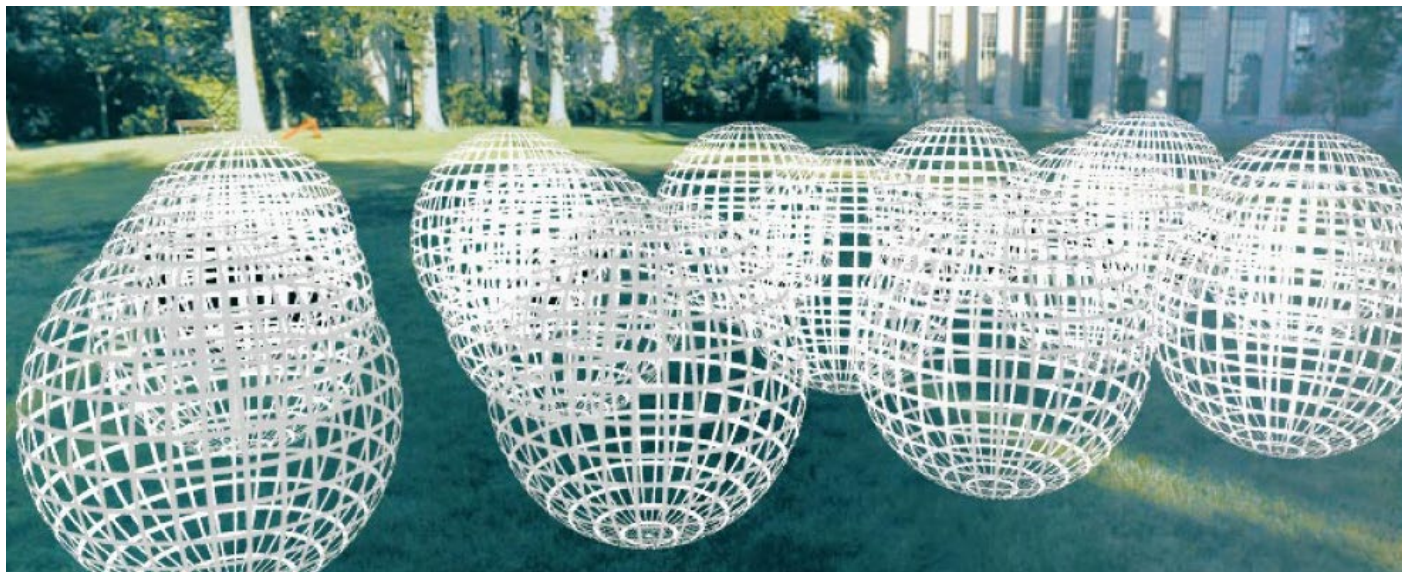


$$P(\theta, \phi, \lambda, t, V_x, V_y, V_z)$$

is intensity of light

- Seen from ANY viewpoint
- Over time
- As a function of wavelength

# The Plenoptic Function



$$P(\theta, \phi, \lambda, t, V_x, V_y, V_z)$$

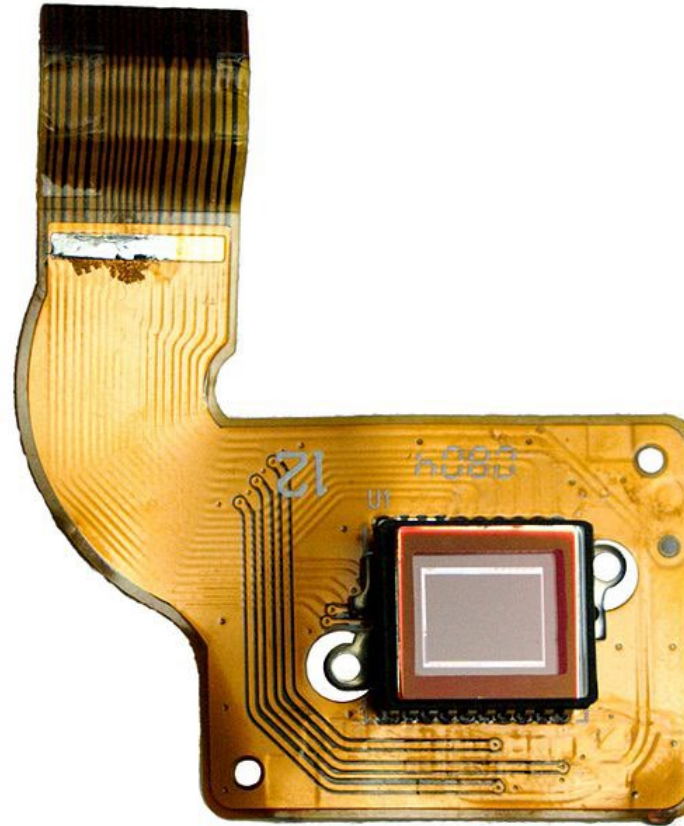
- Can reconstruct every possible view, at every moment, from every position, at every wavelength
- If the domain is complete, contains every photograph, every movie, everything that anyone has ever seen!

# Representing light

The atomic element of light: ~~a pixel~~ **a ray**

# Fundamental limitations and trade-offs

- Only so much light in a given area to capture
- Basic sensor accumulates light at a set of positions from all orientations, over all time
- We want **intensity** of light at a **given time** at **one position** for a **set of orientations**
- Solutions:
  - funnel, constrain, redirect light
  - change the sensor



CCD inside camera



# Trade-offs of conventional camera

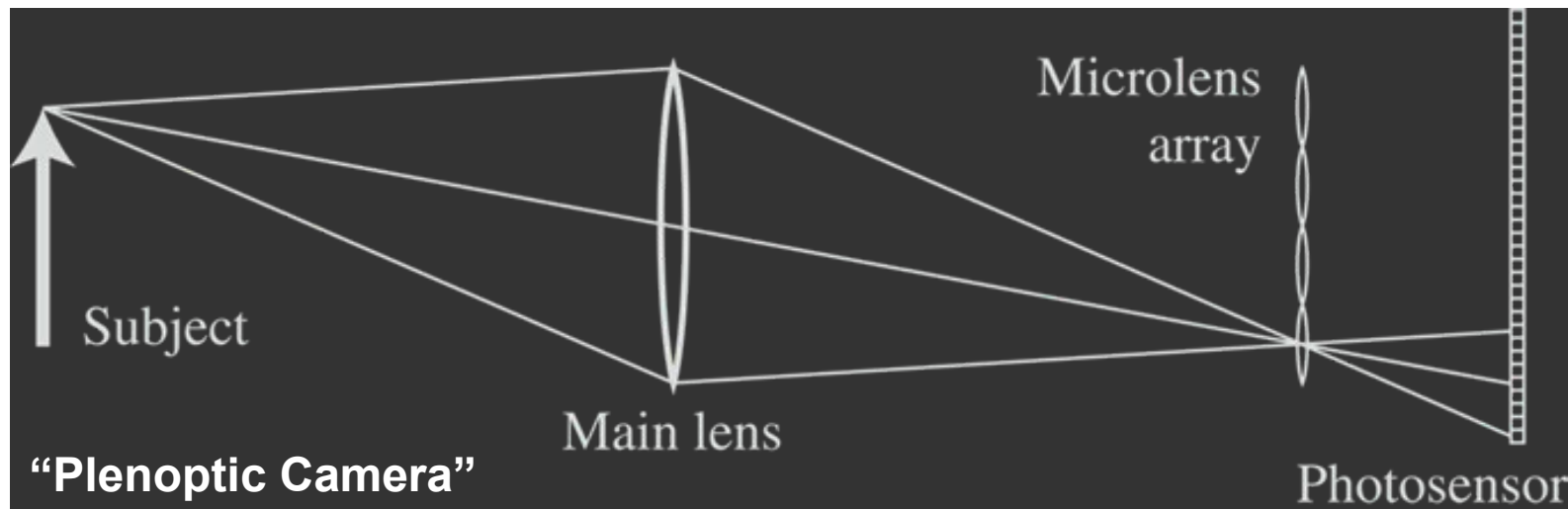
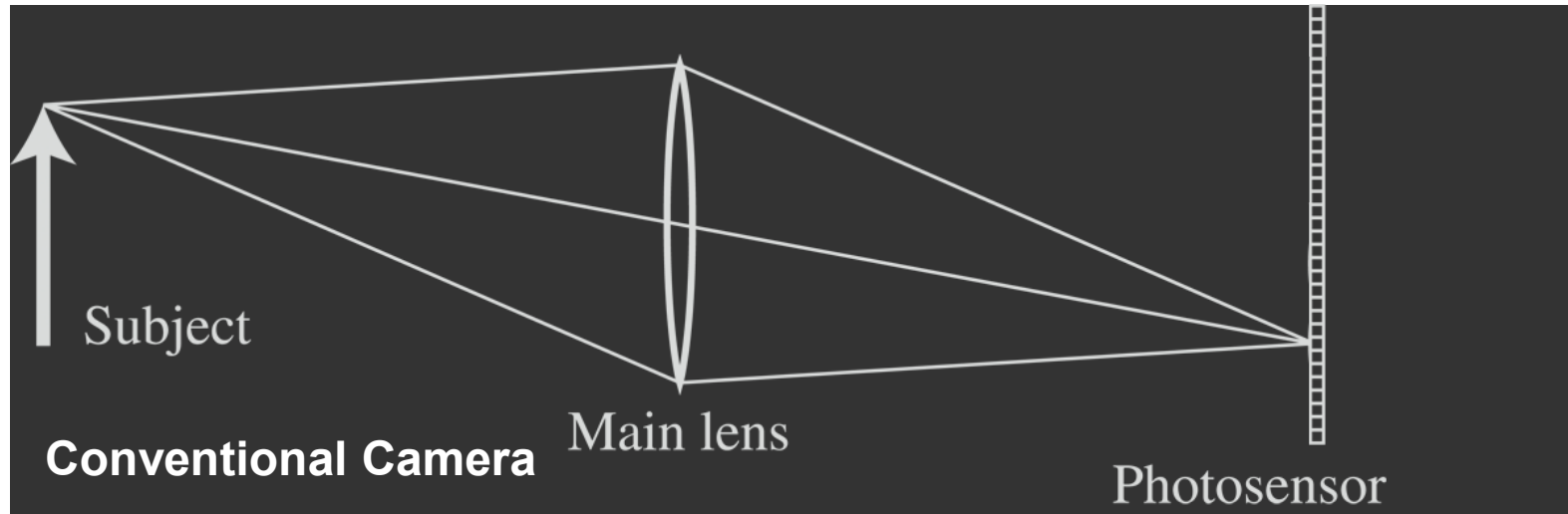
- Add a pinhole
  - ✓ Pixels correspond to small range of orientations at the camera center, instead of all gathered light at one position
  - ✗ Much less light hits sensor
- Add a lens
  - ✓ More light hits sensor
  - ✗ Limited depth of field
  - ✗ Chromatic aberration
- Add a shutter
  - Capture average intensity at a particular range of times
- Increase sensor resolution
  - ✓ Each pixel represents a smaller range of orientations
  - ✗ Less light per pixel
- Controls: aperture size, focal length, shutter time

How else can we design cameras?

What do they sacrifice/gain?

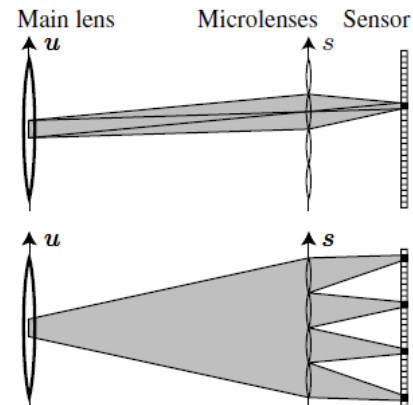
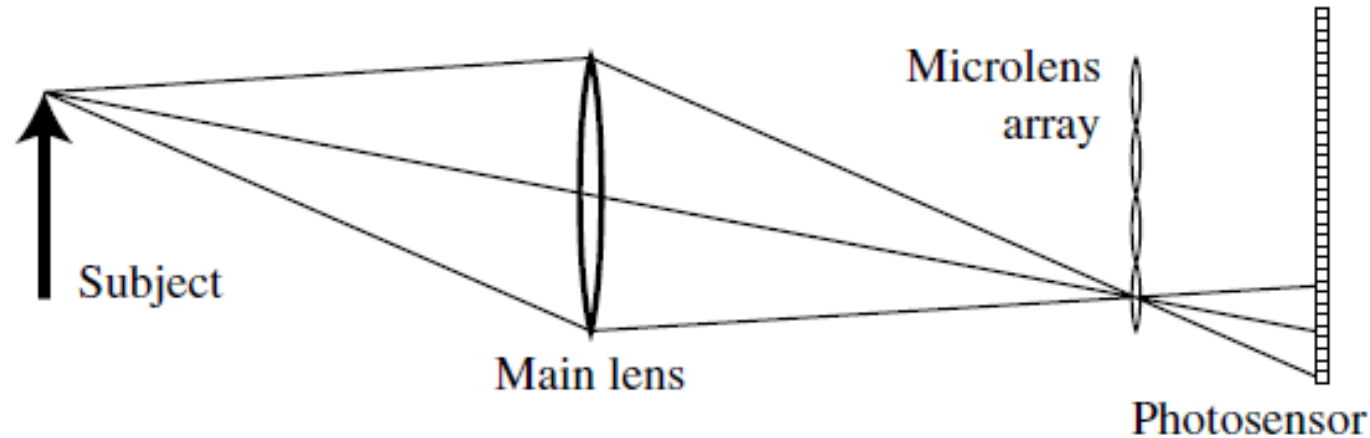


# 1. Light Field Photography with “Plenoptic Camera”



# Light field photography

- Like replacing the human retina with an insect compound eye
- Records where light ray hits the lens



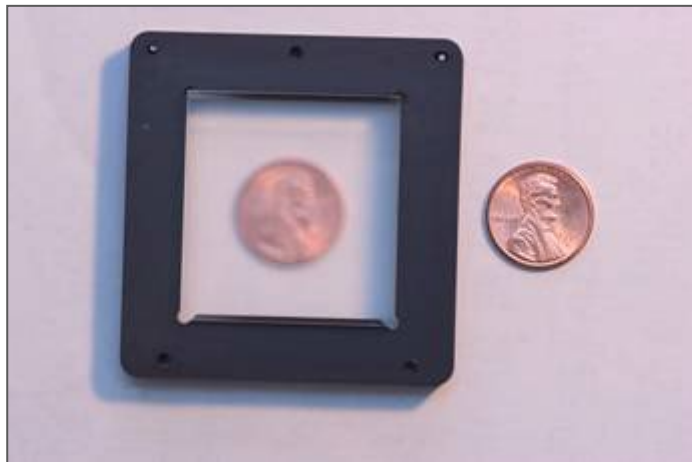
# Stanford Plenoptic Camera [Ng et al 2005]



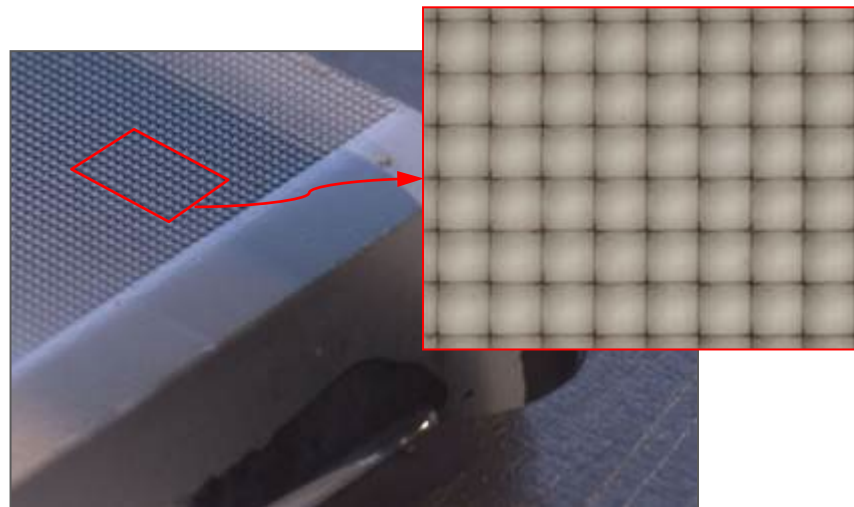
Contax medium format camera



Kodak 16-megapixel sensor



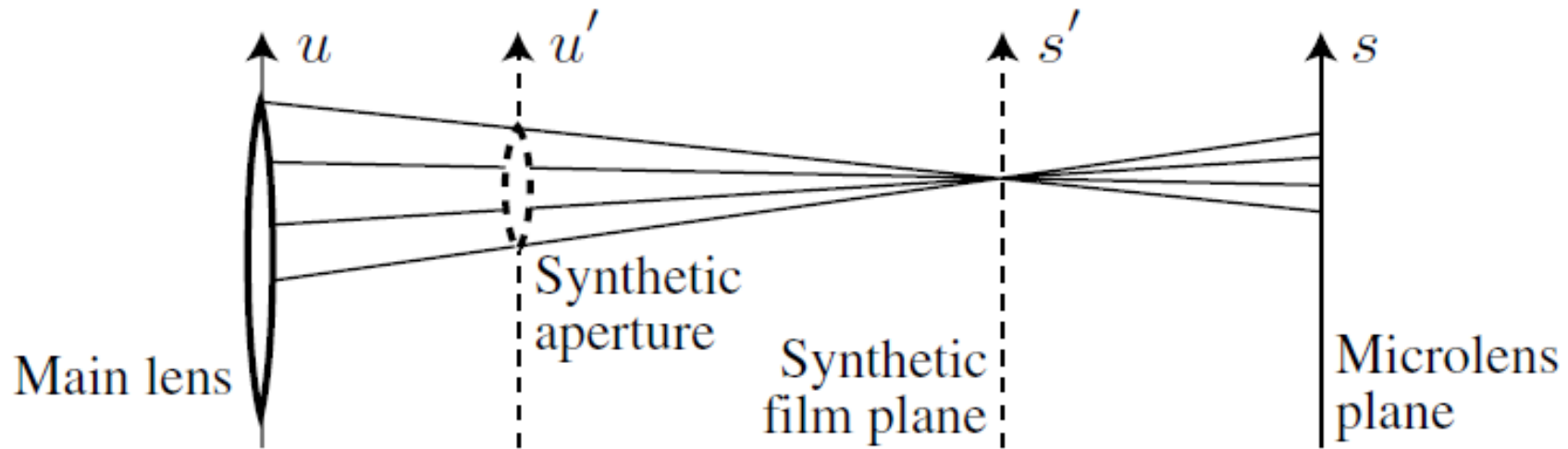
Adaptive Optics microlens array



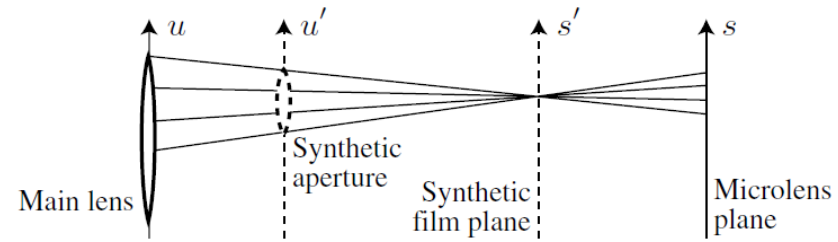
125μ square-sided microlenses

$$4000 \times 4000 \text{ pixels} \div 292 \times 292 \text{ lenses} = 14 \times 14 \text{ pixels per lens}$$

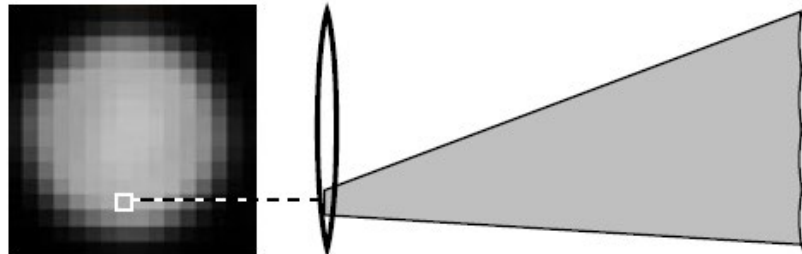
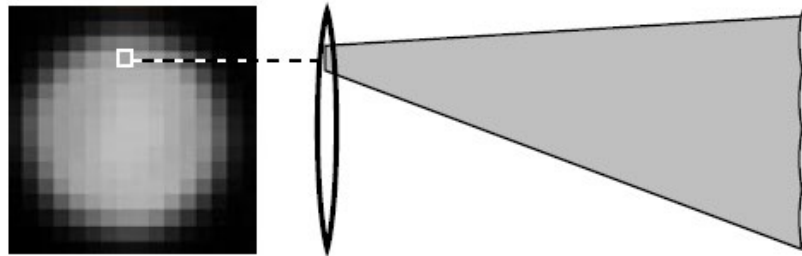
# Light field photography: applications



# Light field photography: applications



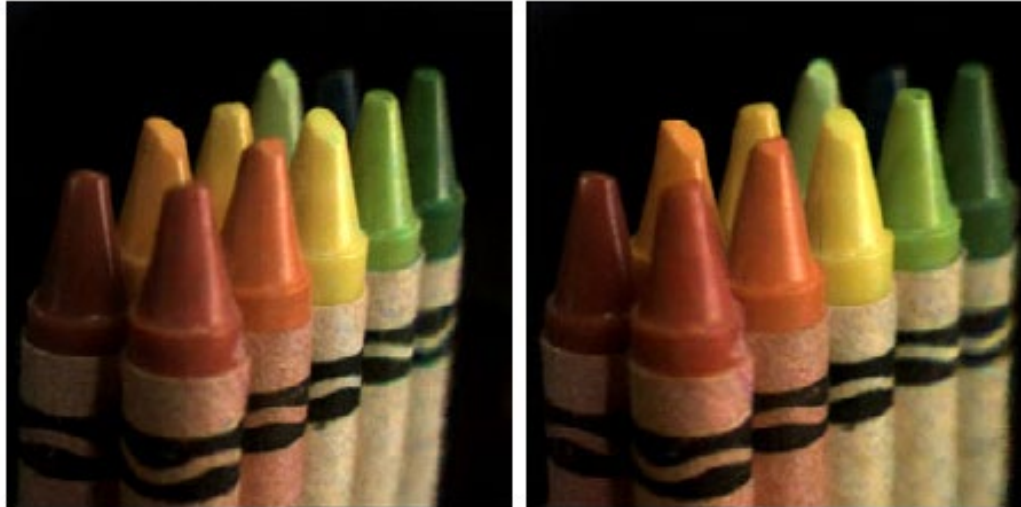
Change in  
viewpoint



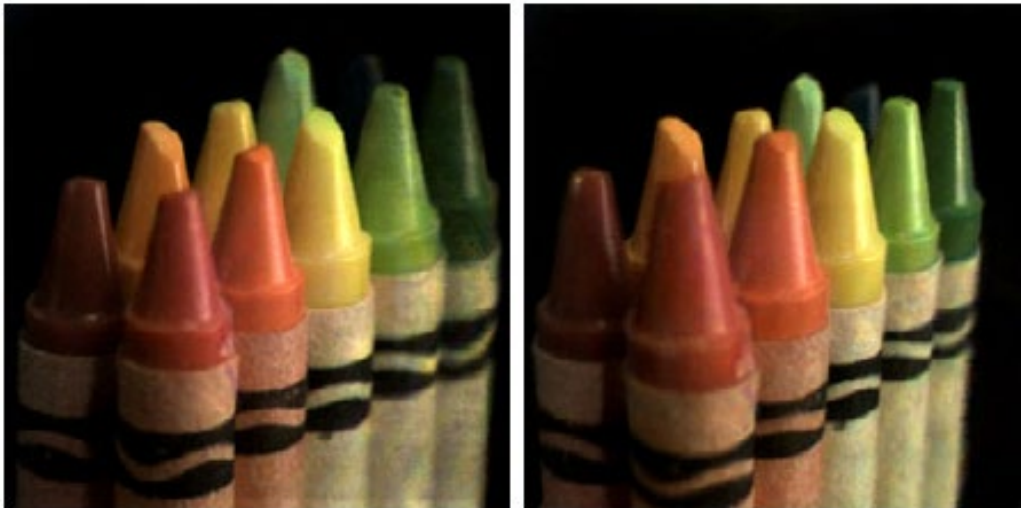
# Light field photography: applications

## Change in viewpoint

Lateral



Along Optical Axis





# Digital Refocusing



# Light field photography w/ microlenses

- We gain
  - Ability to refocus or increase depth of field
  - Ability for small viewpoint shifts
- What do we lose (vs. conventional camera)?

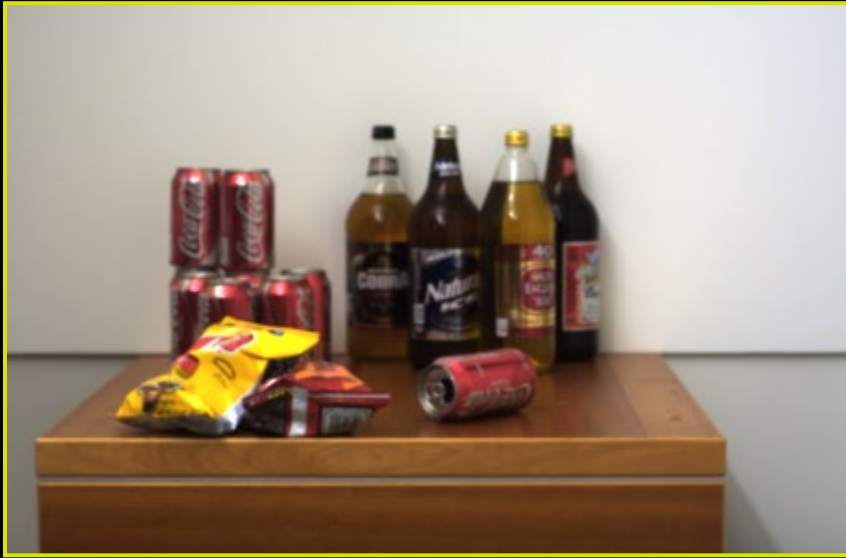
## 2. Coded apertures

# **Image and Depth from a Conventional Camera with a Coded Aperture**

**Anat Levin, Rob Fergus,  
Frédo Durand, William Freeman**

**MIT CSAIL**

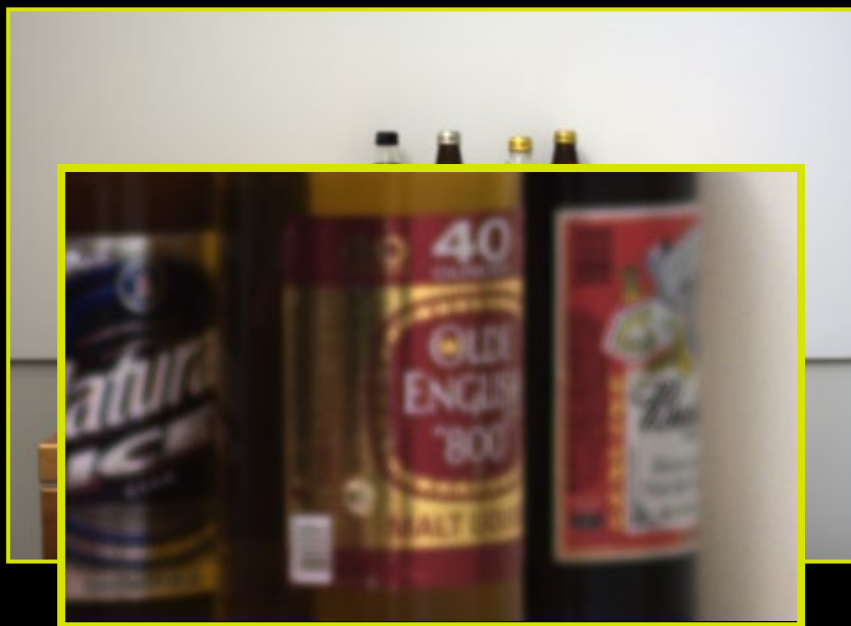
Single input image:



Output #1: Depth map



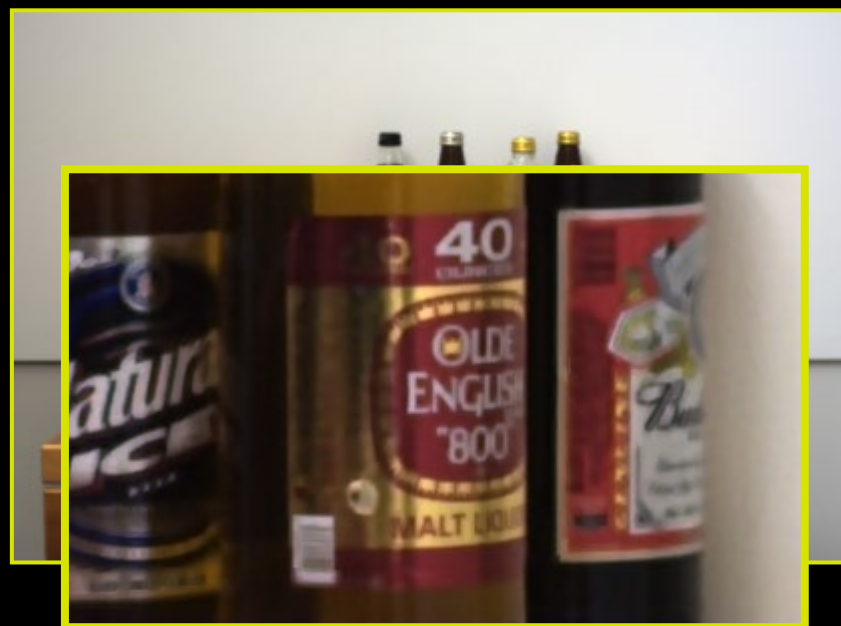
**Single input image:**



**Output #1: Depth map**



**Output #2: All-focused image**





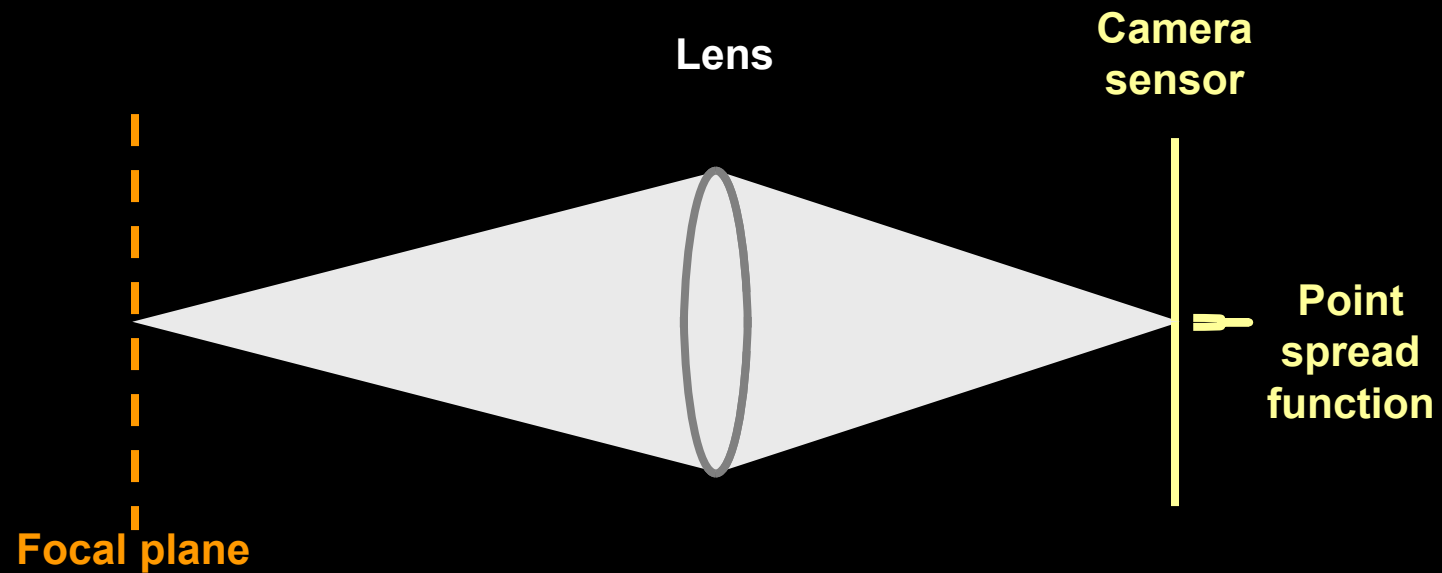
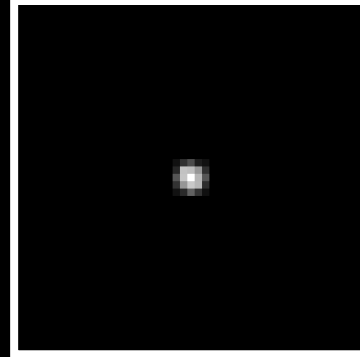
# Lens and defocus

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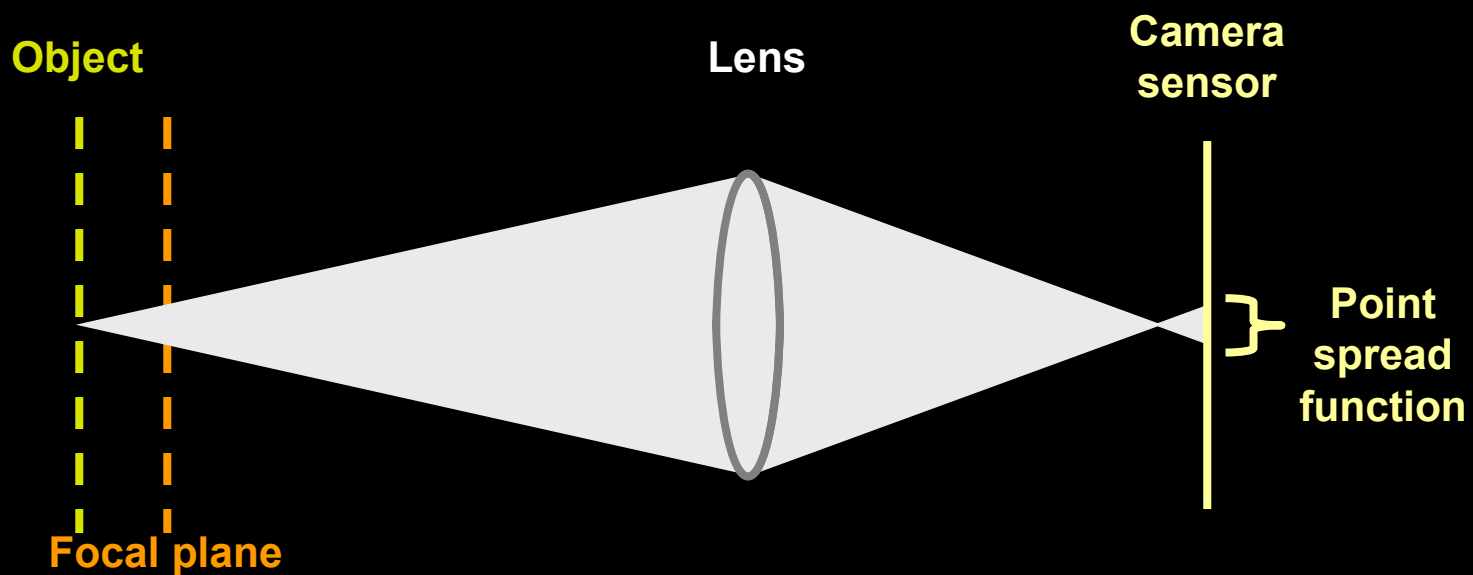
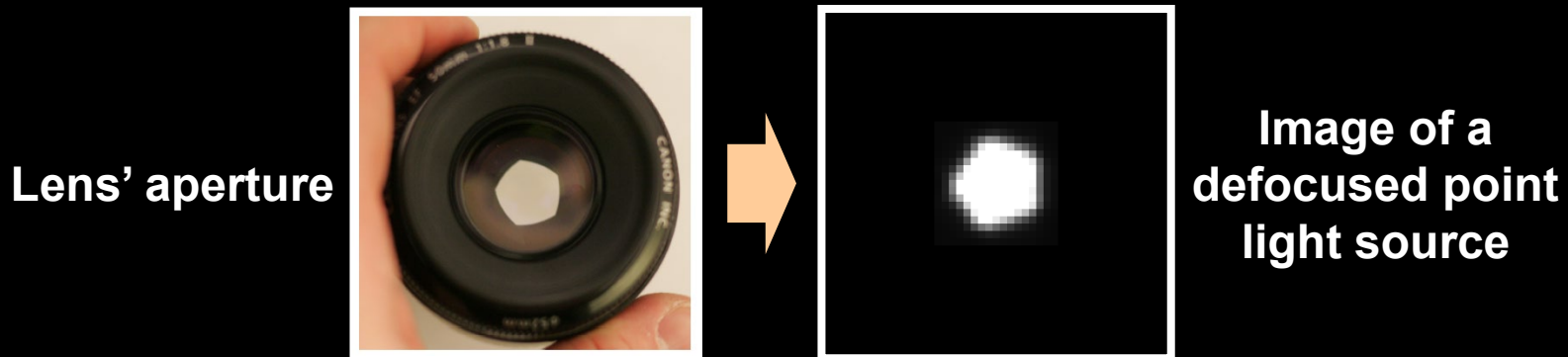
Lens' aperture



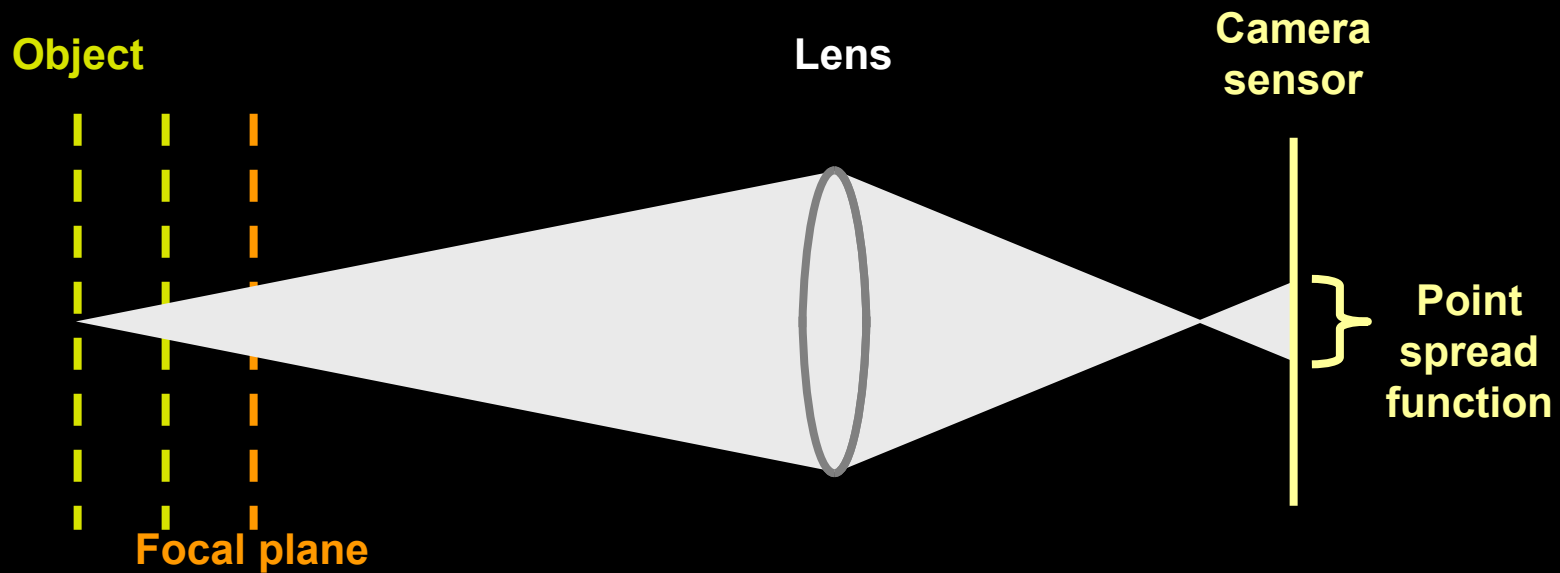
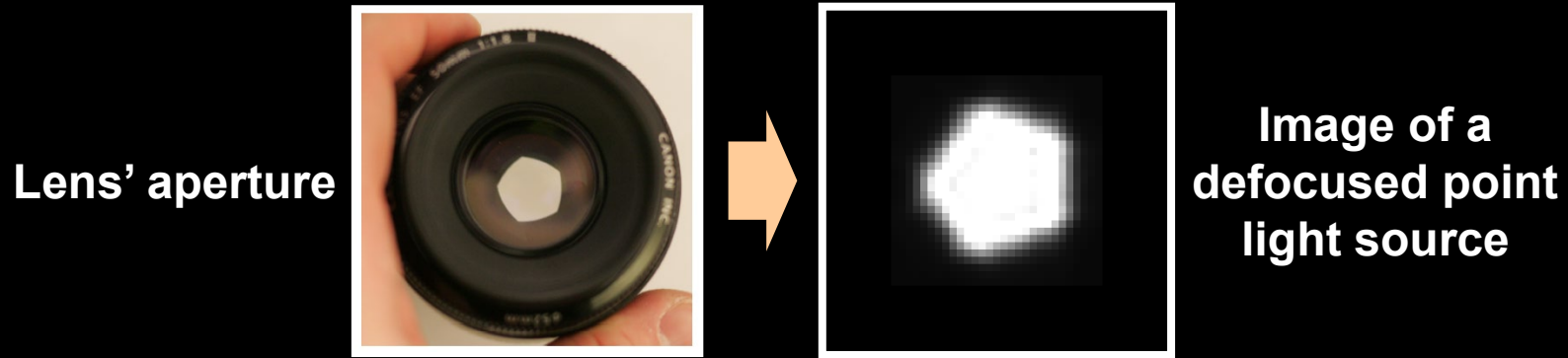
Image of a point light source



# Lens and defocus



# Lens and defocus



# Lens and defocus

Lens' aperture

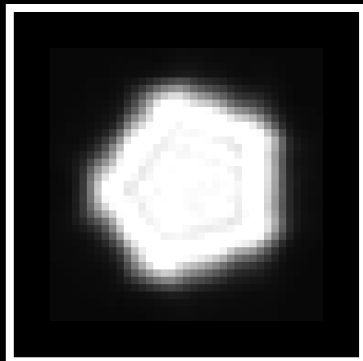
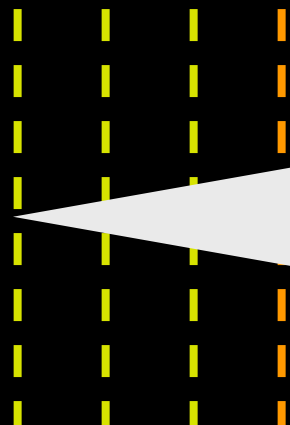


Image of a defocused point light source

Object

Lens

Camera sensor



Focal plane



Point spread function

# Lens and defocus

Lens' aperture

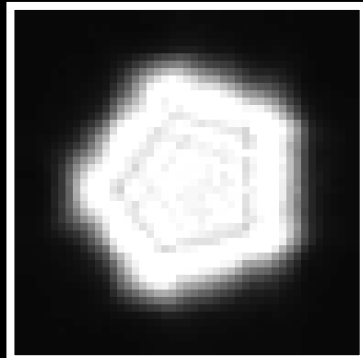
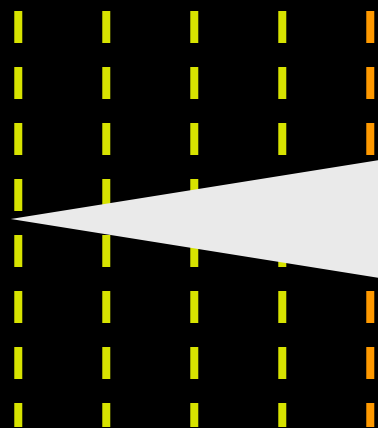


Image of a defocused point light source

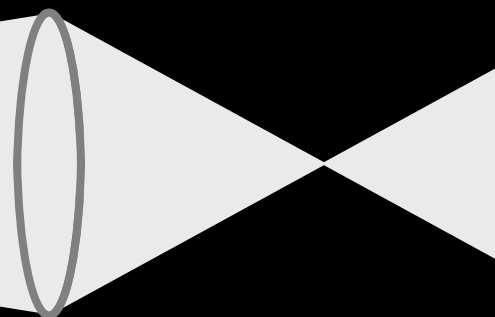
Object

Lens

Camera sensor



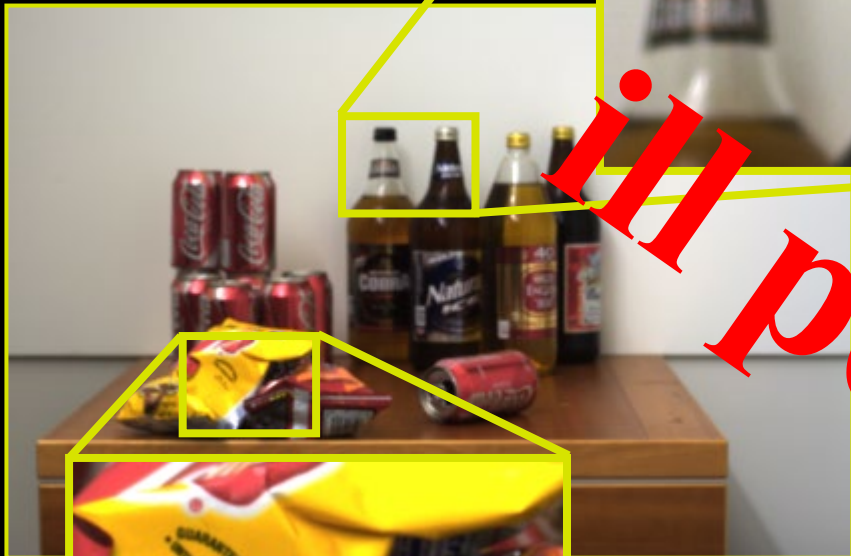
Focal plane



Point spread function

# Depth and defocus

Out of focus



In focus

*ill posed*



**Depth from defocus:**

Infer depth by analyzing local scale of defocus blur



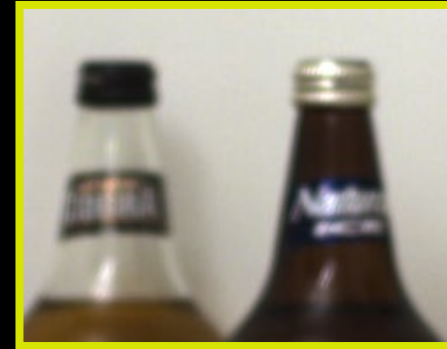
# Challenges

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- Hard to discriminate a smooth scene from defocus blur

?

Out of focus



- Hard to undo defocus blur



Input



Ringing with conventional  
deblurring algorithm

# Key ideas

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- **Exploit prior on natural images**

- Improve deconvolution
- Improve depth discrimination



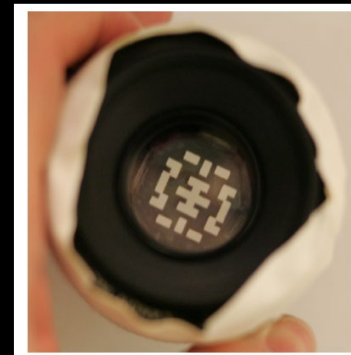
Natural



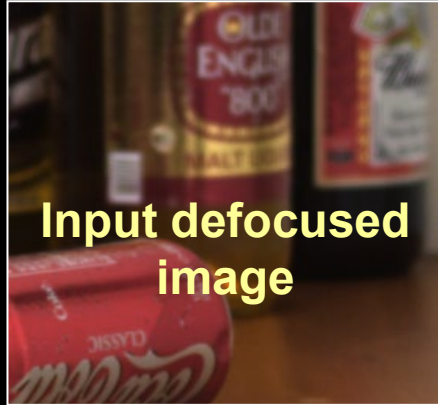
Unnatural

- **Coded aperture (mask inside lens)**

- make defocus patterns different from natural images and easier to discriminate



# Defocus as local convolution



$$y = f_k \otimes x$$

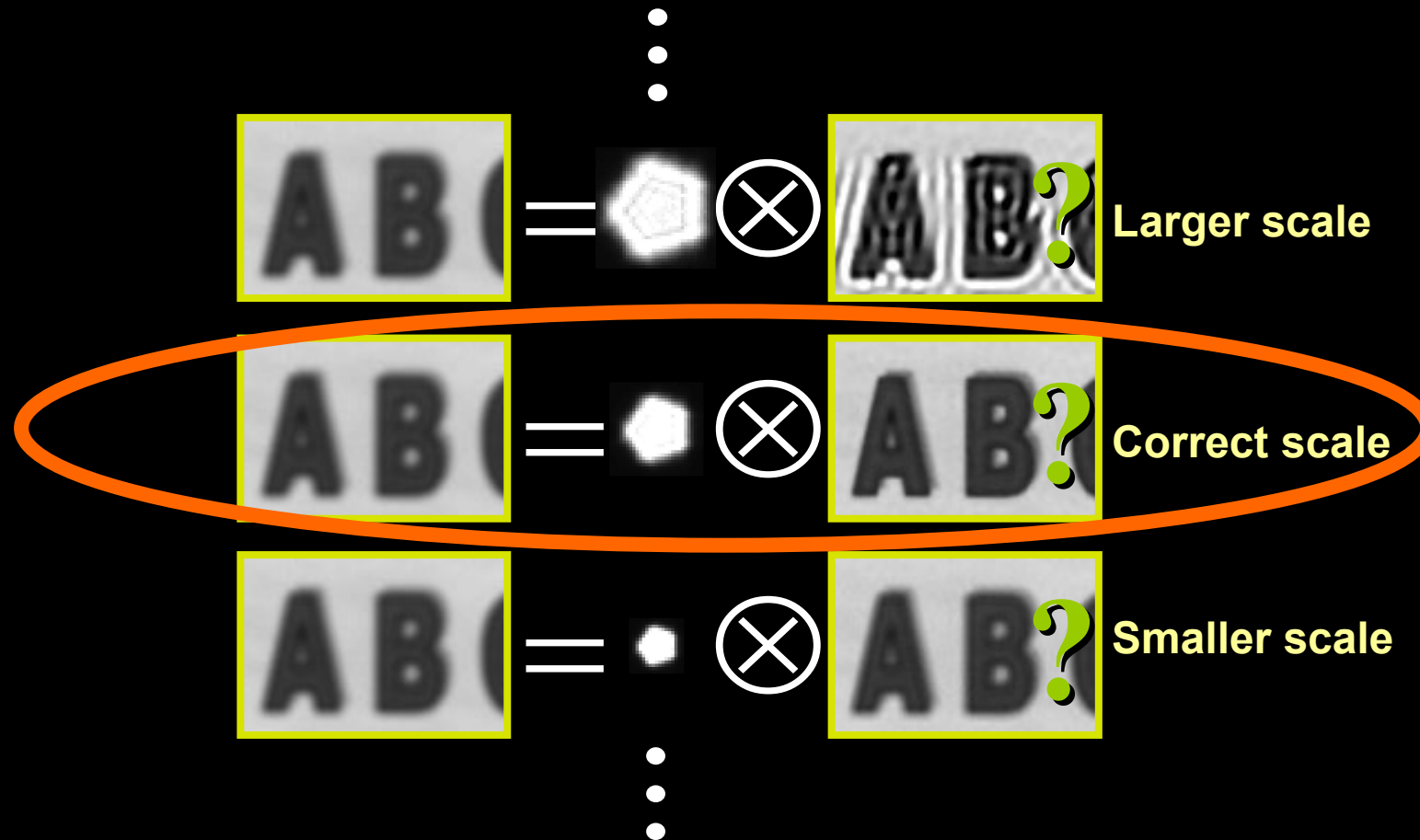
Local sub-window      Calibrated blur kernels at depth  $k$       Sharp sub-window



# Overview

---

Try deconvolving local input windows with different scaled filters:



Somehow: select best scale.

# Challenges

- Hard to deconvolve even when kernel is known



Input



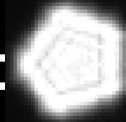
Ringing with the traditional Richardson-Lucy deconvolution algorithm

- Hard to identify correct scale:

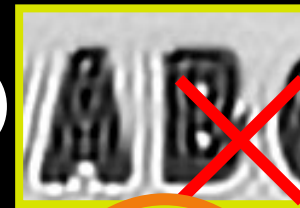
?



=



⊗

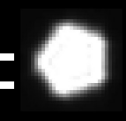


Larger scale

?



=



⊗



Correct scale

?



=



⊗

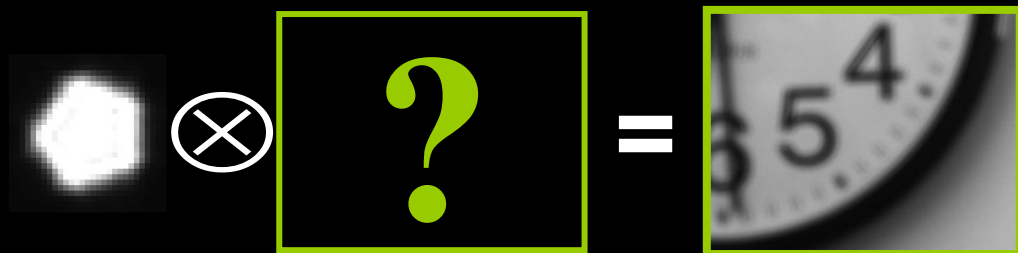


Smaller scale

# Deconvolution is ill posed

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$$f \otimes x = y$$

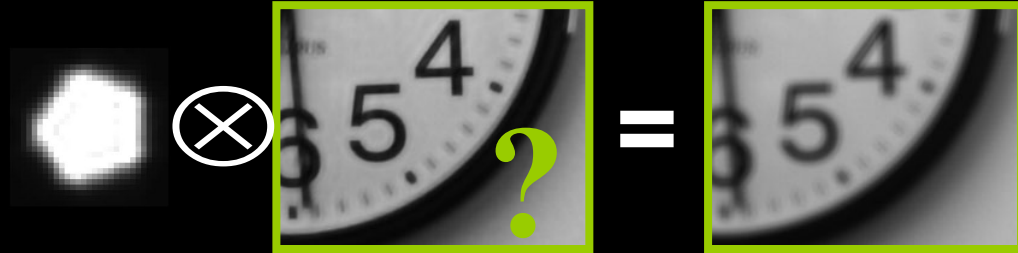


# Deconvolution is ill posed

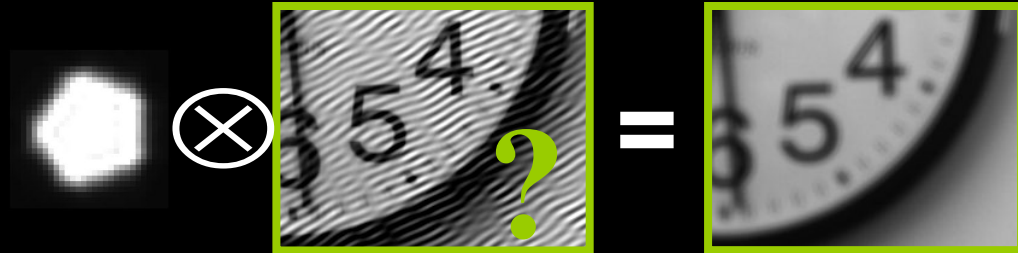
---

$$f \otimes x = y$$

Solution 1:



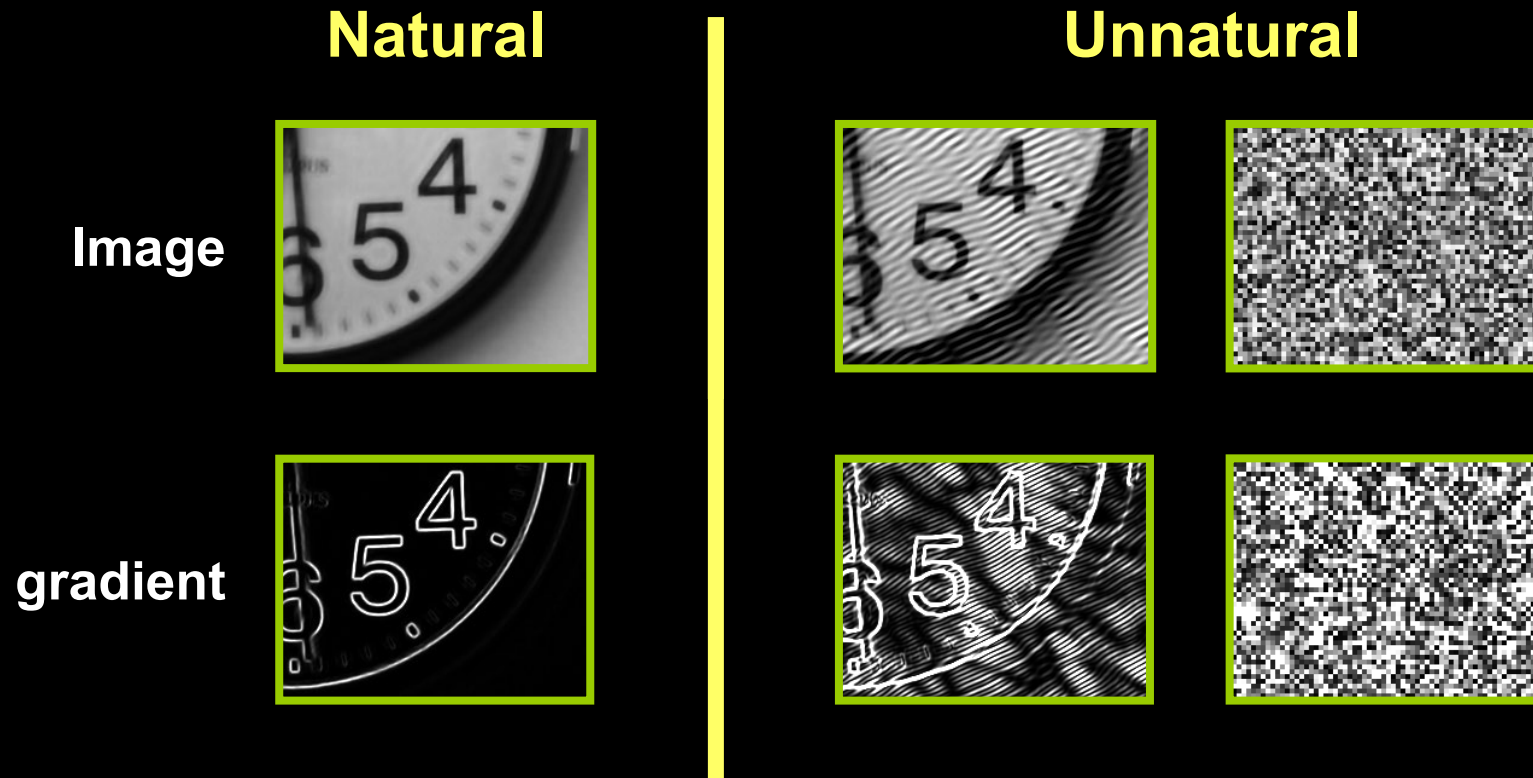
Solution 2:



# Idea 1: Natural images prior

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## What makes images special?



Natural images have sparse gradients

➡ put a penalty on gradients



# Deconvolution with prior

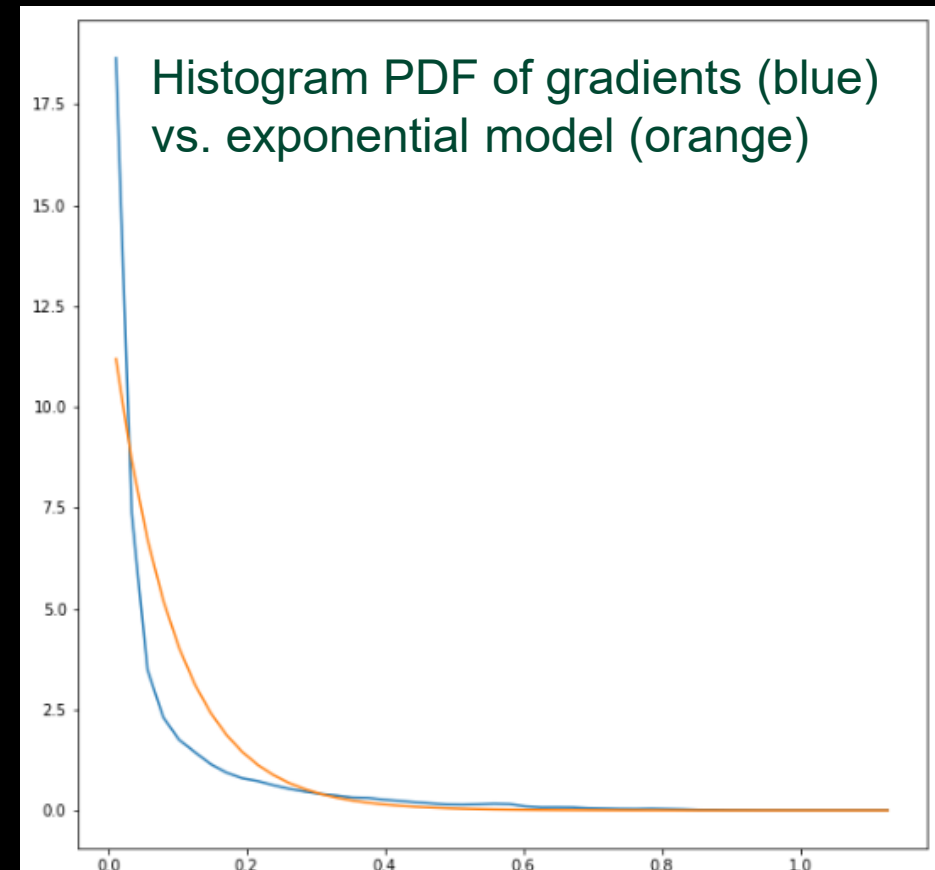
$$x = \arg \min \underbrace{|f \otimes x - y|^2}_{\text{Convolution error}} + \lambda \underbrace{\sum_i \rho(\nabla x_i)}_{\text{Derivatives prior}}$$

$$\left| \begin{array}{c} \text{Kernel} \otimes \text{Input} - \text{Output} \end{array} \right|^2 + \begin{array}{c} \text{Derivatives prior} \\ \text{Low} \end{array}$$


Equal convolution error

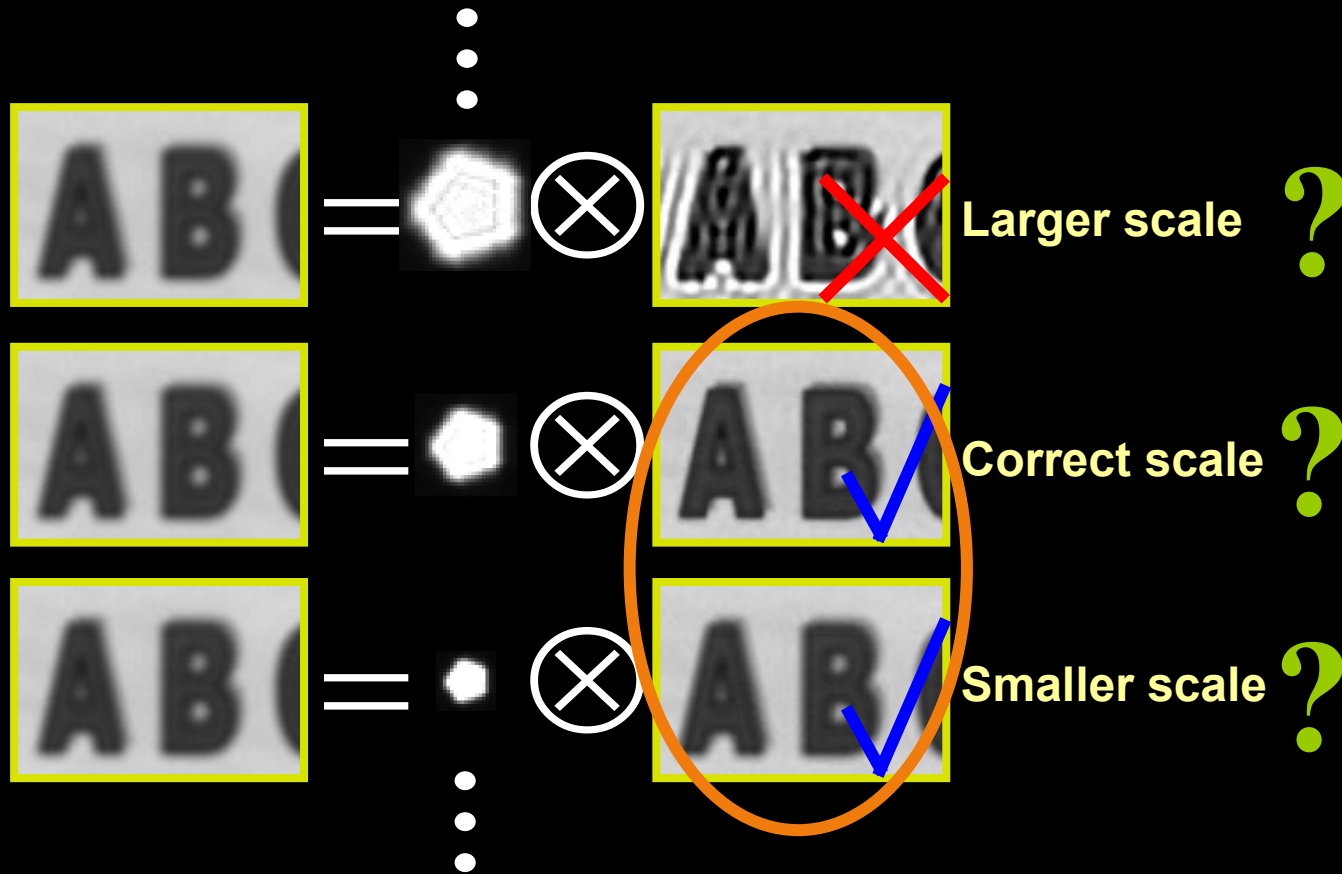
$$\left| \begin{array}{c} \text{Kernel} \otimes \text{Input} - \text{Output} \end{array} \right|^2 + \begin{array}{c} \text{Derivatives prior} \\ \text{High} \end{array}$$


# Example of gradient statistics ( $\sim$ exponential pdf)



# Recall: Overview

Try deconvolving local input windows with different scaled filters:



Somehow: select best scale.

Challenge: smaller scale not so different than correct

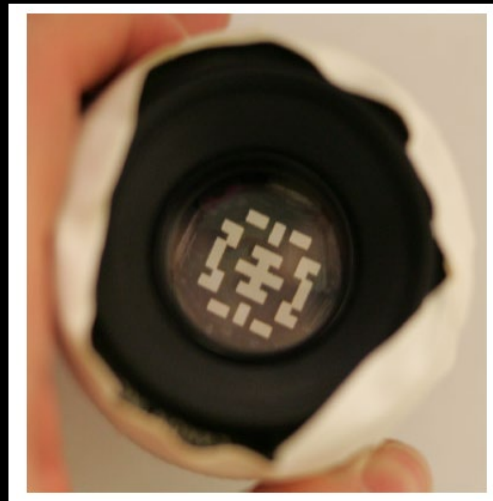
# Idea 2: Coded Aperture

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- **Mask (code) in aperture plane**
  - make defocus patterns different from natural images and easier to discriminate



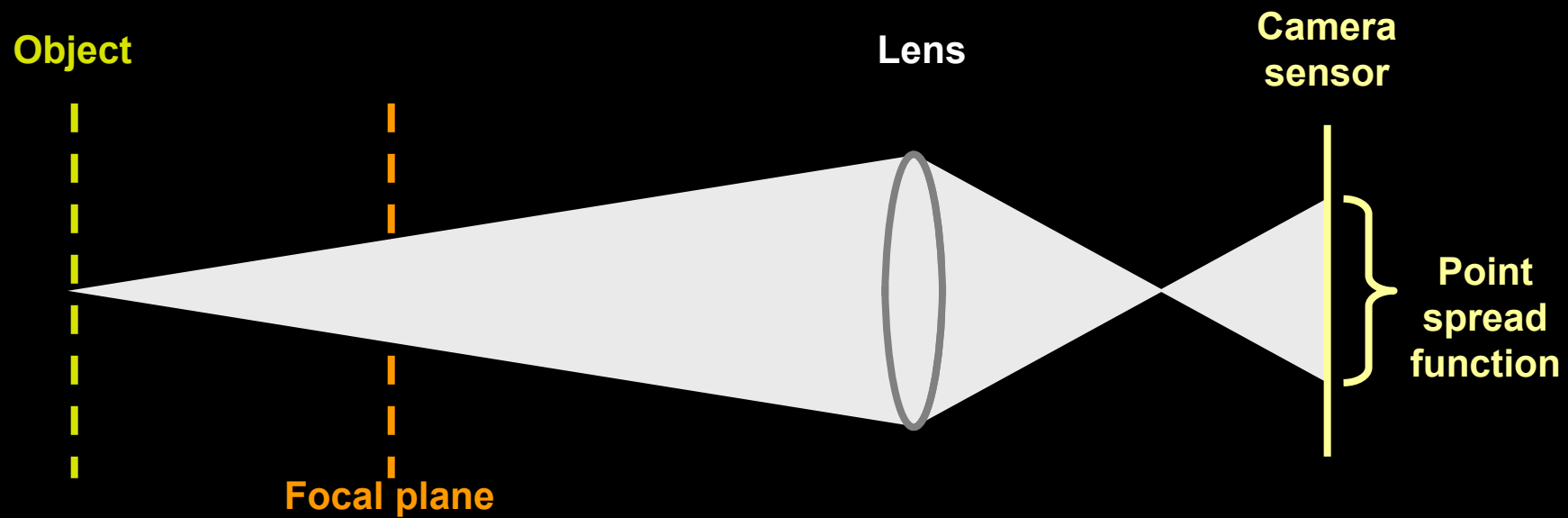
**Conventional  
aperture**



**Our coded  
aperture**

# Solution: lens with occluder

---



# Solution: lens with occluder

---

Aperture pattern

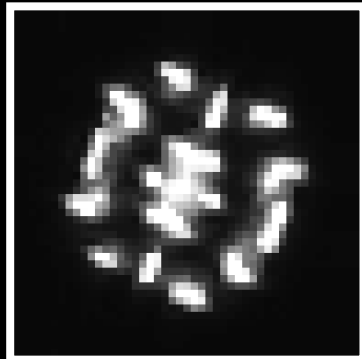
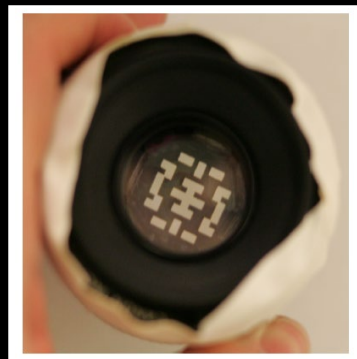
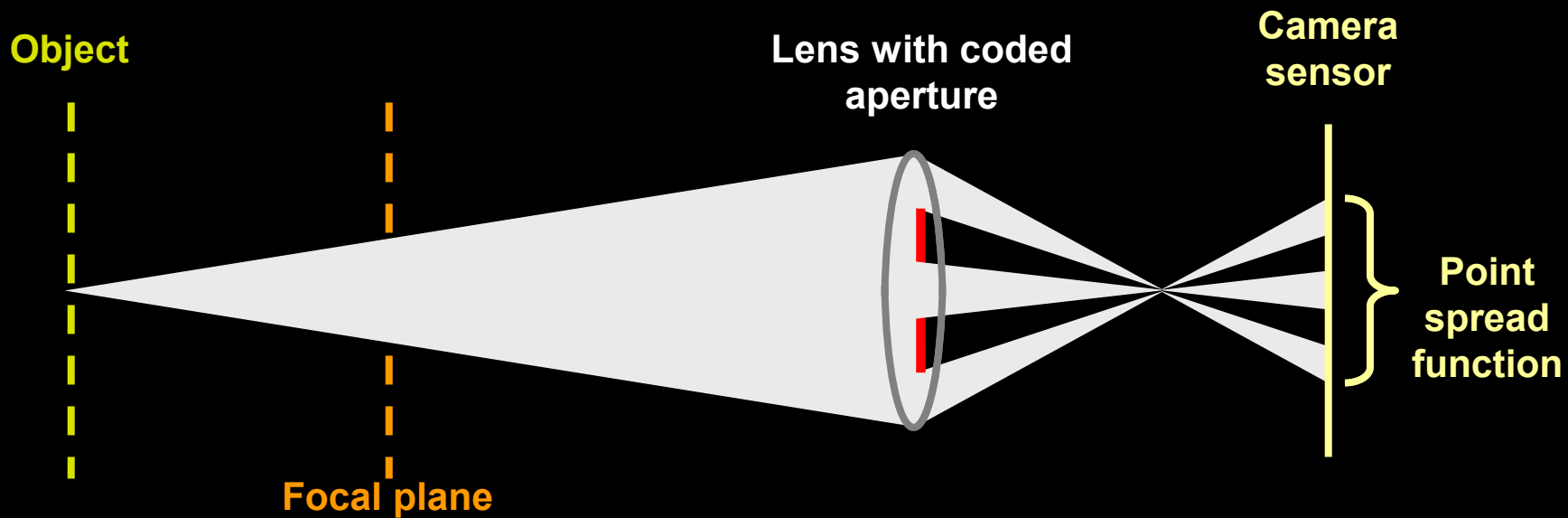
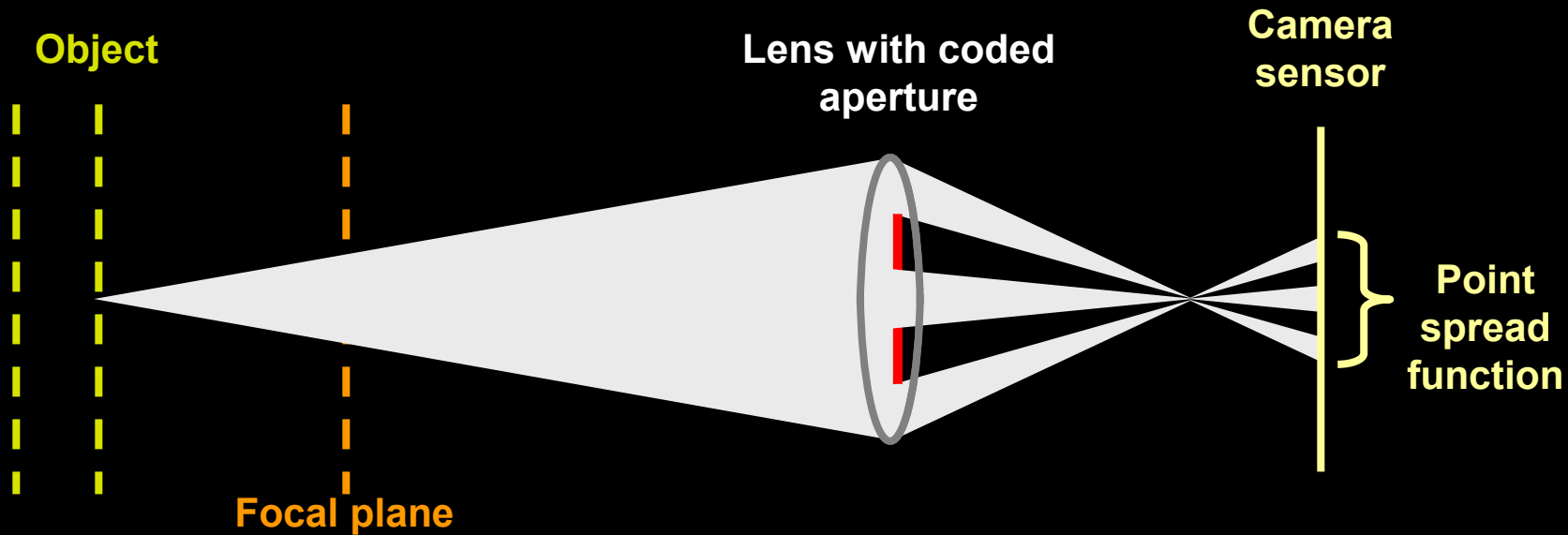
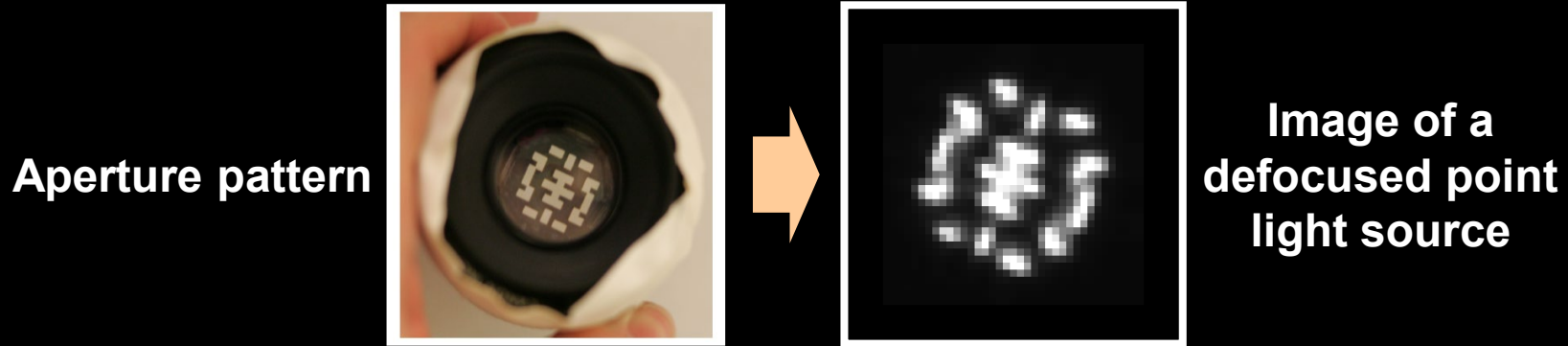


Image of a defocused point light source



# Solution: lens with occluder



# Solution: lens with occluder

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Aperture pattern

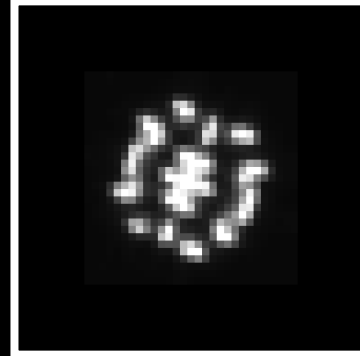
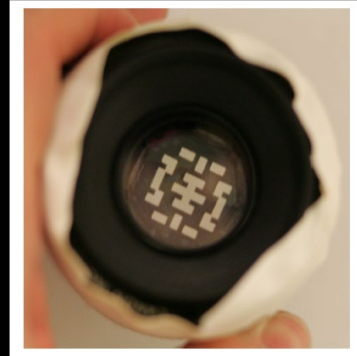
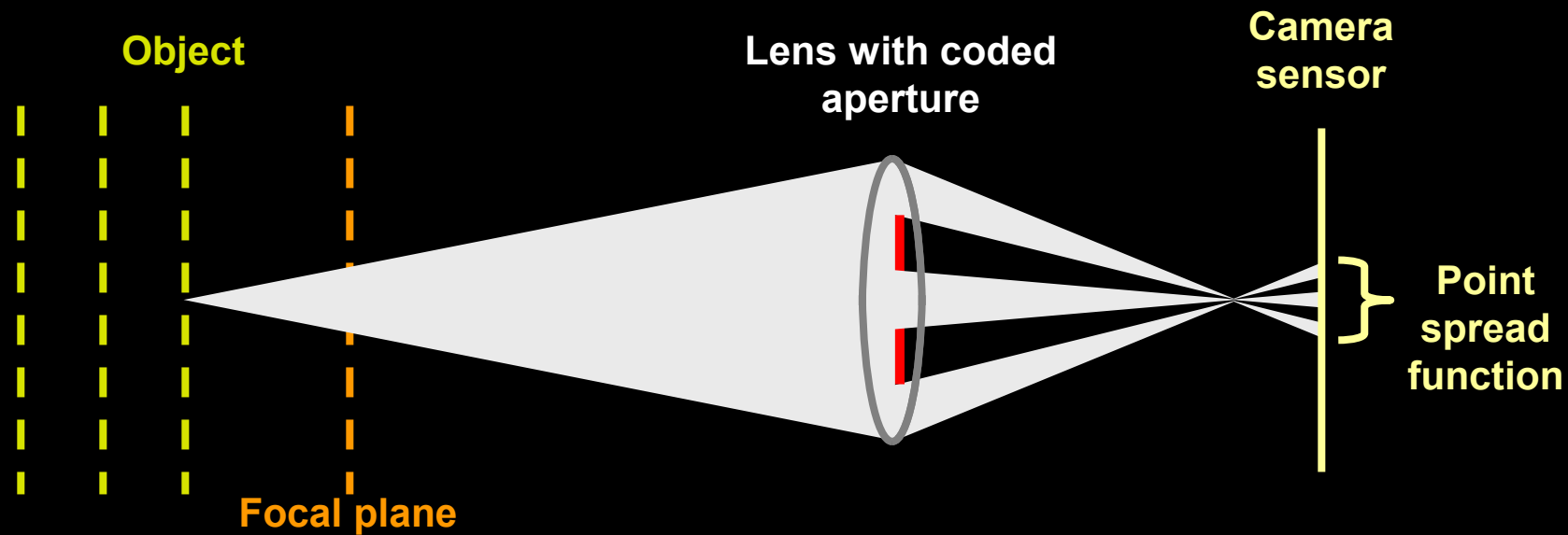


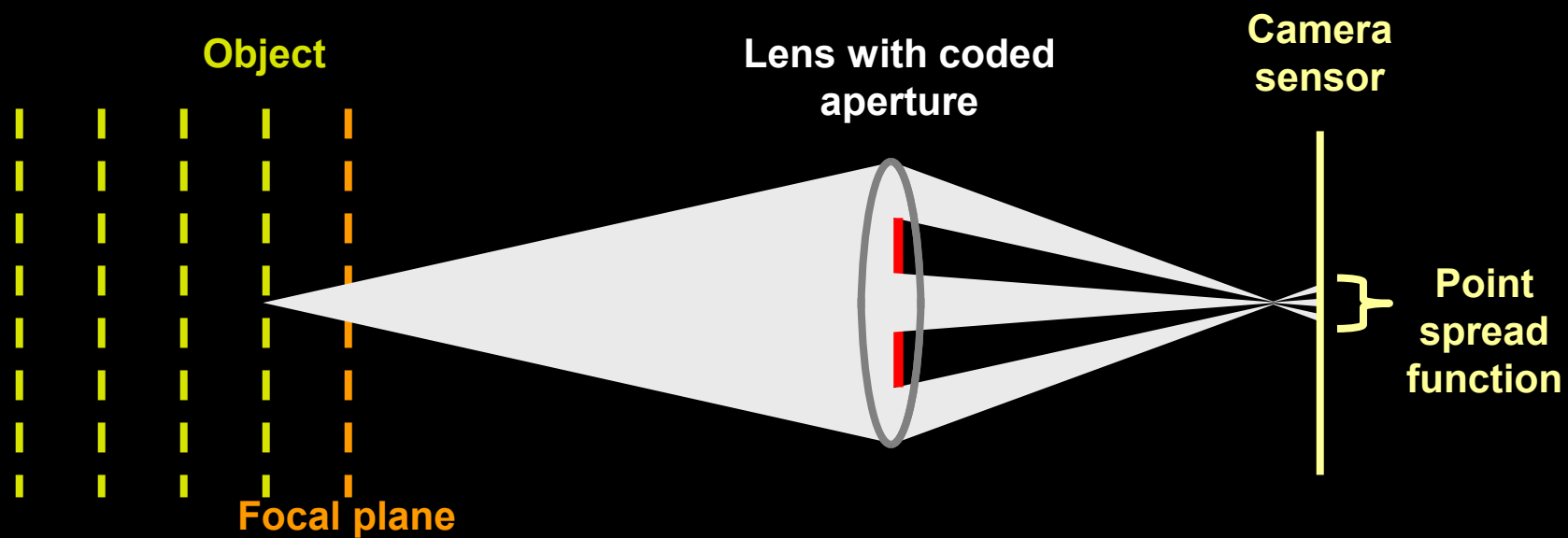
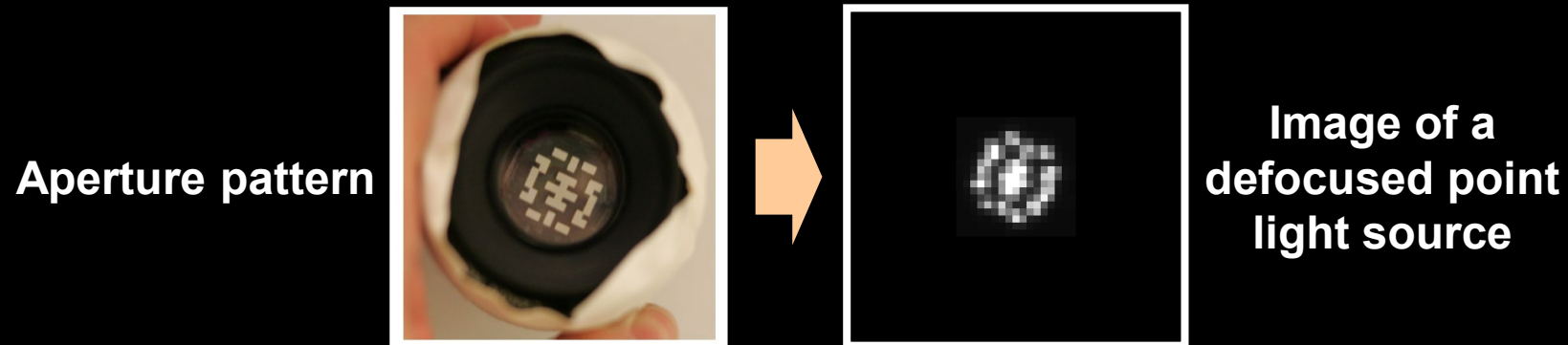
Image of a defocused point light source





# Solution: lens with occluder

---



# Solution: lens with occluder

---

Aperture pattern

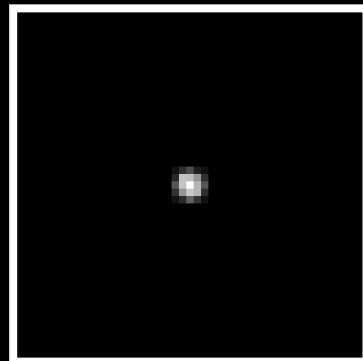
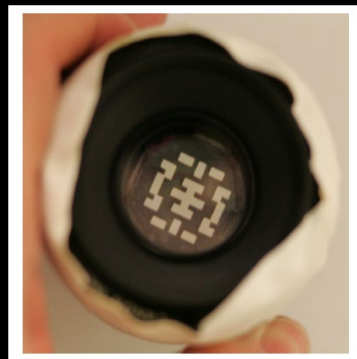
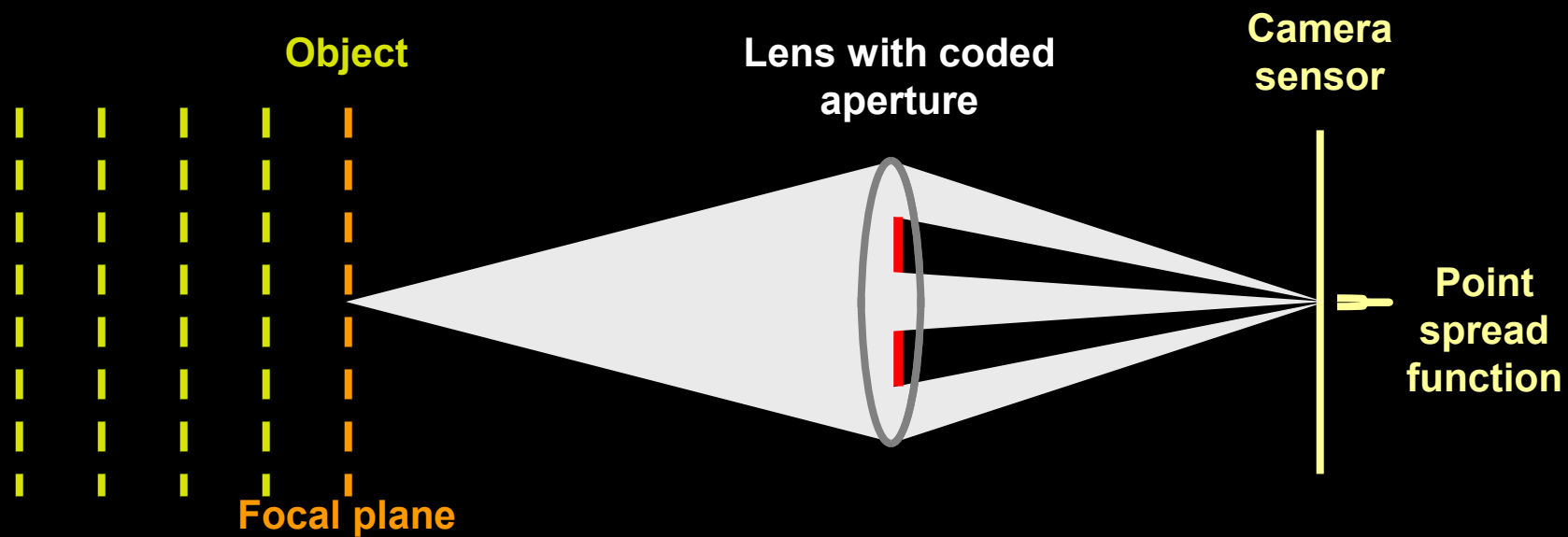
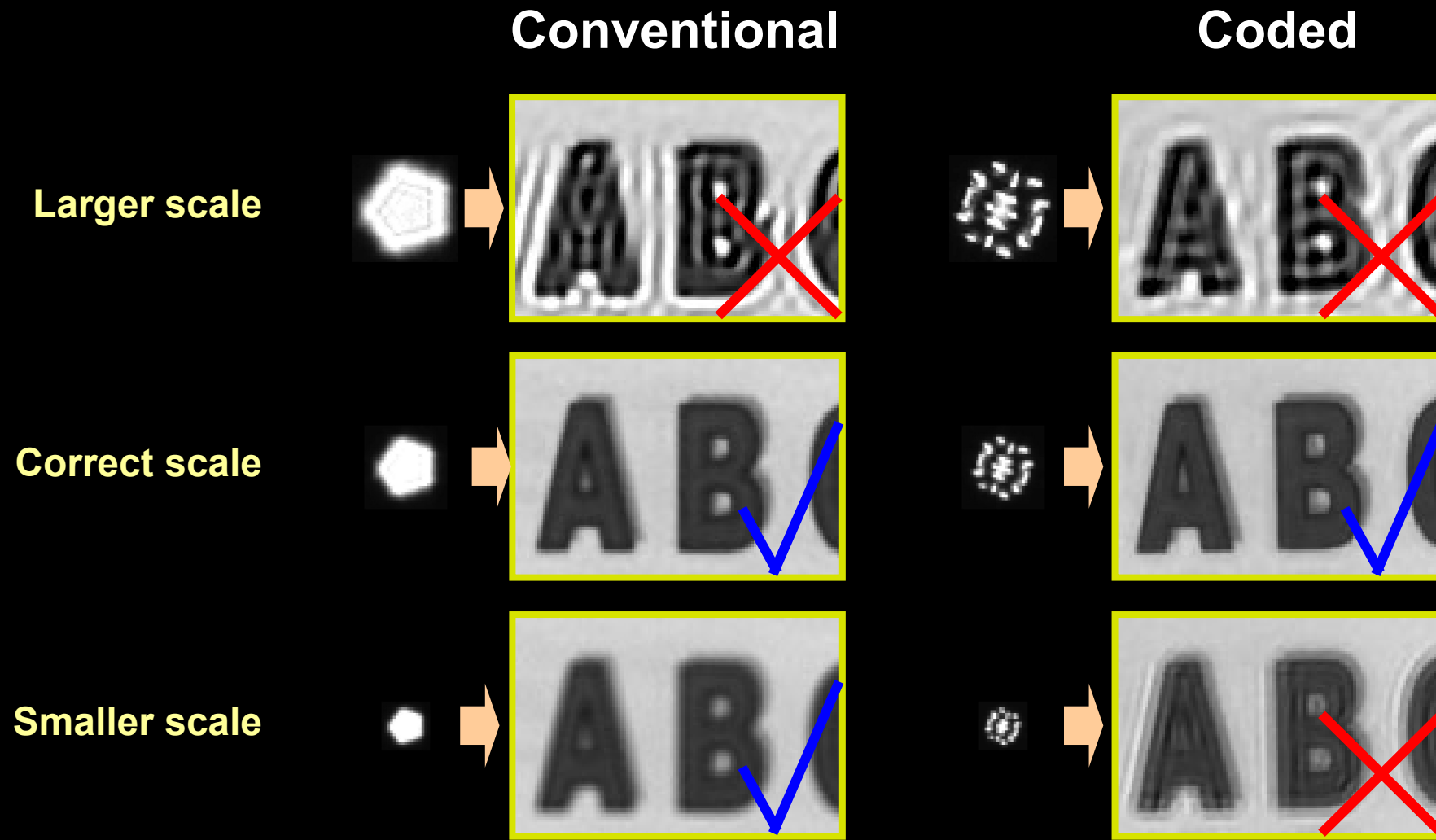


Image of a defocused point light source

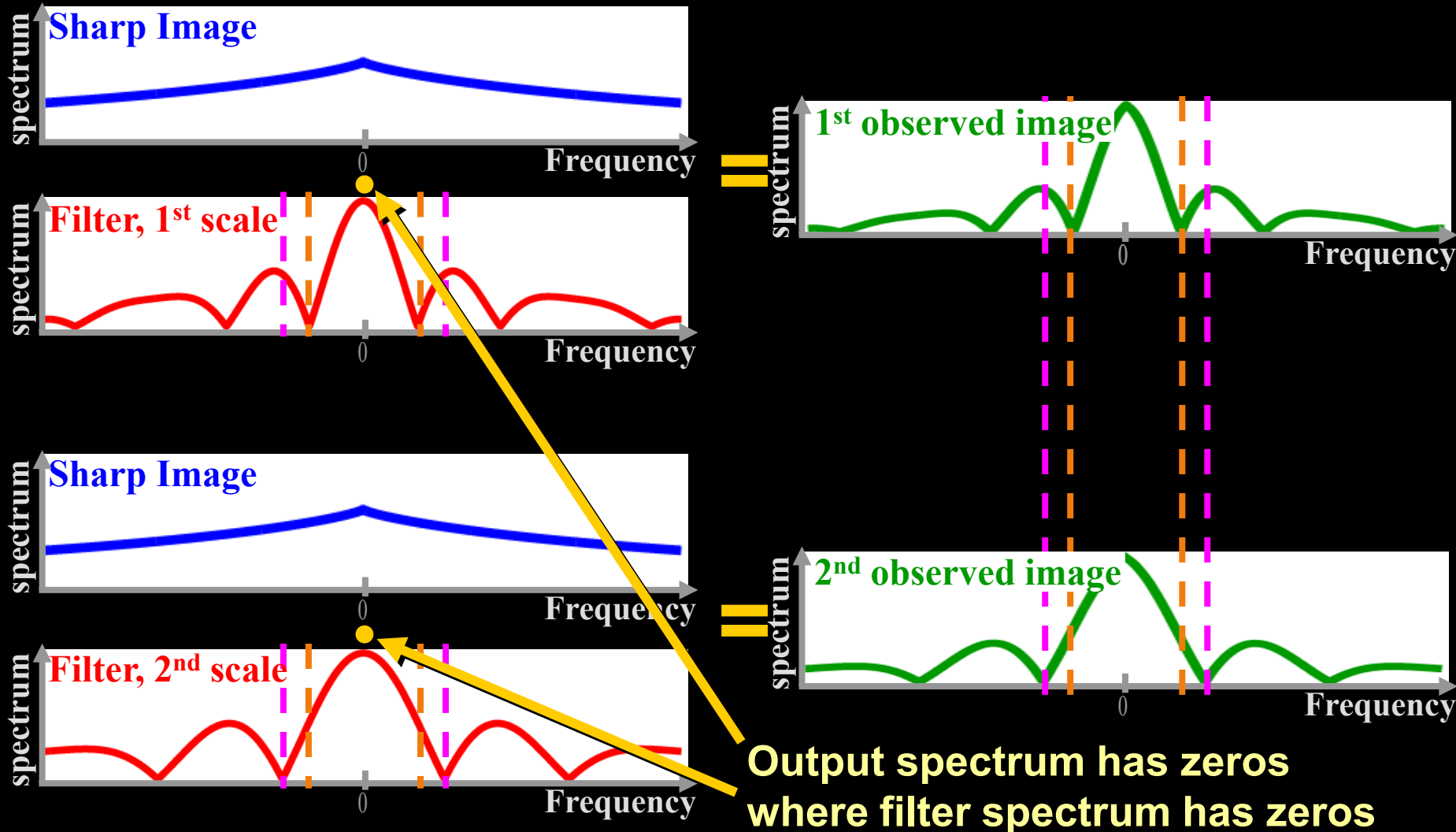


# Coded aperture reduces uncertainty in scale identification

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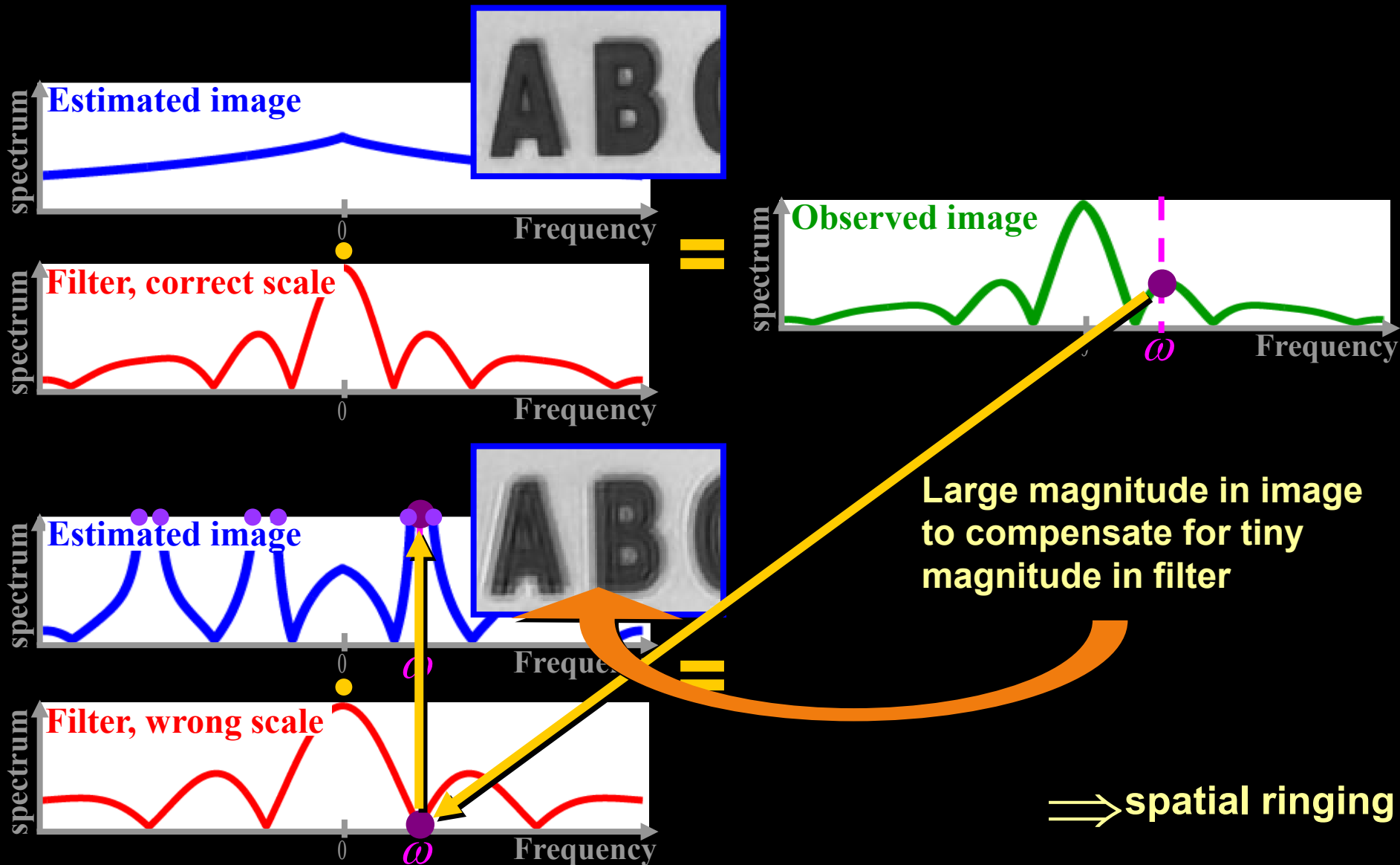


# Convolution- frequency domain representation



**Spatial convolution  $\Leftrightarrow$  frequency multiplication**

# Coded aperture: Scale estimation and division by zero

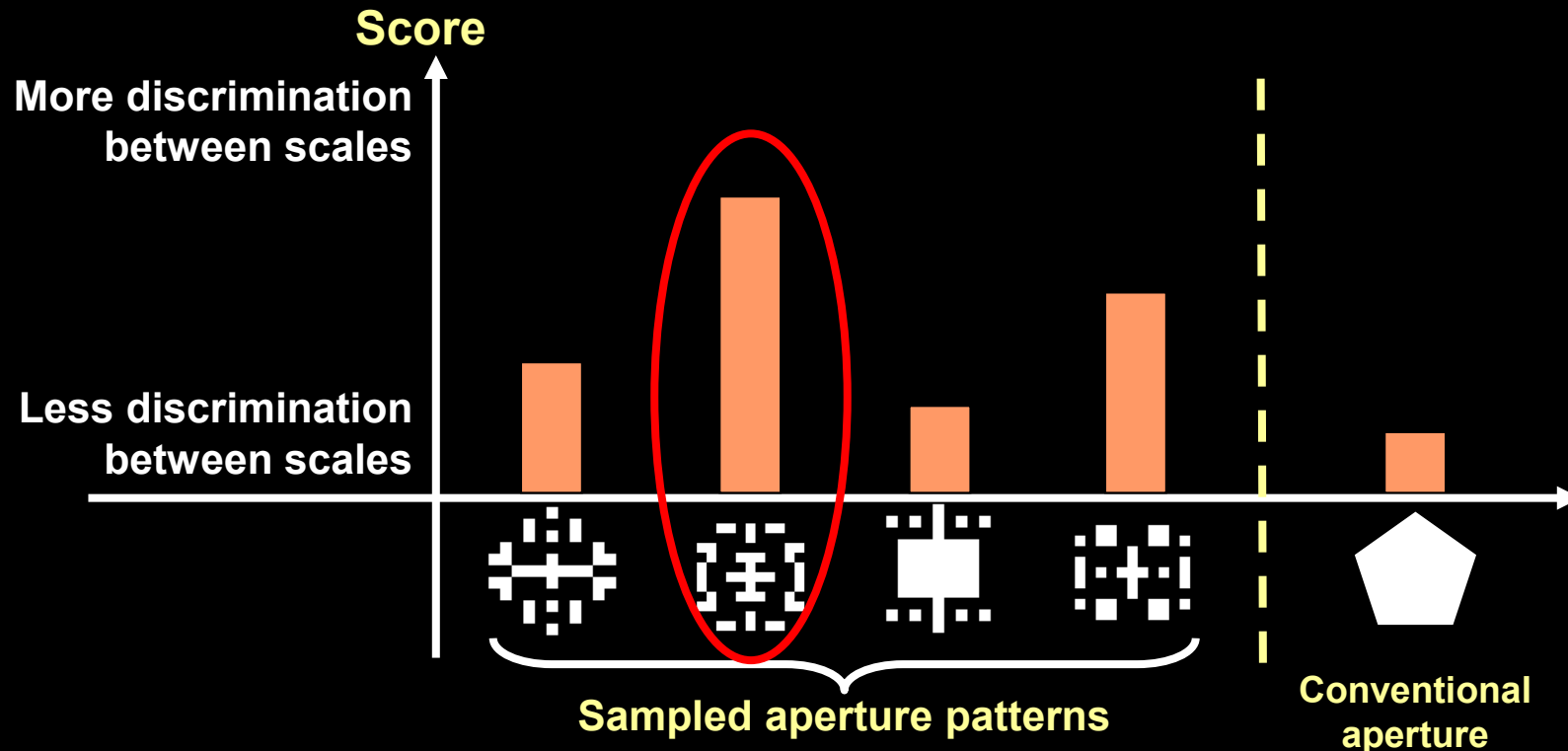




# Filter Design

Analytically search for a pattern maximizing discrimination between images at different defocus scales (*KL-divergence*)

Account for image prior and physical constraints



# Depth results

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# Regularizing depth estimation

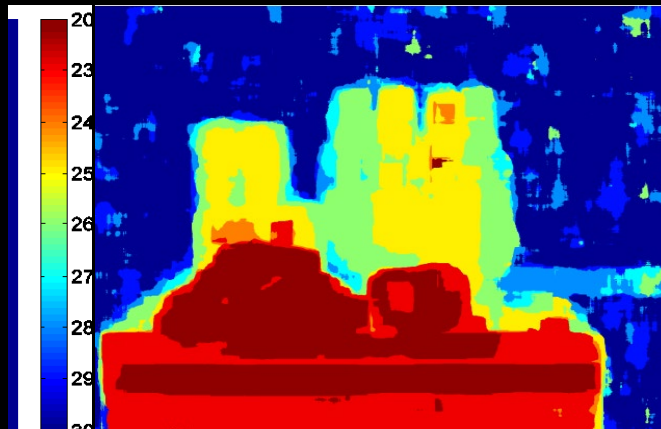
Try deblurring with 10 different aperture scales

$$x = \arg \min \underbrace{|f \otimes x - y|^2}_{\text{Convolution error}} + \lambda \underbrace{\sum_i \rho(\nabla x_i)}_{\text{Derivatives prior}}$$

Keep minimal error scale in each local window + regularization



Input



Local depth estimation



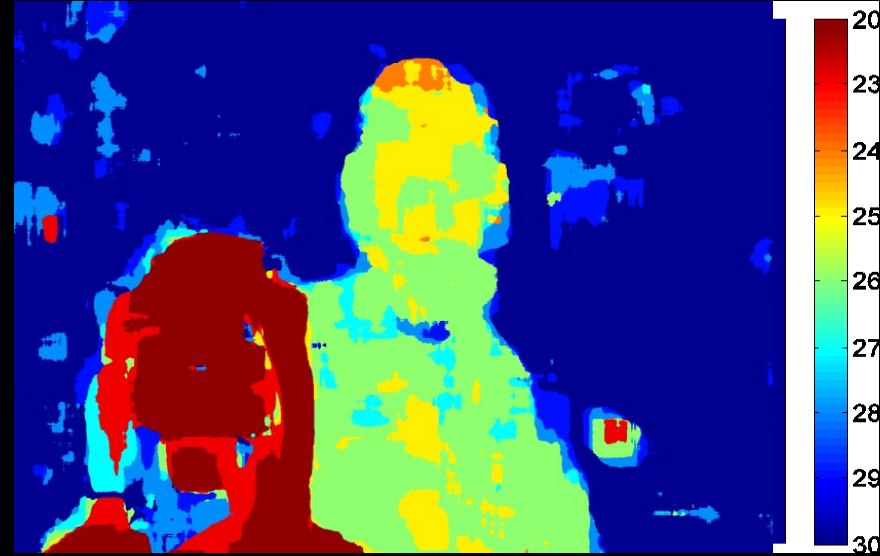
Regularized depth

# Regularizing depth estimation

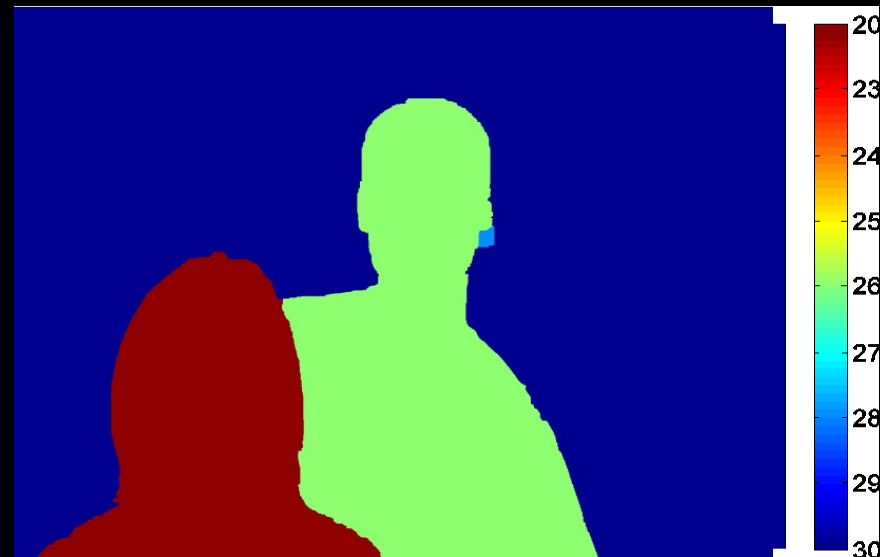
---



Input



Local depth estimation



Regularized depth

**All focused results**

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# Input





# All-focused (deconvolved)



# Close-up

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Original image



All-focus image



# Comparison- conventional aperture result

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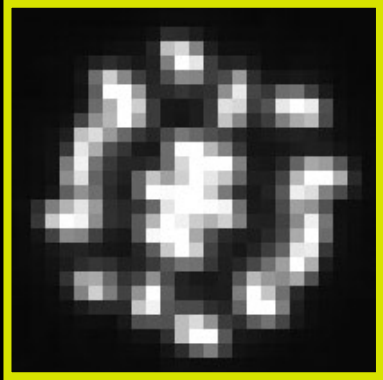
Ringing due to wrong scale estimation





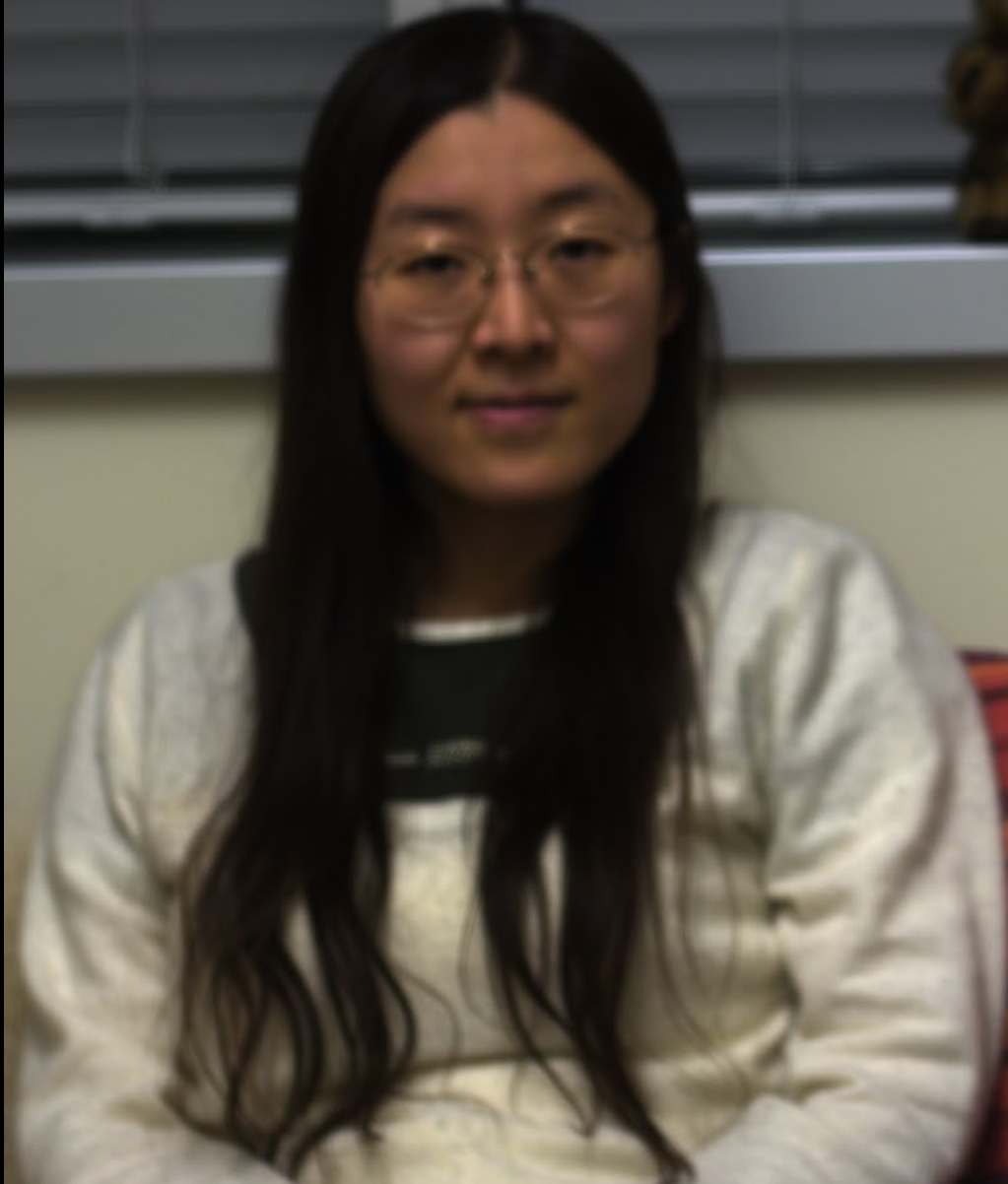
# Comparison- conventional aperture result

---





Input





**All-focused  
(deconvolved)**



# Close-up

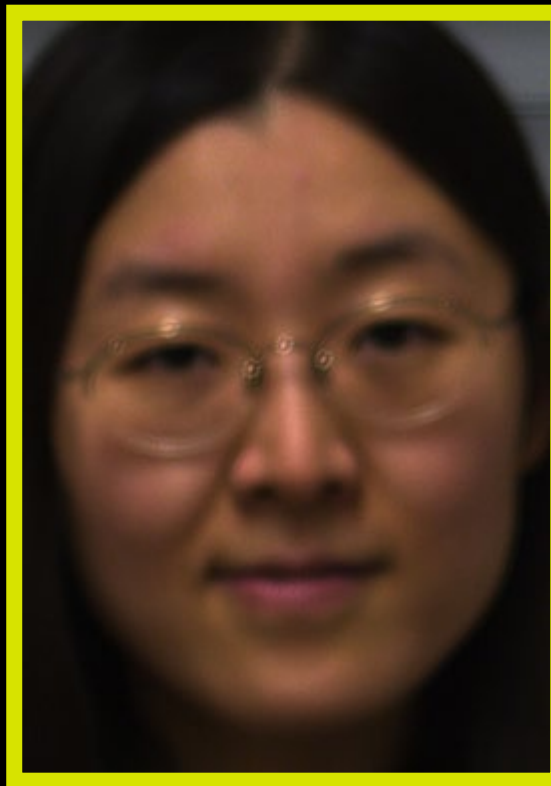
---



Original image



All-focus image



Naïve sharpening



# Application: Digital refocusing from a single image

---



# Application: Digital refocusing from a single image

---



# Application: Digital refocusing from a single image

---





# Application: Digital refocusing from a single image

---



# Application: Digital refocusing from a single image

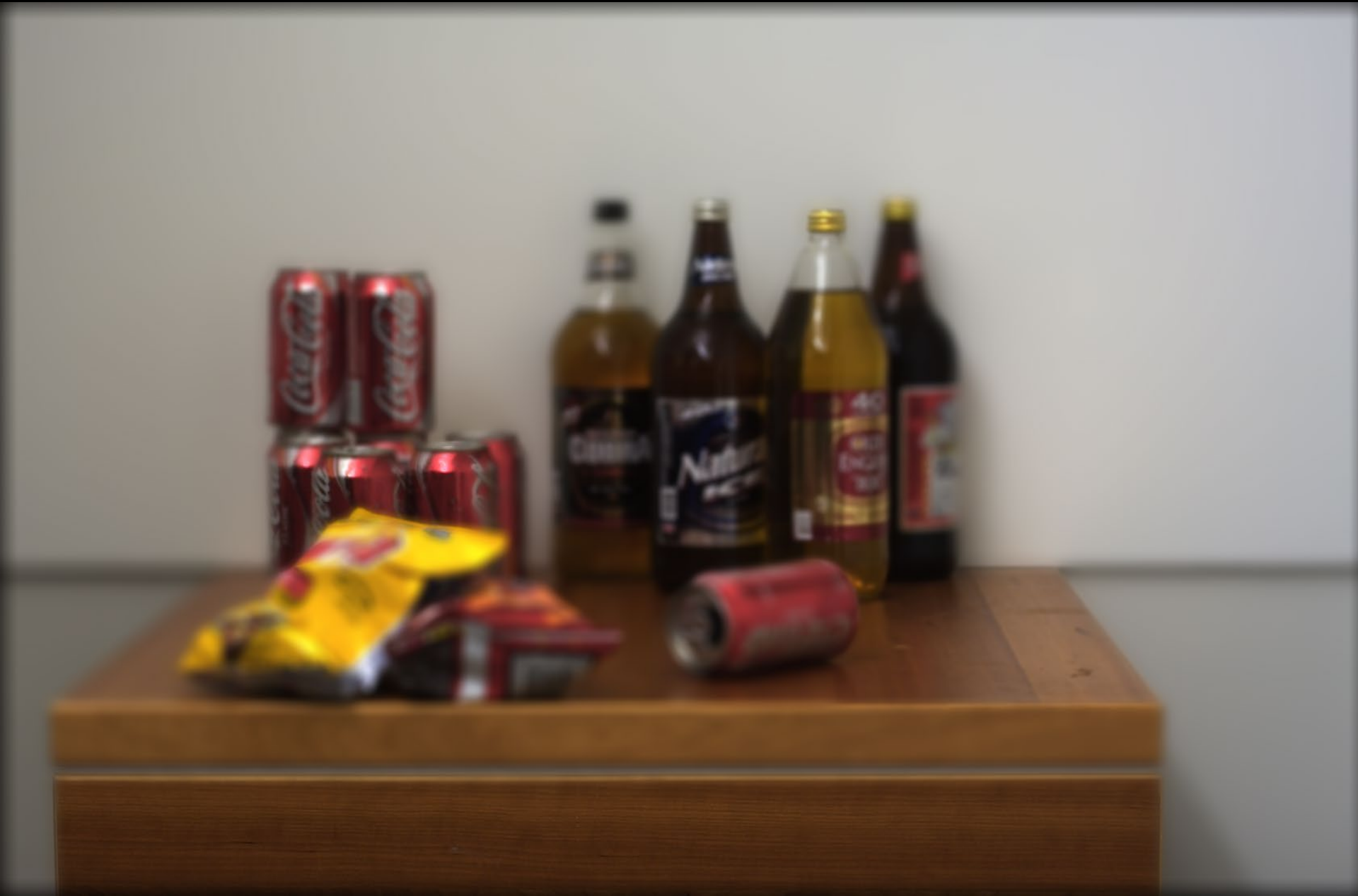
---





# Application: Digital refocusing from a single image

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# Application: Digital refocusing from a single image

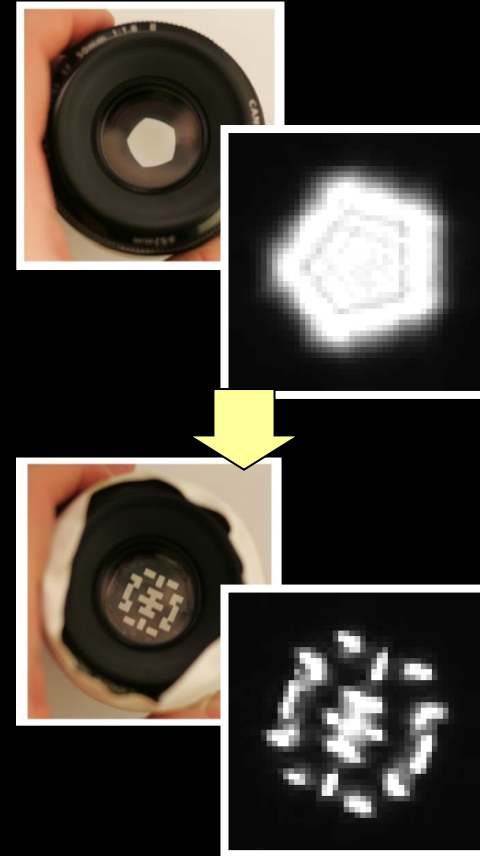
---



# Coded aperture: pros and cons

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- + Image AND depth at a single shot
- + No loss of image resolution
- + Simple modification to lens
- Depth is coarse
  - unable to get depth at untextured areas, might need manual corrections.
- + But depth is a pure bonus
- Lose some light
- + But deconvolution increases depth of field





50mm f/1.8: \$79.95

Cardboard: \$1

Tape: \$1

Depth acquisition: priceless



Some more quick examples



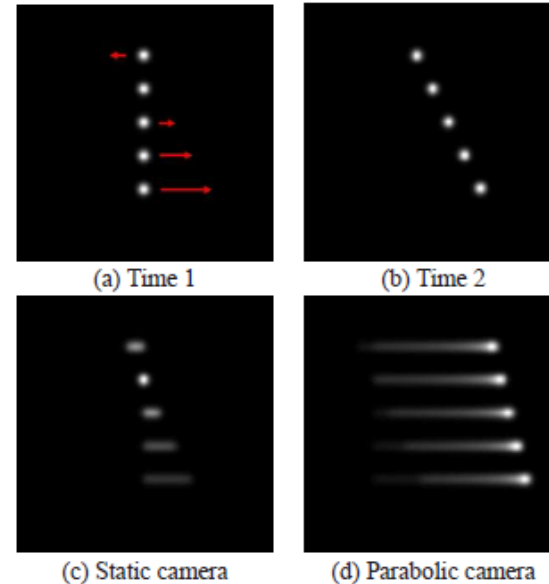
# Motion-Invariant Photography

Anat Levin Peter Sand Taeg Sang Cho Frédo Durand William T. Freeman

Massachusetts Institute of Technology, Computer Science and Artificial Intelligence Laboratory

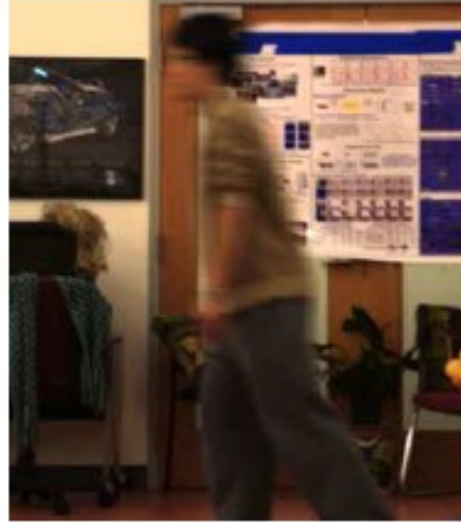


- Quickly move camera in a parabola when taking a picture
- A motion at any speed in the direction of the parabola will give the same blur kernel



# Results

Static  
Camera



Parabolic  
Camera



# Results

Static Camera



Parabolic Camera



Motion in  
wrong  
direction

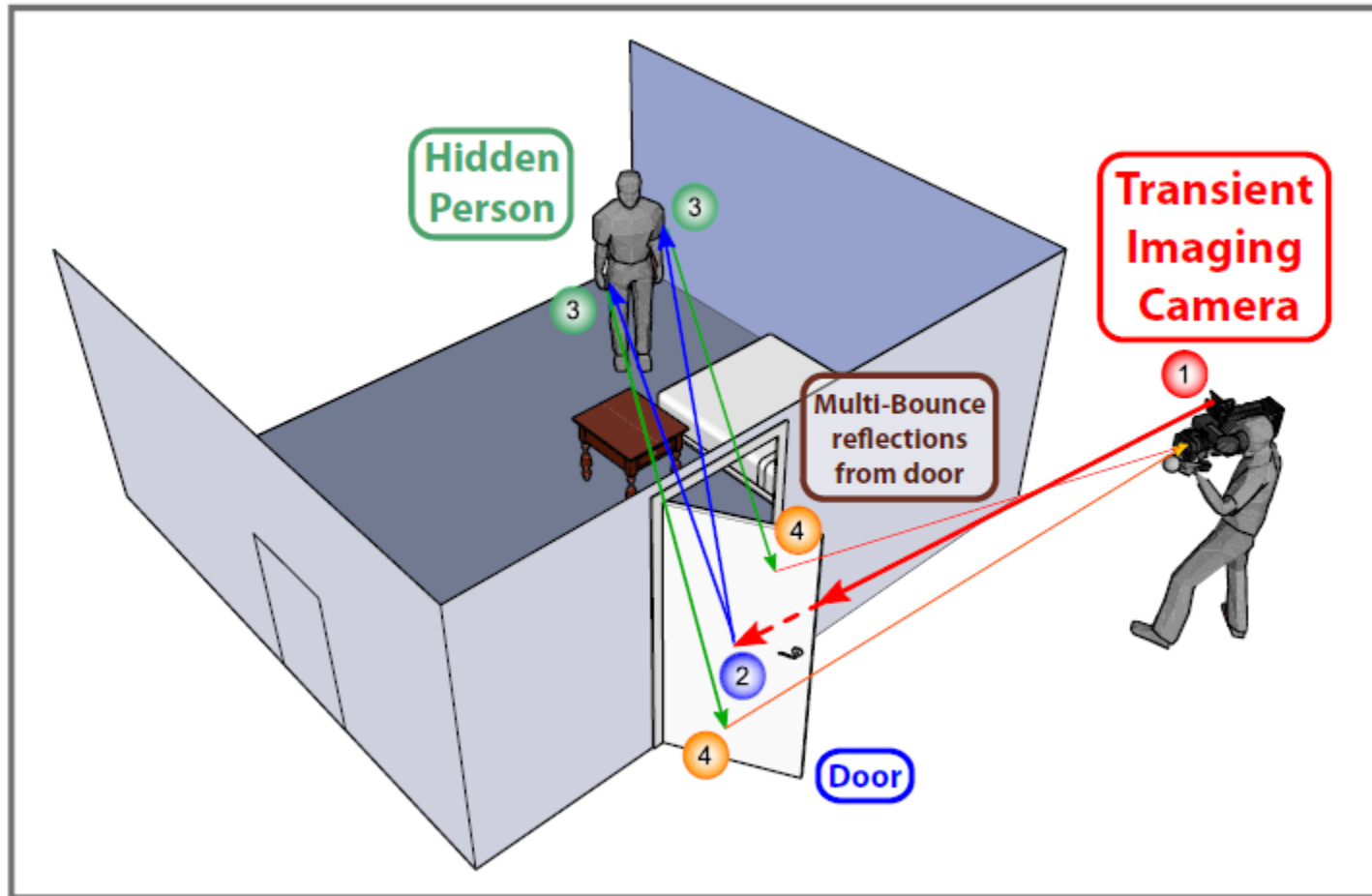


# Looking Around the Corner using Transient Imaging

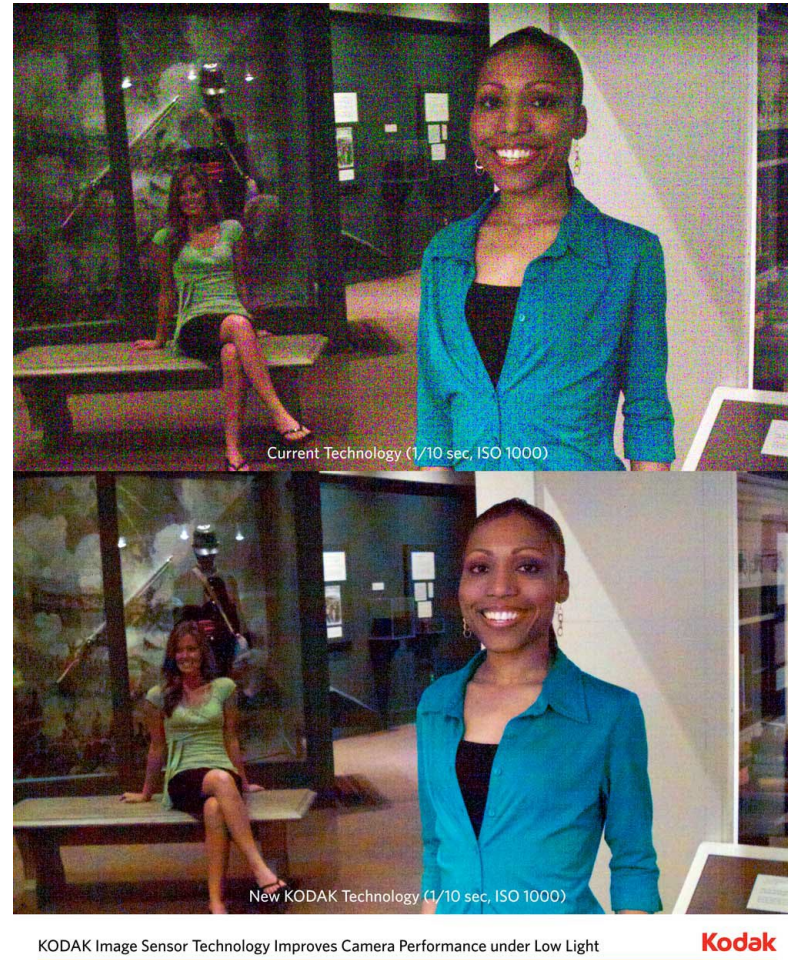
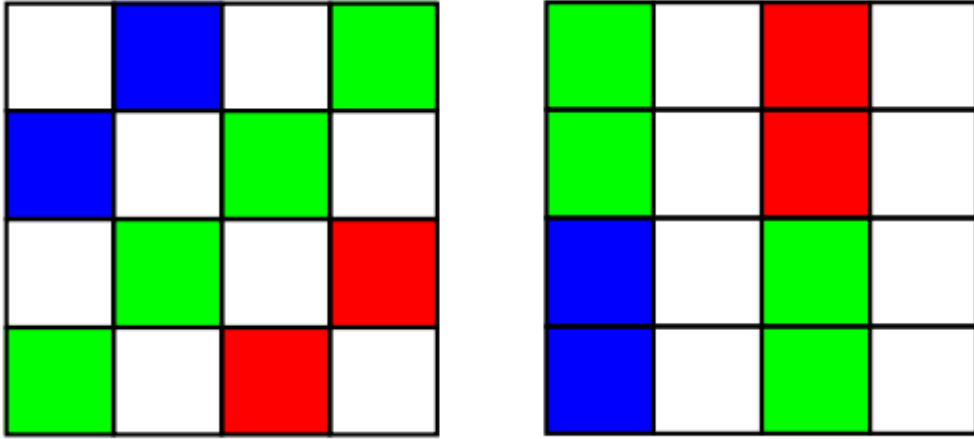
Ahmed Kirmani <sup>\*1</sup>, Tyler Hutchison<sup>1</sup>, James Davis <sup>†2</sup>, and Ramesh Raskar<sup>‡1</sup>

<sup>1</sup>MIT Media Laboratory

<sup>2</sup> UC Santa Cruz



# RGBW Sensors



- 2007: Kodak 'Panchromatic' Pixels
- Outperforms Bayer Grid
  - 2X-4X sensitivity (W: no filter loss)
  - May improve dynamic range (W >> RGB sensitivity)

# Computational Approaches to Display

- 3D TV without glasses
  - 20", \$2900, available in Japan (2010)
  - You see different images from different angles



Toshiba

[http://news.cnet.com/8301-13506\\_3-20018421-17.html](http://news.cnet.com/8301-13506_3-20018421-17.html)

Newer version: <http://www.pcmag.com/article2/0,2817,2392380,00.asp>

<http://reviews.cnet.com/3dtv-buying-guide/>

# Recap of questions

- How can we represent all of the information contained in light?
- What are the fundamental limitations of cameras?
- What sacrifices have we made in conventional cameras? For what benefits?
- How else can we design cameras for better focus, deblurring, multiple views, depth, etc.?

# Next class

- Video Magnification