

# ***Chapter 2: Memory Hierarchy Design – Part 2***

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Introduction (Section 2.1, Appendix B)

Caches

    Review of basics (Section 2.1, Appendix B)

    Advanced methods (Section 2.3)

Main Memory

Virtual Memory

# ***Fundamental Cache Parameters***

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## Cache Size

How large should the cache be?

## Block Size

What is the smallest unit represented in the cache?

## Associativity

How many entries must be searched for a given address?

# Cache Size

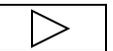
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Cache size is the total capacity of the cache

Bigger caches exploit temporal locality better than smaller caches

But are *not always* better

Why?



# Cache Size\*\*

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Too large a cache size

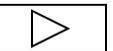
Smaller means faster  $\Rightarrow$  bigger means slower

Access time may degrade critical path

Too small a cache size

Don't exploit temporal locality well

Useful data is prematurely replaced



# *Block Size*

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Block (line) size is the data size that is both

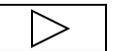
(a) associated with an address tag, and

(b) transferred to/from memory

Advanced caches allow different (a) & (b)

Problem with too small blocks

Problem with large blocks



# *Block Size\*\**

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(a) associated with an address tag, and

(b) transferred to/from memory

Advanced caches allow different (a) & (b)

Too small blocks

Don't exploit spatial locality well

Don't amortize memory access time well

Have inordinate address tag overhead

Too large blocks cause

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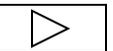
Don't amortize memory access time well

Have inordinate address tag overhead

Too large blocks cause

Unused data to be transferred

Useful data to be prematurely replaced



# *Set Associativity*

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Partition cache block frames & memory blocks in equivalence classes (usually w/ bit selection)

Number of sets,  $s$ , is the number of classes

Associativity (set size),  $n$ , is the number of block frames per class

Number of block frames in the cache is  $s \times n$

Cache Lookup (assuming read hit)

- Select set

- Associatively compare stored tags to incoming tag

- Route data to processor

# ***Associativity, cont.***

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Typical values for associativity

1 -- direct-mapped

$n = 2, 4, 8, 16$  --  $n$ -way set-associative

All blocks – fully-associative

Larger associativity

Smaller associativity

## ***Associativity, cont. \*\****

---

Typical values for associativity

1 -- direct-mapped

n = 2, 4, 8, 16 -- n-way set-associative

All blocks – fully-associative

Larger associativities

Lower miss ratios

Less variance

Smaller associativities

Lower cost

Faster access (hit) time (perhaps)

# ***Advanced Cache Design (Section 2.3)***

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Evaluation Methods

Two Levels of Cache

Getting Benefits of Associativity without Penalizing Hit Time

Reducing Miss Cost to Processor

Lockup-Free Caches

Beyond Simple Blocks

Prefetching

Pipelining and Banking for Higher Bandwidth

Software Restructuring

Handling Writes

# *Evaluation Methods*

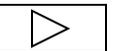
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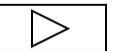
# *Evaluation Methods\*\**

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Hardware Counters

Analytic Models

Simulation



# *Method 1: Hardware Counters*

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## Advantages

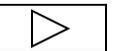
+

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## Disadvantages

-

-



# *Method 1: Hardware Counters\*\**

---

Count hits & misses in hardware

Advantages

+

+

Disadvantages

-

-

Many recent processors have hardware counters

# *Method 1: Hardware Counters\*\**

---

Count hits & misses in hardware

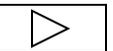
Advantages

- + Accurate
- + Realistic workload

Disadvantages

- Requires machine to exist
- Hard to vary cache parameters
- Experiments not deterministic

Many recent processors have hardware counters



# *Method 2: Analytic Models*

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Mathematical expressions

Advantages

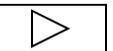
+

+

Disadvantages

-

-



## ***Method 2: Analytic Models\*\****

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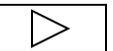
Mathematical expressions

Advantages

- + Insight -- can vary parameters
- + Fast

Disadvantages

- (Absolute) accuracy?
- Hard/time-consuming to determine many parameter values



## ***Method 3: Simulation***

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Software model of the system driven by model of program

Can be at different levels of abstraction

Functional vs. timing

Trace-driven vs. execution-driven

Advantages

Disadvantages

## ***Method 3: Simulation\*\****

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Software model of the system driven by model of program

Can be at different levels of abstraction

Functional vs. timing

Trace-driven vs. execution-driven

Advantages

- + Experiments repeatable
- + Can be accurate for many detailed metrics

Disadvantages

- Slow
- Still a model, can be inaccurate
- Only provides insight for the input programs simulated

# *Trace-Driven Simulation*

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Step 1:

Program + Input Data  $\xrightarrow{\text{Execute and Trace}}$  Trace File

Trace files may have only memory references or all instructions

Step 2:

Trace File + Input Cache Parameters

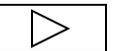
↓ Run simulator

Get miss ratio, tavg, execution time, etc.

Repeat Step 2 as often as desired

# ***Trace-Driven Simulation: Limitation?***

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# *Trace-Driven Simulation: Limitation?\**

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Impact of aggressive processor?

Does not model mispredicted paths, actual order of accesses

Reasonable traces are very large

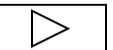
(Can integrate step 1 and step 2)

Alternative: Execution-driven simulation

Simulate entire application execution

Model full impact of processor

Mispredicted paths, reordering of accesses



# ***Average Memory Access Time and Performance***

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# ***Average Memory Access Time and Performance\*\****

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Old: Avg memory time = Hit time + Miss rate \* Miss penalty

But what is miss penalty in an out of order processor?

Hit time is no longer one cycle, hits can stall the processor

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Old: Avg memory time = Hit time + Miss rate \* Miss penalty

But what is miss penalty in an out of order processor?

Hit time is no longer one cycle, hits can stall the processor

Execution cycles = Busy cycles + Cycles due to CPU stalls + Cycles due to memory stalls

Cycles from memory stalls = stalls from misses + stalls from hits

Stalls from misses = # misses \*

(Total miss latency – overlapped latency)

# ***Average Memory Access Time and Performance\*\****

---

Stalls from misses = # misses \*

(Total miss latency – overlapped latency)

What is a stall?

Processor is stalled if it does not retire at its full rate

Charge stall to first instruction that cannot retire

Where do you start measuring latency?

From time instruction is queued in instruction window, or when address is generated, or when sent to memory system?

Anything works as long as is consistent

Miss latency is also made of latency due to and w/o contention

Hit stalls are analogous

# ***What About Non-Performance Metrics?***

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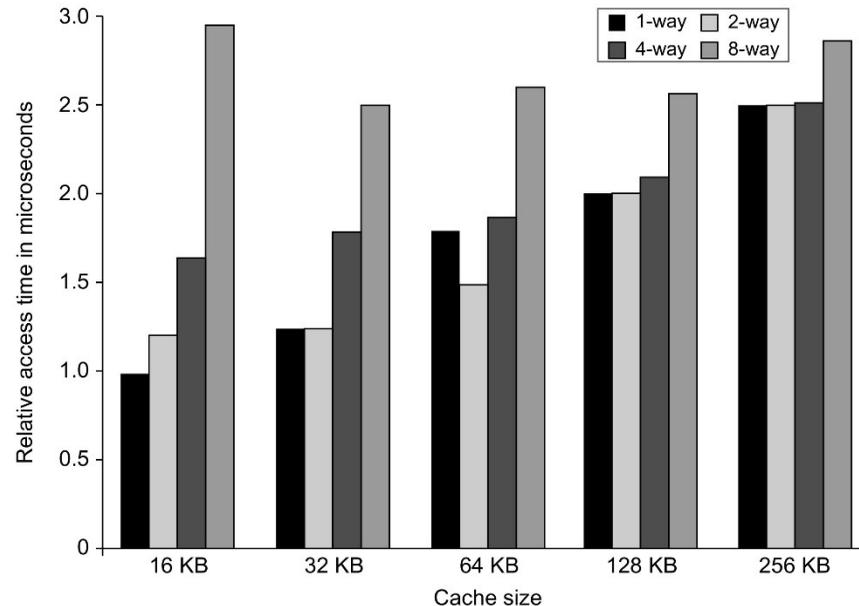
Area, power, detailed timing

CACTI for caches

McPAT: microarchitecture model for full multicore

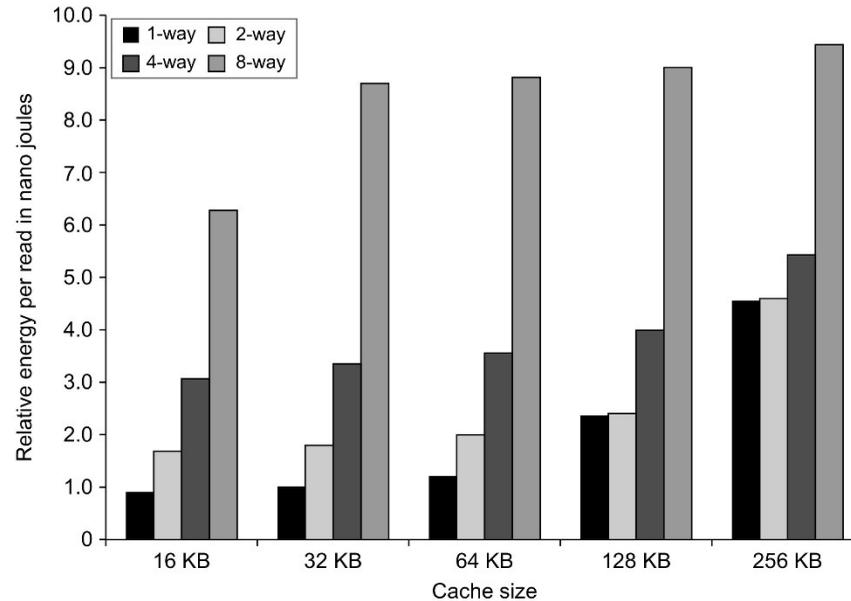
# Timing Data from CACTI

Y-axis unit  
incorrect



**Figure 2.8 Relative access times generally increase as cache size and associativity are increased.** These data come from the CACTI model 6.5 by Tarjan et al. (2005). The data assume typical embedded SRAM technology, a single bank, and 64-byte blocks. The assumptions about cache layout and the complex trade-offs between interconnect delays (that depend on the size of a cache block being accessed) and the cost of tag checks and multiplexing lead to results that are occasionally surprising, such as the lower access time for a 64 KiB with two-way set associativity versus direct mapping. Similarly, the results with eight-way set associativity generate unusual behavior as cache size is increased. Because such observations are highly dependent on technology and detailed design assumptions, tools such as CACTI serve to reduce the search space. These results are relative; nonetheless, they are likely to shift as we move to more recent and denser semiconductor technologies.

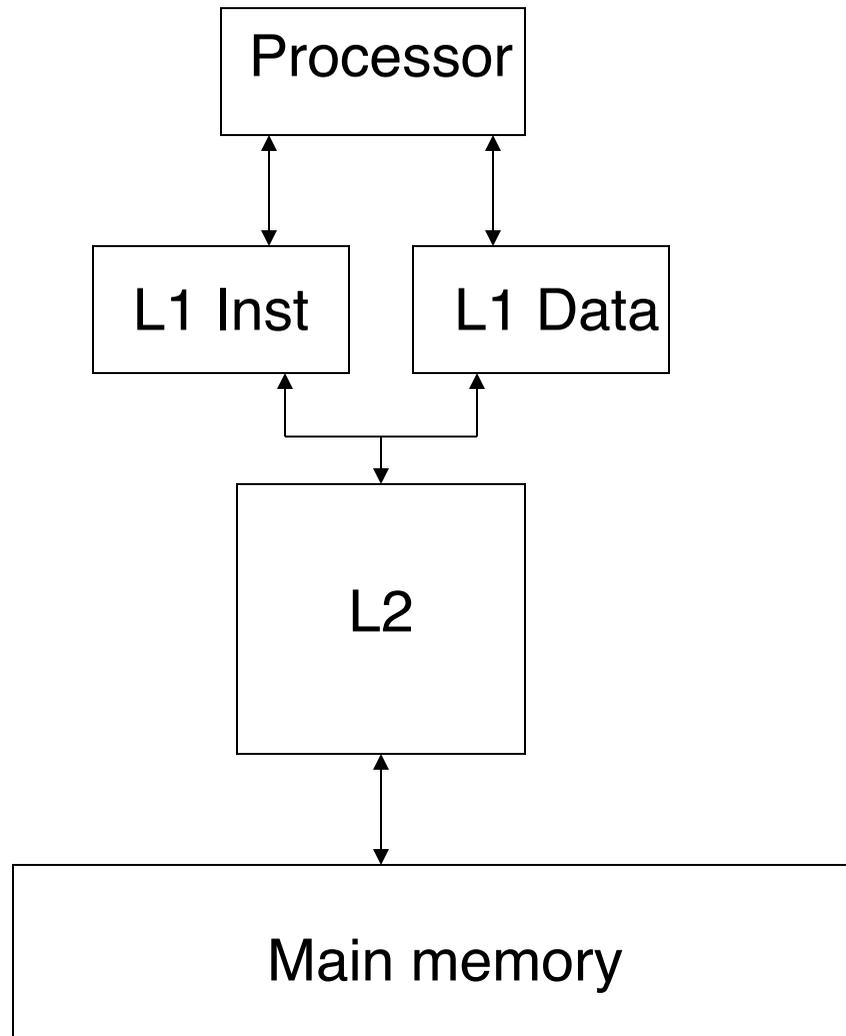
# Energy Data from CACTI



**Figure 2.9 Energy consumption per read increases as cache size and associativity are increased.** As in the previous figure, CACTI is used for the modeling with the same technology parameters. The large penalty for eight-way set associative caches is due to the cost of reading out eight tags and the corresponding data in parallel.

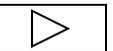
# Multilevel Caches

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# *Why Multilevel Caches?*

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# *Why Multilevel Caches?\**

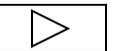
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Processors getting faster w.r.t. main memory

Want larger caches to reduce frequency of more costly misses

But larger caches are too slow for processor

Solution: reduce the cost of misses with a second (and third!)  
level of cache instead



# *Multilevel Inclusion*

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Multilevel inclusion holds if L2 cache always contains superset of data in L1 cache(s)

- Filter coherence traffic

- Makes L1 writes simpler

Example: Local LRU not sufficient

- Assume that L1 and L2 hold two and three blocks and both use local LRU

- Processor references: 1, 2, 1, 3, 1, 4

- Final contents of L1: 1, 4

- L1 misses: 1, 2, 3, 4

- Final contents of L2: 2, 3, 4, but not 1

## ***Multilevel Inclusion, cont.***

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Multilevel inclusion takes effort to maintain

(Typically L1/L2 cache line sizes are different)

Make L2 cache have bits or pointers giving L1 contents

Invalidate from L1 before replacing block from L2

Number of pointers per L2 block is  $(L2 \text{ blocksize} / L1 \text{ blocksize})$

## ***Multilevel Exclusion***

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What if the L2 cache is only slightly larger than L1?

Multilevel exclusion => A line in L1 is never in L2 (AMD Athlon)

# *Level Two Cache Design*

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L1 cache design similar to single-level cache design when main memories were ``faster''

Apply previous experience to L2 cache design?

What is ``miss ratio''?

Global -- L2 misses after L1 / references

Local -- L2 misses after L1 / L1 misses

BUT: L2 caches bigger than L1 experience (several MB)

BUT: L2 affects miss penalty, L1 affects clock rate

# ***Benefits of Associativity W/O Paying Hit Time***

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Victim Caches

Pseudo-Associative Caches

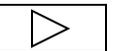
Way Prediction

# *Victim Cache*

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Add a small fully associative cache next to main cache

On a miss in main cache



# *Victim Cache\*\**

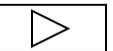
---

Add a small fully associative cache next to main cache

On a miss in main cache

Search in victim cache

Put any replaced data in victim cache



# *Pseudo-Associative Cache*

---

To determine where block is placed

Check one block frame as in direct mapped cache, but

If miss, check another block frame

E.g., frame with inverted MSB of index bit

Called a pseudo-set

Hit in first frame is fast

Placement of data

Put most often referenced data in “first” block frame and the other in the “second” frame of pseudo-set

# *Way Prediction*

---

Keep extra bits in cache to predict the “way” of the next access

Access predicted way first

If miss, access other ways like in set associative caches

Fast hit when prediction is correct

## *Reducing Miss Cost*

---

If main memory takes  $M$  cycles before delivering two words per cycle, we previously assumed

$$t_{memory} = t_{access} + B \times t_{transfer} = M + B \times 1/2$$

where  $B$  is block size in words

How can we do better?

## Reducing Miss Cost, cont.

---

$$t_{memory} = t_{access} + B \times t_{transfer} = M + B \times 1/2$$

⇒ the whole block is loaded before data returned

If main memory returned the reference first (requested-word-first)  
and the cache returned it to the processor before loading it into  
the cache data array (fetch-bypass, early restart),

$$t_{memory} = t_{access} + W \times t_{transfer} = M + W \times 1/2$$

where  $W$  is memory bus width in words

BUT ...

## *Reducing Miss Cost, cont.*

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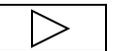
What if processor references unloaded word in block being loaded?

Why not generalize?

Handle other references that hit before any part of block is back?

Handle other references to other blocks that miss?

Called ``lockupfree" or ``nonblocking" cache



## *Reducing Miss Cost, cont.\*\**

---

What if processor references unloaded word in block being loaded?

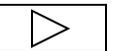
Must add (equivalent to) ``word" valid bits

Why not generalize?

Handle other references that hit before any part of block is back?

Handle other references to other blocks that miss?

Called ``lockup-free" or ``non-blocking" cache



# *Lockup-Free Caches*

---

Normal cache stalls while a miss is pending

Lockup-Free Caches

(a) Handle hits while first miss is pending

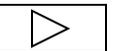
(b) Handle hits & misses until  $K$  misses are pending

Potential benefit

(a) Overlap misses with useful work & hits

(b) Also overlap misses with each other

Only makes sense if



# *Lockup-Free Caches\*\**

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Lockup-Free Caches

- (a) Handle hits while first miss is pending
- (b) Handle hits & misses until K misses are pending

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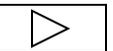
- (a) Overlap misses with useful work & hits
- (b) Also overlap misses with each other

Only makes sense if processor

Handles pending references correctly

Often can do useful work with references pending (Tomasulo, etc.)

Has misses that can be overlapped (for (b))



## *Lockup-Free Caches, cont.*

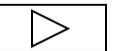
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Key implementation problems

- (1) Handling reads to pending miss
- (2) Handling writes to pending miss
- (3) Keep multiple requests straight

MSHRs -- miss status holding registers

What state do we need in MSHR?



## *Lockup-Free Caches, cont. \*\**

---

Key implementation problems

- (1) Handling reads to pending miss
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MSHRs -- miss status holding registers

For every MSHR – Valid bit

Block request address

For every word – Destination register?

Valid bit

Format (byte load, etc.)

Comparator (for later miss requests)

Limitation?

## *Lockup-Free Caches, cont.\*\**

---

Key implementation problems

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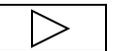
For every word – Destination register?

Valid bit

Format (byte load, etc.)

Comparator (for later miss requests)

Limitation: Must block on next access to same word



# *Beyond Simple Blocks*

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Break block size into

- Address block associated with tag

- Transfer block transferred to/from memory

Larger address blocks

- Decrease address tag overhead

- But allow fewer blocks to be resident

Larger transfer blocks

- Exploit spatial locality

- Amortize memory latency

- But take longer to load

- But replace more data already cached

- But cause unnecessary traffic

## ***Beyond Simple Blocks, cont.***

---

Address block size  $>$  transfer block size

Usually implies valid (& dirty) bit per transfer block

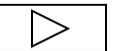
Used in 360/85 to reduce tag comparison logic

1K byte sectors with 64 byte subblocks

Transfer block size  $>$  address block size

``Prefetch on miss''

E.g., early MIPS R2000 board



# *Prefetching*

---

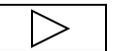
Prefetch instructions/data before processor requests them

Even "demand fetching" prefetches other words in the referenced block

Prefetching is useless unless a prefetch "costs" less than demand miss

Prefetches should

???



# *Prefetching\*\**

---

Prefetch instructions/data before processor requests them

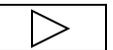
Even "demand fetching" prefetches other words in the referenced block

Prefetching is useless unless a prefetch "costs" less than demand miss

Prefetches should

- (a) Always get data back before it is referenced
- (b) Never get data not used
- (c) Never prematurely replace other data
- (d) Never interfere with other cache activity

Item (a) conflicts with (b), (c) and (d)



# *Prefetching Policy*

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Policy

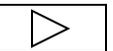
What to prefetch?

When to prefetch?

Simplest Policy

?

Enhancements



# *Prefetching Policy\*\**

---

## Policy

What to prefetch?

When to prefetch?

## Simplest Policy

One block (spatially) ahead on every access

## Enhancements

# *Prefetching Policy* \*\*

---

## Policy

What to prefetch?

When to prefetch?

## Simplest Policy

One block (spatially) ahead on every access

## Enhancements

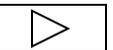
On every miss

Because hard to determine on every reference whether block to be prefetched is already in cache

Detect stride and prefetch on stride

Prefetch into prefetch buffer

Prefetch more than 1 block (for instruction caches, when block small)



# *Software Prefetching*

---

Use compiler to

Prefetch early

E.g., one loop iteration ahead

Prefetch accurately

# *Software Prefetching Example*

---

```
for (i = 0; i < N-1; i++) {  
    ... = A[i]  
    /* computation */  
}
```

Assume each iteration takes 10 cycles with a hit,  
memory latency is 100 cycles

# *Software Prefetching Example\*\**

---

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for (i = 0; i < N-1; i++) {  
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```

Assume each iteration takes 10 cycles with a hit,  
memory latency is 100 cycles

```
for (i = 0; i < N-1; i++) {  
    prefetch(A[i+10])  
    ... = A[i]  
    /* computation */  
}
```

## *Software Prefetching Example\*\**

---

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for (i = 0; i < N-1; i++) {  
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```
for (i = 0; i < N-1; i++) {  
    prefetch(A[i+10])  
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    /* computation */  
}
```

This is good with one word cache blocks

# Software Prefetching Example

---

```
for (i = 0; i < N-1; i++) {  
    ... = A[i]  
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```

Assume each iteration takes 10 cycles with a hit,  
memory latency is 100 cycles, **cache block is two words**

## Changes?

```
for (i = 0; i < N-1; i++) {  
    prefetch(A[i+10])  
    ... = A[i]  
    /* computation */  
}
```

# Software Prefetching Example\*\*

---

```
for (i = 0; i < N-1; i++) {  
    ... = A[i]  
    /* computation */  
}
```

Assume each iteration takes 10 cycles with a hit,

memory latency is 100 cycles, **cache block is two words**

```
for (i = 0; i < N-1; i+=2) {  
    prefetch(A[i+10])  
    ... = A[i]  
    ... = A[i+1]  
    /* computation for two iterations */  
}
```

# Software Restructuring

---

Restructure so that operations on a cache block done before going to next block

```
do i = 1 to rows
  do j = 1 to cols
    sum = sum + x[i,j]
```

What is the cache behavior?

# Software Restructuring (Cont.)

---

```
do i = 1 to rows
  do j = 1 to cols
    sum = sum + x[i,j]
```

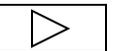
Column major order in memory

Code access pattern

Better code??

Called loop interchange

Many such optimizations possible (merging, fusion, blocking)



# Software Restructuring (Cont.) \*\*

---

```
do i = 1 to rows
  do j = 1 to cols
    sum = sum + x[i,j]
```

Column major order in memory

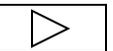
$x[i,j], x[i+1,j], x[i+2,j], \dots$

Code access pattern

Better code??

Called loop interchange

Many such optimizations possible (merging, fusion, blocking)



# Software Restructuring (Cont.) \*\*

---

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do i = 1 to rows
  do j = 1 to cols
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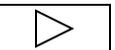
Code access pattern

$x[1,1], x[1,2], x[1,3], \dots$

Better code??

Called loop interchange

Many such optimizations possible (merging, fusion, blocking)



# Software Restructuring (Cont.) \*\*

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do i = 1 to rows
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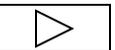
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Better code

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do j = 1 to cols
  do i = 1 to rows
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Called loop interchange

Many such optimizations possible (merging, fusion, blocking)



# ***Pipelining and Banking for Higher Bandwidth***

---

## Pipelining

Old: cache access = 1 cycle

New: 1 cycle caches would slow the whole processor

Pipeline: cache hit may take 4 cycles (affects misspeculation penalty)

## Multiple banks

Block based interleaving allows multiple accesses per cycle

# *Handling Writes - Pipelining*

---

Writing into a writeback cache

- Read tags (1 cycle)

- Write data (1 cycle)

Key observation

- Data RAMs unused during tag read

- Could complete a previous write

Add a special "Cache Write Buffer" (CWB)

- During tag check, write data and address to CWB

- If miss, handle in normal fashion

- If hit, written data stays in CWB

- When data RAMs are free (e.g., next write) store contents of CWB in data RAMs.

- Cache reads must check CWB (bypass)

Used in VAX 8800

# *Handling Writes - Write Buffers*

---

Writethrough caches are simple

But 5-15% of all instructions are stores

Need to buffer writes to memory

Write buffer

Write result in buffer

Buffer writes results to memory

Stall only when buffer is full

Can combine writes to same line (Coalescing write buffer - Alpha)

Allow reads to pass writes

What about data dependencies?

Could stall (slow)

Check address and bypass result

# *Handling Writes - Writeback Buffers*

---

Writeback caches need buffers too

- 10-20% of all blocks are written back

- 10-20% increase in miss penalty without buffer

On a miss

- Initiate fetch for requested block

- Copy dirty block into writeback buffer

- Copy requested block into cache, resume CPU

- Now write dirty block back to memory