

Programming Languages and Compilers (CS 421)

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Based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha

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Terminology: Review

- A function is in **Direct Style** when it returns its result back to the caller.
- A function is in **Continuation Passing Style** when it, and every function call in it, passes its result to another function.
- A **Tail Call** occurs when a function returns the result of another function call without any more computations (eg tail recursion)
- Instead of returning the result to the caller, we pass it forward to another function giving the computation after the call.

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CPS Transformation

- Step 1: Add continuation argument to any function definition:
 - $\text{let } f \text{ arg} = e \Rightarrow \text{let } f \text{ arg } k = e$
 - Idea: Every function takes an extra parameter saying where the result goes
- Step 2: A simple expression in tail position should be passed to a continuation instead of returned:
 - $\text{return } a \Rightarrow k \ a$
 - Assuming a is a constant or variable.
 - “Simple” = “No available function calls.”

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CPS Transformation

- Step 3: Pass the current continuation to every function call in tail position
 - $\text{return } f \text{ arg} \Rightarrow f \text{ arg } k$
 - The function “isn’t going to return,” so we need to tell it where to put the result.

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CPS Transformation

- Step 4: Each function call not in tail position needs to be converted to take a new continuation (containing the old continuation as appropriate)
 - $\text{return } \text{op } (f \text{ arg}) \Rightarrow f \text{ arg } (\text{fun } r \rightarrow k(\text{op } r))$
 - op represents a primitive operation
- $\text{return } g(f \text{ arg}) \Rightarrow f \text{ arg } (\text{fun } r \rightarrow g \ r \ k)$

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Example

Before:	After:
<pre>let rec add_list lst = match lst with [] -> 0 0 :: xs -> add_list xs x :: xs -> (+) x (add_list xs);;</pre>	<pre>let rec add_listk lst k = (* rule 1 *) match lst with [] -> k 0 (* rule 2 *) 0 :: xs -> add_listk xs k (* rule 3 *) x :: xs -> add_listk xs (fun r -> k ((+) x r)); (* rule 4 *)</pre>

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Example

Before:

```
let rec mem (y,lst) =  
  match lst with  
  [ ] -> false  
  | x :: xs ->  
    if (x = y)  
    then true  
    else mem(y,xs);;
```

After:

```
let rec memk (y,lst) k =  
  (* rule 1 *)
```

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Example

Before:

```
let rec mem (y,lst) =  
  match lst with  
  [ ] -> false  
  | x :: xs ->  
    if (x = y)  
    then true  
    else mem(y,xs);;
```

After:

```
let rec memk (y,lst) k =  
  (* rule 1 *)  
  k false (* rule 2 *)  
  k true (* rule 2 *)
```

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Example

Before:

```
let rec mem (y,lst) =  
  match lst with  
  [ ] -> false  
  | x :: xs ->  
    if (x = y)  
    then true  
    else mem(y,xs);;
```

After:

```
let rec memk (y,lst) k =  
  (* rule 1 *)  
  k false (* rule 2 *)  
  k true (* rule 2 *)  
  memk (y, xs) k (* rule 3 *)
```

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Example

Before:

```
let rec mem (y,lst) =  
  match lst with  
  [ ] -> false  
  | x :: xs ->  
    if (x = y)  
    then true  
    else mem(y,xs);;
```

After:

```
let rec memk (y,lst) k =  
  (* rule 1 *)  
  k false (* rule 2 *)  
  eqk (x, y)  
  (fun b -> b (* rule 4 *)  
   k true (* rule 2 *)  
   memk (y, xs) (* rule 3 *))
```

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Example

Before:

```
let rec mem (y,lst) =  
  match lst with  
  [ ] -> false  
  | x :: xs ->  
    if (x = y)  
    then true  
    else mem(y,xs);;
```

After:

```
let rec memk (y,lst) k =  
  (* rule 1 *)  
  k false (* rule 2 *)  
  eqk (x, y)  
  (fun b -> if b (* rule 4 *)  
   then k true (* rule 2 *)  
   else memk (y, xs) (* rule 3 *))
```

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Example

Before:

```
let rec mem (y,lst) =  
  match lst with  
  [ ] -> false  
  | x :: xs ->  
    if (x = y)  
    then true  
    else mem(y,xs);;
```

After:

```
let rec memk (y,lst) k =  
  (* rule 1 *)  
  match lst with  
  | [ ] -> k false (* rule 2 *)  
  | x :: xs ->  
    eqk (x, y)  
    (fun b -> if b (* rule 4 *)  
     then k true (* rule 2 *)  
     else memk (y, xs) k (* rule 3 *))
```

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Example

Before:

```
let rec mem (y,lst) =
  match lst with
  [ ] -> false
| x :: xs ->
  if (x = y)
  then true
  else mem(y,xs);;
```

After:

```
let rec memk (y,lst) k =
  (* rule 1 *)
  match lst with
  | [ ] -> k false (* rule 2 *)
  | x :: xs ->
    eqk (x, y)
    (fun b -> if b (* rule 4 *)
    then k true (* rule 2 *)
    else memk (y, xs) k (* rule 3 *))
```

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Data type in Ocaml: lists

- Frequently used lists in recursive program
- Matched over two structural cases
 - `[]` - the empty list
 - `(x :: xs)` a non-empty list
- Covers all possible lists
- `type 'a list = [] | (::) of 'a * 'a list`
 - Not quite legitimate declaration because of special syntax

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Variants - Syntax (slightly simplified)

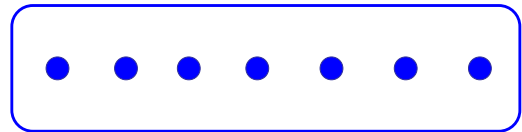
- `type name = C1[of ty1] | ... | Cn[of tyn]`
- Introduce a type called *name*
- `(fun x -> Cix) : tyi -> name`
- *C_i* is called a *constructor*; if the optional type argument is omitted, it is called a *constant*
- Constructors are the basis of almost all pattern matching

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Enumeration Types as Variants

An enumeration type is a collection of distinct values



In C and Ocaml they have an order structure; order by order of input

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Enumeration Types as Variants

```
# type weekday = Monday | Tuesday | Wednesday
  | Thursday | Friday | Saturday | Sunday;;
type weekday =
  Monday
| Tuesday
| Wednesday
| Thursday
| Friday
| Saturday
| Sunday
```

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Functions over Enumerations

```
# let day_after day = match day with
  Monday -> Tuesday
  | Tuesday -> Wednesday
  | Wednesday -> Thursday
  | Thursday -> Friday
  | Friday -> Saturday
  | Saturday -> Sunday
  | Sunday -> Monday;;
val day_after : weekday -> weekday = <fun>
```

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Functions over Enumerations

```
# let rec days_later n day =  
  match n with 0 -> day  
  | _ -> if n > 0  
    then day_after (days_later (n - 1) day)  
    else days_later (n + 7) day;;  
val days_later : int -> weekday -> weekday  
= <fun>
```

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Functions over Enumerations

```
# days_later 2 Tuesday;;  
- : weekday = Thursday  
# days_later (-1) Wednesday;;  
- : weekday = Tuesday  
# days_later (-4) Monday;;  
- : weekday = Thursday
```

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Problem:

```
# type weekday = Monday | Tuesday |  
  Wednesday  
  | Thursday | Friday | Saturday | Sunday;;  
■ Write function is_weekend : weekday -> bool  
let is_weekend day =
```

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Problem:

```
# type weekday = Monday | Tuesday |  
  Wednesday  
  | Thursday | Friday | Saturday | Sunday;;  
■ Write function is_weekend : weekday -> bool  
let is_weekend day =  
  match day with Saturday -> true  
  | Sunday -> true  
  | _ -> false
```

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Example Enumeration Types

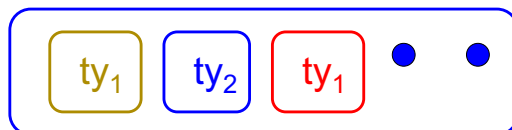
```
# type bin_op = IntPlusOp | IntMinusOp  
  | EqOp | CommaOp | ConsOp  
  
# type mon_op = HdOp | TIOp | FstOp  
  | SndOp
```

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Disjoint Union Types

- Disjoint union of types, with some possibly occurring more than once



- We can also add in some new singleton elements

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Disjoint Union Types

```
# type id = DriversLicense of int
| SocialSecurity of int | Name of string;;
type id = DriversLicense of int | SocialSecurity
of int | Name of string
# let check_id id = match id with
  DriversLicense num ->
    not (List.mem num [13570; 99999])
  | SocialSecurity num -> num < 900000000
  | Name str -> not (str = "John Doe");;
val check_id : id -> bool = <fun>
```

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Problem

- Create a type to represent the currencies for US, UK, Europe and Japan

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Problem

- Create a type to represent the currencies for US, UK, Europe and Japan

```
type currency =
  Dollar of int
| Pound of int
| Euro of int
| Yen of int
```

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Example Disjoint Union Type

```
# type const =
  BoolConst of bool
  | IntConst of int
  | FloatConst of float
  | StringConst of string
  | NilConst
  | UnitConst
```

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Example Disjoint Union Type

```
# type const = BoolConst of bool
  | IntConst of int | FloatConst of float
  | StringConst of string | NilConst
  | UnitConst
```

- How to represent 7 as a const?
- Answer: `IntConst 7`

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Polymorphism in Variants

- The type `'a option` gives us something to represent non-existence or failure

```
# type 'a option = Some of 'a | None;;
type 'a option = Some of 'a | None
```

- Used to encode partial functions
- Often can replace the raising of an exception

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Functions producing option

```
# let rec first p list =
  match list with [ ] -> None
  | (x::xs) -> if p x then Some x else first p xs;;
val first : ('a -> bool) -> 'a list -> 'a option = <fun>
# first (fun x -> x > 3) [1;3;4;2;5];;
- : int option = Some 4
# first (fun x -> x > 5) [1;3;4;2;5];;
- : int option = None
```

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Functions over option

```
# let result_ok r =
  match r with None -> false
  | Some _ -> true;;
val result_ok : 'a option -> bool = <fun>
# result_ok (first (fun x -> x > 3) [1;3;4;2;5]);;
- : bool = true
# result_ok (first (fun x -> x > 5) [1;3;4;2;5]);;
- : bool = false
```

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Problem

- Write a hd and tl on lists that doesn't raise an exception and works at all types of lists.

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Problem

- Write a hd and tl on lists that doesn't raise an exception and works at all types of lists.
- let hd list =
 match list with [] -> None
 | (x::xs) -> Some x
- let tl list =
 match list with [] -> None
 | (x::xs) -> Some xs

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Mapping over Variants

```
# let optionMap f opt =
  match opt with None -> None
  | Some x -> Some (f x);;
val optionMap : ('a -> 'b) -> 'a option -> 'b option = <fun>
# optionMap
  (fun x -> x - 2)
  (first (fun x -> x > 3) [1;3;4;2;5]);;
- : int option = Some 2
```

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Folding over Variants

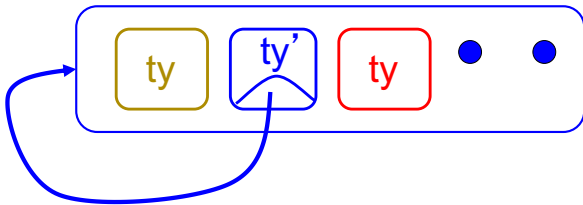
```
# let optionFold someFun noneVal opt =
  match opt with None -> noneVal
  | Some x -> someFun x;;
val optionFold : ('a -> 'b) -> 'b -> 'a option -> 'b = <fun>
# let optionMap f opt =
  optionFold (fun x -> Some (f x)) None opt;;
val optionMap : ('a -> 'b) -> 'a option -> 'b option = <fun>
```

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Recursive Types

- The type being defined may be a component of itself



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Recursive Data Types

```
# type int_Bin_Tree =  
  Leaf of int | Node of (int_Bin_Tree *  
  int_Bin_Tree);;
```

```
type int_Bin_Tree = Leaf of int | Node of  
(int_Bin_Tree * int_Bin_Tree)
```

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Recursive Data Type Values

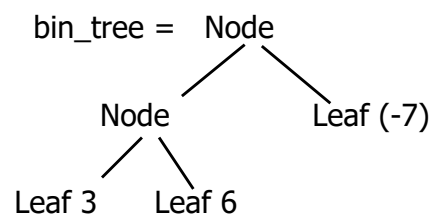
```
# let bin_tree =  
  Node(Node(Leaf 3, Leaf 6),Leaf (-7));;
```

```
val bin_tree : int_Bin_Tree = Node (Node  
(Leaf 3, Leaf 6), Leaf (-7))
```

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Recursive Data Type Values



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Recursive Functions

```
# let rec first_leaf_value tree =  
  match tree with (Leaf n) -> n  
  | Node (left_tree, right_tree) ->  
    first_leaf_value left_tree;;  
val first_leaf_value : int_Bin_Tree -> int =  
  <fun>  
# let left = first_leaf_value bin_tree;;  
val left : int = 3
```

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Recursive Data Types

```
# type exp =  
  VarExp of string  
  | ConstExp of const  
  | MonOpAppExp of mon_op * exp  
  | BinOpAppExp of bin_op * exp * exp  
  | IfExp of exp * exp * exp  
  | AppExp of exp * exp  
  | FunExp of string * exp
```

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Recursive Data Types

```
# type bin_op = IntPlusOp | IntMinusOp
  | EqOp | CommaOp | ConsOp | ...
# type const = BoolConst of bool | IntConst of int |
...
# type exp = VarExp of string | ConstExp of const
  | BinOpAppExp of bin_op * exp * exp | ...
```

- How to represent 6 as an exp?

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Recursive Data Types

```
# type bin_op = IntPlusOp | IntMinusOp
  | EqOp | CommaOp | ConsOp | ...
# type const = BoolConst of bool | IntConst of int |
...
# type exp = VarExp of string | ConstExp of const
  | BinOpAppExp of bin_op * exp * exp | ...
```

- How to represent 6 as an exp?
- Answer: ConstExp (IntConst 6)

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Recursive Data Types

```
# type bin_op = IntPlusOp | IntMinusOp
  | EqOp | CommaOp | ConsOp | ...
# type const = BoolConst of bool | IntConst of int |
...
# type exp = VarExp of string | ConstExp of const
  | BinOpAppExp of bin_op * exp * exp | ...
```

- How to represent (6, 3) as an exp?

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Recursive Data Types

```
# type bin_op = IntPlusOp | IntMinusOp
  | EqOp | CommaOp | ConsOp | ...
# type const = BoolConst of bool | IntConst of int |
...
# type exp = VarExp of string | ConstExp of const
  | BinOpAppExp of bin_op * exp * exp | ...
```

- How to represent (6, 3) as an exp?
- BinOpAppExp (CommaOp, ConstExp (IntConst 6), ConstExp (IntConst 3))

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Recursive Data Types

```
# type bin_op = IntPlusOp | IntMinusOp
  | EqOp | CommaOp | ConsOp | ...
# type const = BoolConst of bool | IntConst of int |
...
# type exp = VarExp of string | ConstExp of const
  | BinOpAppExp of bin_op * exp * exp | ...
```

- How to represent [(6, 3)] as an exp?
- BinOpAppExp (ConsOp, BinOpAppExp (CommaOp, ConstExp (IntConst 6), ConstExp (IntConst 3)), ConstExp NilConst))

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Problem

```
type int_Bin_Tree = Leaf of int
  | Node of (int_Bin_Tree * int_Bin_Tree);;
```

- Write sum_tree : int_Bin_Tree -> int
 - Adds all ints in tree
- ```
let rec sum_tree t =
```

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## Problem

```
type int_Bin_Tree = Leaf of int
| Node of (int_Bin_Tree * int_Bin_Tree);;
■ Write sum_tree : int_Bin_Tree -> int
■ Adds all ints in tree
let rec sum_tree t =
 match t with Leaf n -> n
 | Node(t1,t2) -> sum_tree t1 + sum_tree t2
```

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## Recursion over Recursive Data Types

```
type exp = VarExp of string | ConstExp of const
| BinOpAppExp of bin_op * exp * exp
| FunExp of string * exp | AppExp of exp * exp
■ How to count the number of variables in an exp?
```

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## Recursion over Recursive Data Types

```
type exp = VarExp of string | ConstExp of const
| BinOpAppExp of bin_op * exp * exp
| FunExp of string * exp | AppExp of exp * exp
■ How to count the number of variables in an exp?
let rec varCnt exp =
 match exp with VarExp x ->
 | ConstExp c ->
 | BinOpAppExp (b, e1, e2) ->
 | FunExp (x,e) ->
 | AppExp (e1, e2) ->
```

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## Recursion over Recursive Data Types

```
type exp = VarExp of string | ConstExp of const
| BinOpAppExp of bin_op * exp * exp
| FunExp of string * exp | AppExp of exp * exp
■ How to count the number of variables in an exp?
let rec varCnt exp =
 match exp with VarExp x -> 1
 | ConstExp c -> 0
 | BinOpAppExp (b, e1, e2) -> varCnt e1 + varCnt e2
 | FunExp (x,e) -> 1 + varCnt e
 | AppExp (e1, e2) -> varCnt e1 + varCnt e2
```

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Your turn now

Try Problem 3 on MP5

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## Mapping over Recursive Types

```
let rec ibtreeMap f tree =
 match tree with (Leaf n) -> Leaf (f n)
 | Node (left_tree, right_tree) ->
 Node (ibtreeMap f left_tree,
 ibtreeMap f right_tree);;
val ibtreeMap : (int -> int) -> int_Bin_Tree ->
int_Bin_Tree = <fun>
```

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## Mapping over Recursive Types

```
ibtreeMap ((+) 2) bin_tree;;

- : int_Bin_Tree = Node (Node (Leaf 5, Leaf
8), Leaf (-5))
```

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## Folding over Recursive Types

```
let rec ibtreeFoldRight leafFun nodeFun tree =
 match tree with Leaf n -> leafFun n
 | Node (left_tree, right_tree) ->
 nodeFun
 (ibtreeFoldRight leafFun nodeFun left_tree)
 (ibtreeFoldRight leafFun nodeFun right_tree);;
val ibtreeFoldRight : (int -> 'a) -> ('a -> 'a -> 'a) ->
int_Bin_Tree -> 'a = <fun>
```

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## Folding over Recursive Types

```
let tree_sum =
 ibtreeFoldRight (fun x -> x) (+);;
val tree_sum : int_Bin_Tree -> int = <fun>
tree_sum bin_tree;;
- : int = 2
```

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600 minutes

## Mutually Recursive Types

```
type 'a tree = TreeLeaf of 'a
 | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree
 | More of ('a tree * 'a treeList);;
type 'a tree = TreeLeaf of 'a | TreeNode of 'a
treeList
and 'a treeList = Last of 'a tree | More of ('a
tree * 'a treeList)
```

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## Mutually Recursive Types - Values

```
let tree =
 TreeNode
 (More (TreeLeaf 5,
 (More (TreeNode
 (More (TreeLeaf 3,
 Last (TreeLeaf 2))),
 Last (TreeLeaf 7)))))
```

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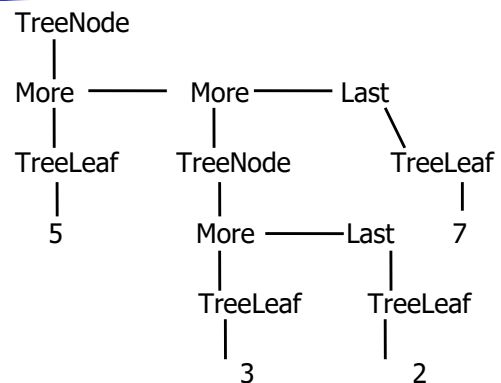
## Mutually Recursive Types - Values

```
val tree : int tree =
 TreeNode
 (More
 (TreeLeaf 5,
 More
 (TreeNode (More (TreeLeaf 3, Last
 (TreeLeaf 2))), Last (TreeLeaf 7))))
```

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## Mutually Recursive Types - Values

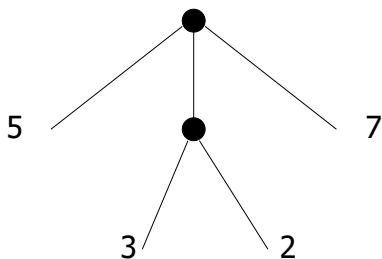


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## Mutually Recursive Types - Values

A more conventional picture



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## Mutually Recursive Functions

```
let rec fringe tree =
 match tree with (TreeLeaf x) -> [x]
 | (TreeNode list) -> list_fringe list
and list_fringe tree_list =
 match tree_list with (Last tree) -> fringe tree
 | (More (tree,list)) ->
 (fringe tree) @ (list_fringe list);;
```

```
val fringe : 'a tree -> 'a list = <fun>
val list_fringe : 'a treeList -> 'a list = <fun>
```

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## Mutually Recursive Functions

```
fringe tree;;
- : int list = [5; 3; 2; 7]
```

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## Problem

```
type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size
```

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## Problem

```
type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size
let rec tree_size t =
 match t with TreeLeaf _ ->
 | TreeNode ts ->
```

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## Problem

```
type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size
let rec tree_size t =
 match t with TreeLeaf _ -> 1
 | TreeNode ts -> treeList_size ts
```

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## Problem

```
type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size and treeList_size
let rec tree_size t =
 match t with TreeLeaf _ -> 1
 | TreeNode ts -> treeList_size ts
and treeList_size ts =
```

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## Problem

```
type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size and treeList_size
let rec tree_size t =
 match t with TreeLeaf _ -> 1
 | TreeNode ts -> treeList_size ts
and treeList_size ts =
 match ts with Last t ->
 | More t ts' ->
```

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## Problem

```
type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size and treeList_size
let rec tree_size t =
 match t with TreeLeaf _ -> 1
 | TreeNode ts -> treeList_size ts
and treeList_size ts =
 match ts with Last t -> tree_size t
 | More t ts' -> tree_size t + treeList_size ts'
```

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## Problem

```
type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size and treeList_size
let rec tree_size t =
 match t with TreeLeaf _ -> 1
 | TreeNode ts -> treeList_size ts
and treeList_size ts =
 match ts with Last t -> tree_size t
 | More t ts' -> tree_size t + treeList_size ts'
```

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## Mutually Recursive Functions

```
val flatten_tree : 'a labeled_tree -> 'a list =
 <fun>
val flatten_tree_list : 'a labeled_tree list -> 'a
 list = <fun>
flatten_tree ltree;;
- : int list = [5; 3; 2; 1; 7; 5]
```

- Nested recursive types lead to mutually recursive functions

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## Why Data Types?

- Data types play a key role in:

- *Data abstraction* in the design of programs
- *Type checking* in the analysis of programs
- *Compile-time code generation* in the translation and execution of programs
  - Data layout (how many words; which are data and which are pointers) dictated by type

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## Terminology

- Type: A type  $t$  defines a set of possible data values
  - E.g. `short` in C is  $\{x \mid -2^{15} - 1 \leq x \leq 2^{15}\}$
  - A value in this set is said to have type  $t$
- Type system: rules of a language assigning types to expressions

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## Types as Specifications

- Types describe properties
- Different type systems describe different properties, eg
  - Data is read-write versus read-only
  - Operation has authority to access data
  - Data came from “right” source
  - Operation might or could not raise an exception
- Common type systems focus on types describing same data layout and access methods

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## Sound Type System

- If an expression is assigned type  $t$ , and it evaluates to a value  $v$ , then  $v$  is in the set of values defined by  $t$
- SML, OCAML, Scheme and Ada have sound type systems
- Most implementations of C and C++ do not

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## Strongly Typed Language

- When no application of an operator to arguments can lead to a run-time type error, language is *strongly typed*
  - Eg: `1 + 2.3;;`
- Depends on definition of “type error”

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## Strongly Typed Language

- C++ claimed to be “strongly typed”, but
  - Union types allow creating a value at one type and using it at another
  - Type coercions may cause unexpected (undesirable) effects
  - No array bounds check (in fact, no runtime checks at all)
- SML, OCAML “strongly typed” but still must do dynamic array bounds checks, runtime type case analysis, and other checks

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## Static vs Dynamic Types

- *Static type*: type assigned to an expression at compile time
- *Dynamic type*: type assigned to a storage location at run time
- *Statically typed language*: static type assigned to every expression at compile time
- *Dynamically typed language*: type of an expression determined at run time

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## Type Checking

- When is  $op(arg1, \dots, argn)$  allowed?
- *Type checking* assures that operations are applied to the right number of arguments of the right types
  - Right type may mean same type as was specified, or may mean that there is a predefined implicit coercion that will be applied
- Used to resolve overloaded operations

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## Type Checking

- Type checking may be done *statically* at compile time or *dynamically* at run time
- Dynamically typed (aka untyped) languages (eg LISP, Prolog) do only dynamic type checking
- Statically typed languages can do most type checking statically

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## Dynamic Type Checking

- Performed at run-time before each operation is applied
- Types of variables and operations left unspecified until run-time
  - Same variable may be used at different types

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## Dynamic Type Checking

- Data object must contain type information
- Errors aren't detected until violating application is executed (maybe years after the code was written)

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## Static Type Checking

- Performed after parsing, before code generation
- Type of every variable and signature of every operator must be known at compile time

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## Static Type Checking

- Can eliminate need to store type information in data object if no dynamic type checking is needed
- Catches many programming errors at earliest point
- Can't check types that depend on dynamically computed values
  - Eg: array bounds

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## Static Type Checking

- Typically places restrictions on languages
  - Garbage collection
  - References instead of pointers
  - All variables initialized when created
  - Variable only used at one type
    - Union types allow for work-arounds, but effectively introduce dynamic type checks

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