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Example

4/28/23

- For 1, by the sequencing rule it suffices to show
  3. {x>=0 and x = a} fact := 1 {a! = fact \* (x!) and x >=0 }
  And
  4. {a! = fact \* (x!) and x >=0} while x > 0 do
  - (fact := fact \* x; x := x 1) od {a! = fact \* (x!) and x >=0 and not (x > 0)}

• Suffices to show that  $\{a! = fact * (x!) and x \ge 0\}$ holds before the while loop is entered and that if  $\{(a! = fact * (x!)) and x \ge 0 and x > 0\}$ holds before we execute the body of the loop, then  $\{(a! = fact * (x!)) and x \ge 0\}$ holds after we execute the body



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By the assignment rule, we have  $\{(a! = fact * ((x-1)!)) and x - 1 \ge 0\}$  x := x - 1  $\{(a! = fact * (x!)) and x \ge 0\}$ By the sequencing rule, it suffices to show  $\{(a! = fact * (x!)) and x \ge 0 and x \ge 0\}$  fact = fact \* x $\{(a! = fact * ((x-1)!)) and x - 1 \ge 0\}$ 

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## Example

By the assignment rule, we have that  $\{(a! = (fact * x) * ((x-1)!)) and x - 1 \ge 0\}$ fact = fact \* x  $\{(a! = fact * ((x-1)!)) and x - 1 \ge 0\}$ By Precondition strengthening, it suffices to show that  $((a! = fact * (x!)) and x \ge 0 and x \ge 0) \Rightarrow$   $((a! = (fact * x) * ((x-1)!)) and x - 1 \ge 0)$ 



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Therefore, by precondition strengthening  $\{(a! = fact * (x!)) and x \ge 0 and x \ge 0\}$  fact = fact \* x $\{(a! = fact * ((x-1)!)) and x - 1 \ge 0\}$ 

This finishes the proof

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