# Programming Languages and Compilers (CS 421) 

## Elsa L Gunter <br> 2112 SC, UIUC


https://courses.engr.illinois.edu/cs421/sp2023

Based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha

## Ambiguous Grammars and Languages

- A BNF grammar is ambiguous if its language contains strings for which there is more than one parse tree
- If all BNF' s for a language are ambiguous then the language is inherently ambiguous


## Example: Ambiguous Grammar

- $0+1+0$

<Sum>+ <sum> ${ }^{1}$
1
0
 1
0 <Sum> + <Sum>



## Example

- What is the result for:

$$
3+4 * 5+6
$$

## Example

- What is the result for:

$$
3+4 * 5+6
$$

- Possible answers:
- $41=((3+4) * 5)+6$
- $47=3+(4 *(5+6))$
- $29=(3+(4 * 5))+6=3+((4 * 5)+6)$
- $77=(3+4) *(5+6)$


## Example

- What is the value of:

$$
7-5-2
$$

## Example

What is the value of:

$$
7-5-2
$$

## Possible answers:

- In Pascal, C++, SML assoc. left

$$
7-5-2=(7-5)-2=0
$$

- In APL, associate to right

$$
7-5-2=7-(5-2)=4
$$

## Two Major Sources of Ambiguity

- Lack of determination of operator precedence
- Lack of determination of operator associativity
- Not the only sources of ambiguity


## Example

- Ambiguous grammar:

$$
\begin{aligned}
& \text { <exp> }::=0|1|(\text { eexp> ) } \\
& \mid<\operatorname{exp>}+\text { <exp> } \\
& \mid \text { <exp> * <exp> }
\end{aligned}
$$

- Strings with more then one parse:

$$
\begin{gathered}
0+1+0 \\
1 * 1+1
\end{gathered}
$$

- Sources of ambiguity here: associativity and precedence


## Operator Precedence

- Operators of highest precedence get arguments first (bind more tightly).
- This generally means evaluated first
- Precedence for infix binary operators given in following table
- Needs to be reflected in grammar


## Precedence Table - Sample

$\left.$|  | Fortan | Pascal | $\mathrm{C} / \mathrm{C}++$ | Ada | SML |
| :---: | :---: | :---: | :---: | :---: | :---: |
| highest | $* *$ | $*, /$, <br> div, <br> mod | ,++-- | $* *$ | div, <br> mod, <br> $/, *$ |
|  | $*, /$ | ,+- | $*, /$, | $*, /$, |  |
| $\%$ |  |  |  |  |  |
| mod |  |  |  |  |  | | ,,+- |
| :---: |
| $\wedge$ | \right\rvert\,

## Disambiguating a Grammar

- Given ambiguous grammar G, with start symbol S, find a grammar $\mathrm{G}^{\prime}$ with same start symbol, such that

$$
\text { language of } \mathrm{G}=\text { language of } \mathrm{G}^{\prime}
$$

- Not always possible
- No algorithm in general


## Disambiguating a Grammar

- Idea: Each non-terminal represents all strings having some property, its language
- Each rule describes a sublanguage
- Identify these properties (often in terms of things that can't happen)
- Use these properties to inductively guarantee every string in language has a unique parse


## Steps to Grammar Disambiguation

- Identify the rules and a smallest use that display ambiguity
- Decide which parse to keep; why should others be thrown out?
- What syntactic restrictions on subexpressions are needed to throw out the bad (while keeping the good)?
- Add a new non-terminal and rules to describe this set of restricted subexpressions (called stratifying, or refactoring)
- Characterize each non-terminal by a language invariant
- Replace old rules to use new non-terminals
- Rinse and repeat


## How to Enforce Associativity

- Have at most one recursive call per production
- When two or more recursive calls would be natural, leave right-most one for right associativity, left-most one for left associativity


## Example

- <Sum> ::= 0 | 1 | <Sum> + <Sum> | (<Sum>)
- Becomes
- <Sum> ::= <Num> | <Num> + <Sum>
- <Num> ::=0|1|(<Sum>)
<Sum $>+$ SSum $>+<$ Sum $>$


## Predence in Grammar

- Higher precedence translates to longer derivation chain
- Example: * higher than +, both assoc left
<exp> ::=0|1 | (exp>)

$$
|<\exp >+<\exp >|<\exp >*<\exp >
$$

- Becomes

$$
\begin{gathered}
\text { <exp> }::=\text { <mult_exp> } \\
\text { | <exp> + <mult_exp> } \\
\text { <mult_exp> ::= <id> | <mult_exp> * <id> } \\
\text { <id> }::=0|1|(\text { <exp> })
\end{gathered}
$$

## Many other sources

- Many other sources
- Can apply same general approach
- Need insights into cause
- Need insights into restrictions to solve
- No general algorithm
- Process:
- Stratify
- Prove sublanguages disjoint
- Prove union of new sublanguages give old language
- Method: Invariants and Induction

