

## 3.5

### Supplemental: DFA philosophy

# A finite program can be simulated by a DFA...

- 1 Finite program = a program that uses a prespecified bounded amount of memory.
- 2 Given DFA and input, easy to decide if DFA accepts input.
- 3 A finite program is a DFA!  
# of states of memory of a finite program = finite.  
# states  $\approx 2^{\#}$  of memory bits used by program
- 4 Program using 1K memory = has...
- 5 Turing halting theorem: Not possible (in general) to decide if a program stops on an input.
- 6 DFA  $\neq$  programs.

# A finite program can be simulated by a DFA...

- 1 Finite program = a program that uses a prespecified bounded amount of memory.
- 2 Given **DFA** and input, easy to decide if **DFA** accepts input.
- 3 A finite program is a **DFA**!  
# of states of memory of a finite program = finite.  
# states  $\approx 2^{\#}$  of memory bits used by program
- 4 Program using **1K** memory = has...
- 5 Turing halting theorem: Not possible (in general) to decide if a program stops on an input.
- 6 **DFA**  $\neq$  programs.

# A finite program can be simulated by a DFA...

- 1 Finite program = a program that uses a prespecified bounded amount of memory.
- 2 Given **DFA** and input, easy to decide if **DFA** accepts input.
- 3 A finite program is a **DFA!**  
# of states of memory of a finite program = finite.  
# states  $\approx 2^{\#}$  of memory bits used by program
- 4 Program using  $1K$  memory = has...
- 5 Turing halting theorem: Not possible (in general) to decide if a program stops on an input.
- 6 **DFA**  $\neq$  programs.

# A finite program can be simulated by a DFA...

- 1 Finite program = a program that uses a prespecified bounded amount of memory.
- 2 Given **DFA** and input, easy to decide if **DFA** accepts input.
- 3 A finite program is a **DFA**!  
# of states of memory of a finite program = finite.  
# states  $\approx 2^{\# \text{ of memory bits used by program}}$
- 4 Program using **1K** memory = has...
- 5 Turing halting theorem: Not possible (in general) to decide if a program stops on an input.
- 6 **DFA**  $\neq$  programs.

# A finite program can be simulated by a DFA...

- 1 Finite program = a program that uses a prespecified bounded amount of memory.
- 2 Given **DFA** and input, easy to decide if **DFA** accepts input.
- 3 A finite program is a **DFA**!  
# of states of memory of a finite program = finite.  
# states  $\approx 2^{\# \text{ of memory bits used by program}}$
- 4 Program using **1K** memory = has...
- 5 Turing halting theorem: Not possible (in general) to decide if a program stops on an input.
- 6 **DFA**  $\neq$  programs.

# A finite program can be simulated by a DFA...

- 1 Finite program = a program that uses a prespecified bounded amount of memory.
- 2 Given **DFA** and input, easy to decide if **DFA** accepts input.
- 3 A finite program is a **DFA**!  
# of states of memory of a finite program = finite.  
# states  $\approx 2^{\# \text{ of memory bits used by program}}$
- 4 Program using **1K** memory = has...
- 5 Turing halting theorem: Not possible (in general) to decide if a program stops on an input.
- 6 **DFA**  $\neq$  programs.

# But universe is finite...

- 1 Estimate # of atoms in the universe is  $10^{82}$ .
- 2 Assuming each atom can store only finite number of bits.
- 3 So... number of states of the universe is finite!
- 4 So... All programs in this universe are DFAs.
- 5 Checkmate Mate!
- 6 What is all this nonsense?



# But universe is finite...

- 1 Estimate # of atoms in the universe is  $10^{82}$ .
- 2 Assuming each atom can store only finite number of bits.
- 3 So... number of states of the universe is finite!
- 4 So... All programs in this universe are DFAs.
- 5 Checkmate Mate!
- 6 What is all this nonsense?

# But universe is finite...

- 1 Estimate # of atoms in the universe is  $10^{82}$ .
- 2 Assuming each atom can store only finite number of bits.
- 3 So... number of states of the universe is finite!
- 4 So... All programs in this universe are DFAs.
- 5 Checkmate Mate!
- 6 What is all this nonsense?

# But universe is finite...

- 1 Estimate # of atoms in the universe is  $10^{82}$ .
- 2 Assuming each atom can store only finite number of bits.
- 3 So... number of states of the universe is finite!
- 4 So... All programs in this universe are **DFA**s.
- 5 Checkmate Mate!
- 6 What is all this nonsense?

# But universe is finite...

- 1 Estimate # of atoms in the universe is  $10^{82}$ .
- 2 Assuming each atom can store only finite number of bits.
- 3 So... number of states of the universe is finite!
- 4 So... All programs in this universe are **DFA**s.
- 5 Checkmate Mate!
- 6 What is all this nonsense?

# But universe is finite...

- 1 Estimate # of atoms in the universe is  $10^{82}$ .
- 2 Assuming each atom can store only finite number of bits.
- 3 So... number of states of the universe is finite!
- 4 So... All programs in this universe are **DFA**s.
- 5 Checkmate Mate!
- 6 What is all this nonsense?

# So what is going on...

- 1 Theory models the world. (Oversimplifies it.)
- 2 Make it possible to think about it.
- 3 There are cases where theory does not model the world well.
- 4 Know when to apply the theory.
- 5 Reject statements that are correct but not useful.
- 6 Really Large finite numbers are

# THE END

...

# (for now)