Algorithms & Models of Computation CS/ECE 374, Fall 2020

4.3 Closure Properties of NFAs

Closure properties of NFAs

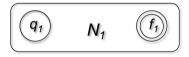
Are the class of languages accepted by NFAs closed under the following operations?

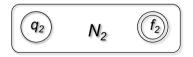
- union
- intersection
- concatenation
- Kleene star
- complement

Closure under union

Theorem

For any two NFAs N_1 and N_2 there is a NFA N such that $L(N) = L(N_1) \cup L(N_2)$.

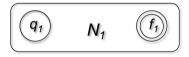


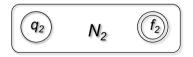


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Closure under concatenation

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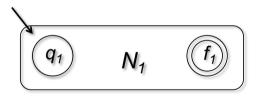
Closure under concatenation

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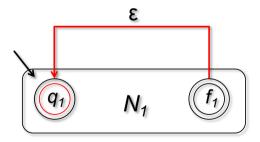
Theorem

For any NFA N_1 there is a NFA N such that $L(N) = (L(N_1))^*$.



Theorem

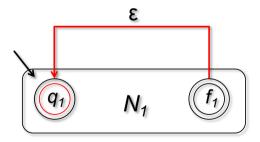
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Does not work! Why?

Theorem

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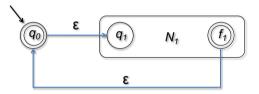


Does not work! Why?

Har-Peled (UIUC)

Theorem

For any NFA N_1 there is a NFA N such that $L(N) = (L(N_1))^*$.



THE END

(for now)

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