

Fav sitcom out of
Prof. Schatz's favorites

CS 340

Building Blocks 0b10
(Selection and Information Storage)

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Q1

~Code~
340



Updates



1. MP 2 - due next Tuesday.
2. HW 3 due next Thursday 1:59pm
 - a. Building Blocks
 - b. If you need help with gates (see video posted on campus wire and the website)
3. Exam 1 - September 23rd
 - a. Sign up now! By the 18th.

Tuesday - no class
mp0 - mp2



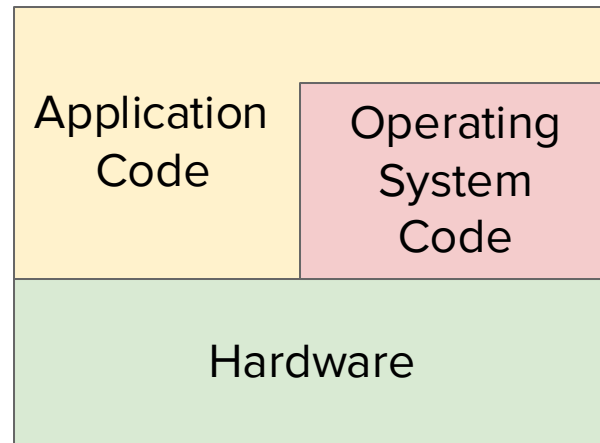
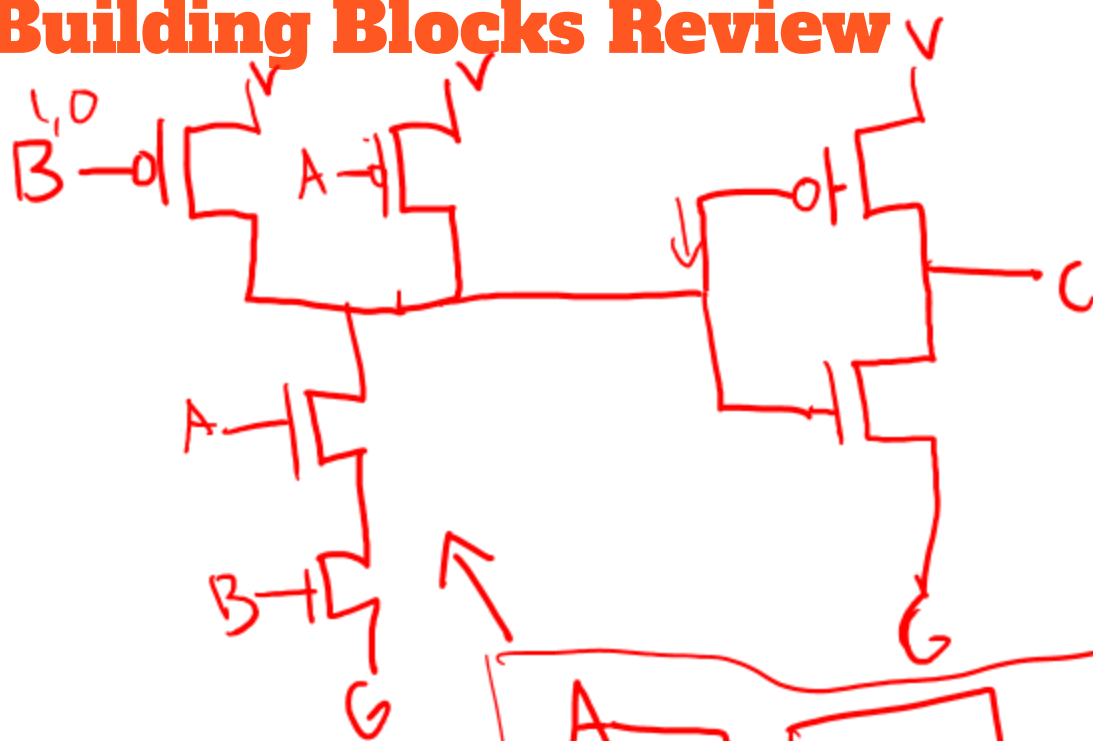
Building Blocks Ob10

Today's LGs:

- Be convinced you can use gates to build calculations and selection.
- Have a brief understanding of why we use base-2 for storage
- Be able to articulate that
 - Computers have different types of storage hardware
 - We utilize the different types of storage by using caching
 - Caching algorithms rely on spatial and temporal locality
- Be able to identify if code is cache friendly or not



Building Blocks Review



Building Blocks

1. Circuit Basics

2. Gates

3. Binary

4. Arithmetic Computations

5. Selection

6. Storage

Arithmetic Calculations

Arithmetic Calculations in Logic

$$5 + 3 = 8 = z$$

$$x = 5 = \begin{array}{cccc} & & & \\ x_3 & x_2 & x_1 & x_0 \end{array}$$

$$y = 3 = \begin{array}{cccc} & & & \\ y_3 & y_2 & y_1 & y_0 \end{array}$$

$$\begin{array}{cccc} & 1 & 1 & 1 \\ 0 & 1 & 0 & 1 \\ + & 0 & 0 & 1 & 1 \\ \hline 1 & 0 & 0 & 0 \end{array}$$

$$\begin{array}{r|cccc} x & 0 & 1 & 0 & 1 \\ y & 0 & 0 & 1 & 1 \\ \hline z & 0 & 0 & 0 & 0 \\ \hline & z_3 & z_2 & z_1 & z_0 \end{array}$$

$$c \begin{array}{l} 0 \ 1 \ 1 \ 0 \\ c_1 \ c_0 \end{array}$$

$$z_0 = x_0 \wedge y_0$$

$$z_0 = 1 \wedge 1$$

$$z_0 = 0$$

$$z_i = c_i \wedge x_i \wedge y_i$$

$$c_{i+1} = (x_i \& y_i) \vee (c_i \& (x_i \vee y_i))$$

$$c_1 = x_0 \& y_0$$

$$c_1 = 1 \& 1 = 1$$

Arithmetic Calculations in Logic

$$Z_0 = x_0 \wedge y_0$$

$$C_1 = x_0 \oplus y_0$$

$$Z_i = C_i \wedge x_i \wedge y_i$$

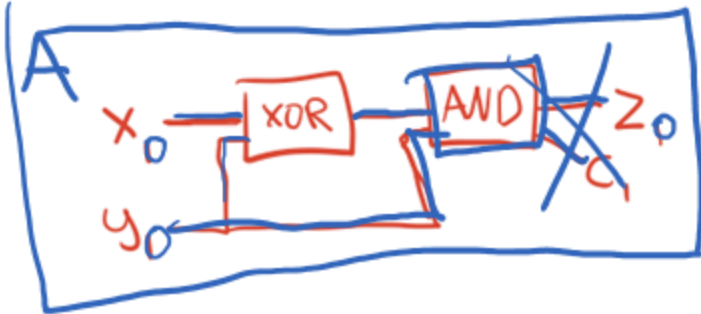
$$C_{i+1} = (x_i \oplus y_i) \vee (C_i \wedge (x_i \wedge y_i))$$

Arithmetic Calculations in Hardware

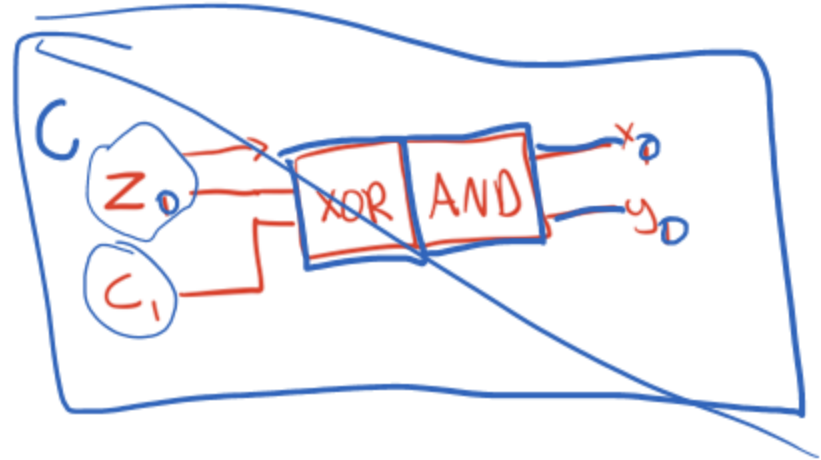
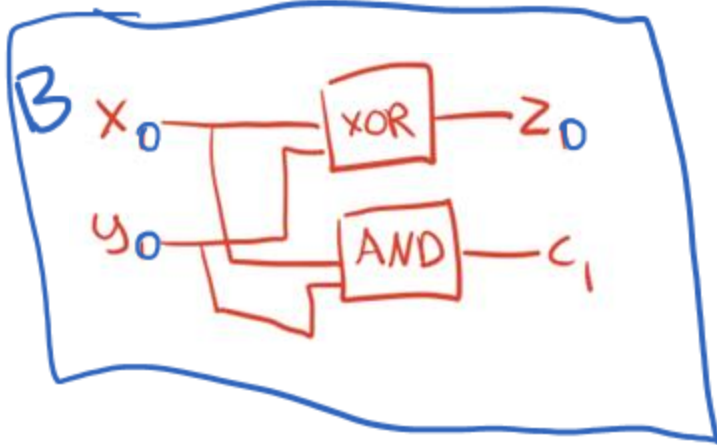
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Q2

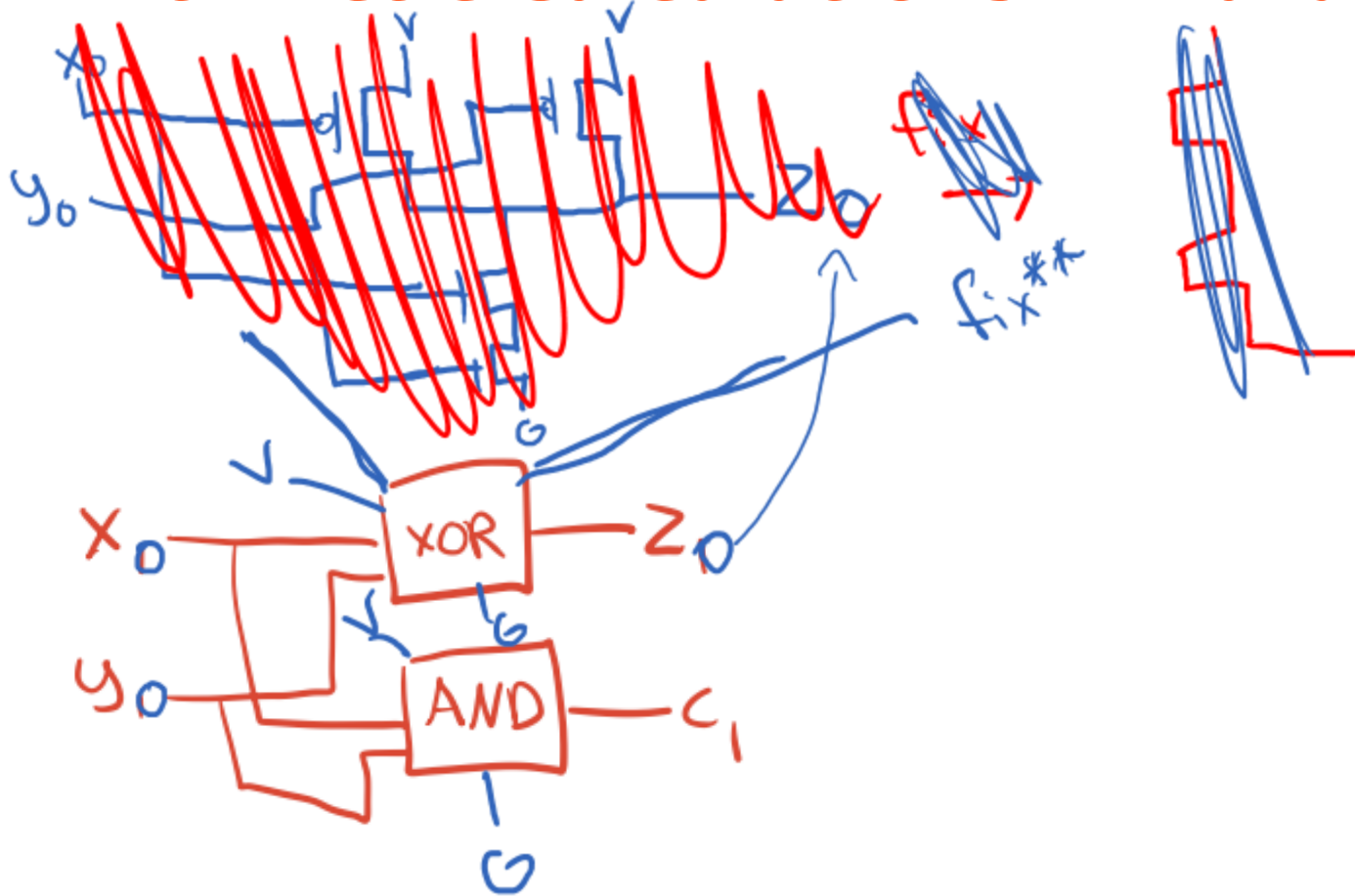
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$$z_0 = x_0 \wedge y_0$$
$$c_1 = x_0 \& y_0$$



Arithmetic Calculations in Hardware



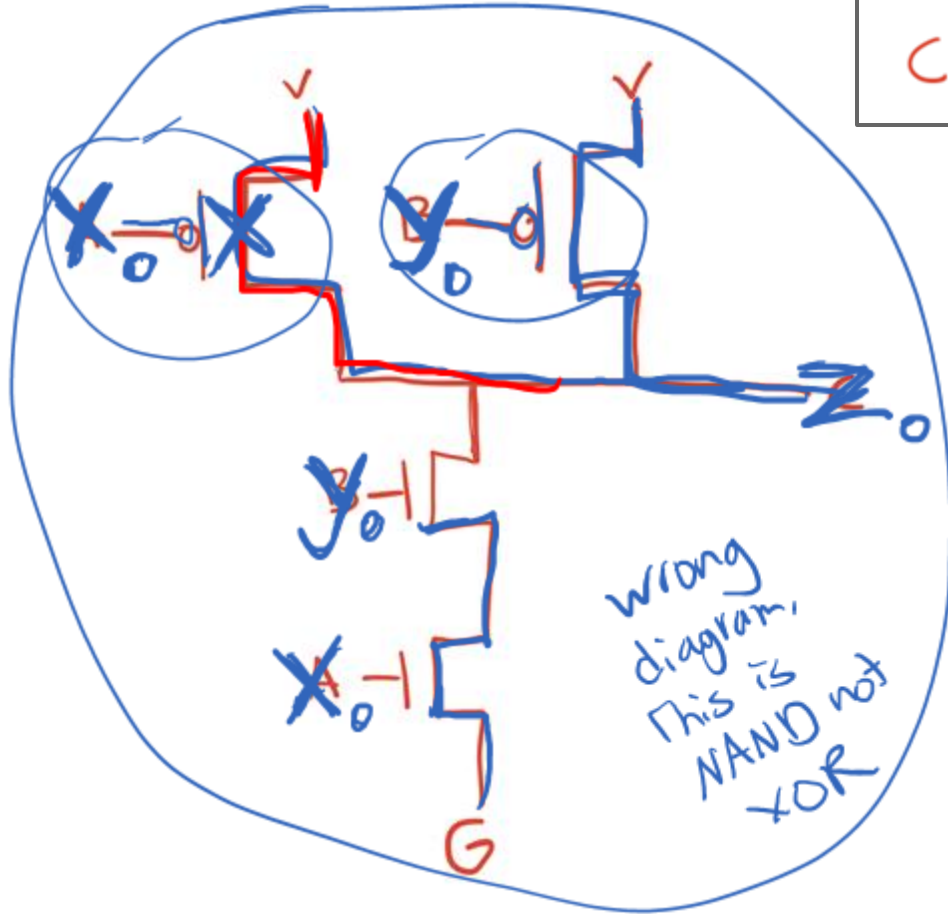
What is Z?

$$Z_0 = x_0 \wedge y_0$$
$$C_1 = x_0 \& y_0$$

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Q3

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wrong
diagram.
This is
NAND not
XOR

$$\begin{array}{c} x_0 \quad y_0 \\ 1+0 = Z_0? \\ \hline 0+0 = 1 \end{array}$$

Selection

MUX (sounds like ducks with an m)

$$\begin{matrix} 0 & 1 \\ a & b \\ 0 & 1 \end{matrix}$$

$$s = 0 \text{ or } 1$$

$$(\neg s \wedge a) \mid (s \wedge b)$$

if $s = 1$
 $= 1, b$

$$\begin{matrix} 0 & 1 \\ (0) & 1 \end{matrix}$$

What is the output?

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$$[a, b] \quad s = 0 \text{ or } 1$$
$$(\neg s \& a) | (s \& b) =$$

$$s = 0$$
$$\begin{bmatrix} 1 & 1 \\ A & B \end{bmatrix}$$

0 1

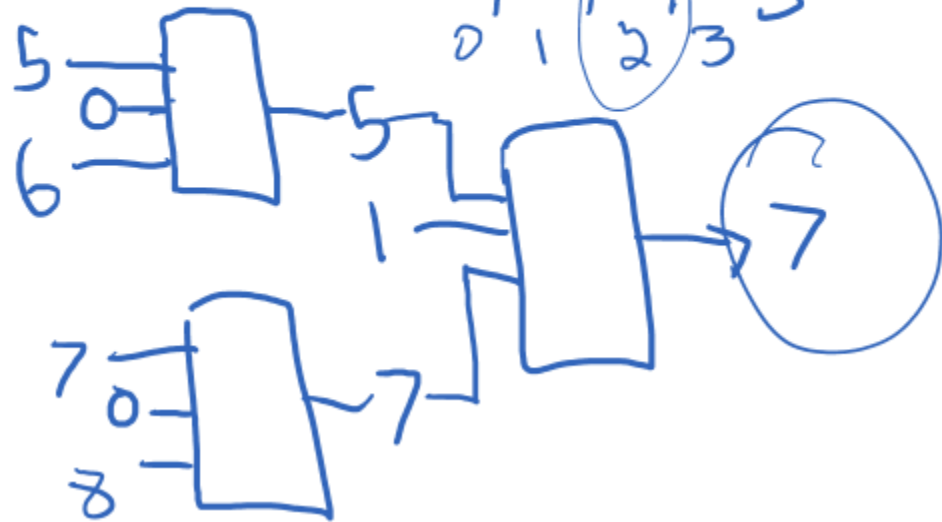
$$(1 \& 0) | (0 \& 1)$$
$$010 = 0$$

$$(1 \& 1) | (0 \& 1)$$
$$110 = 1$$

MUX can scale!

$[5, 6]$

$[5, 6, 7, 8]$

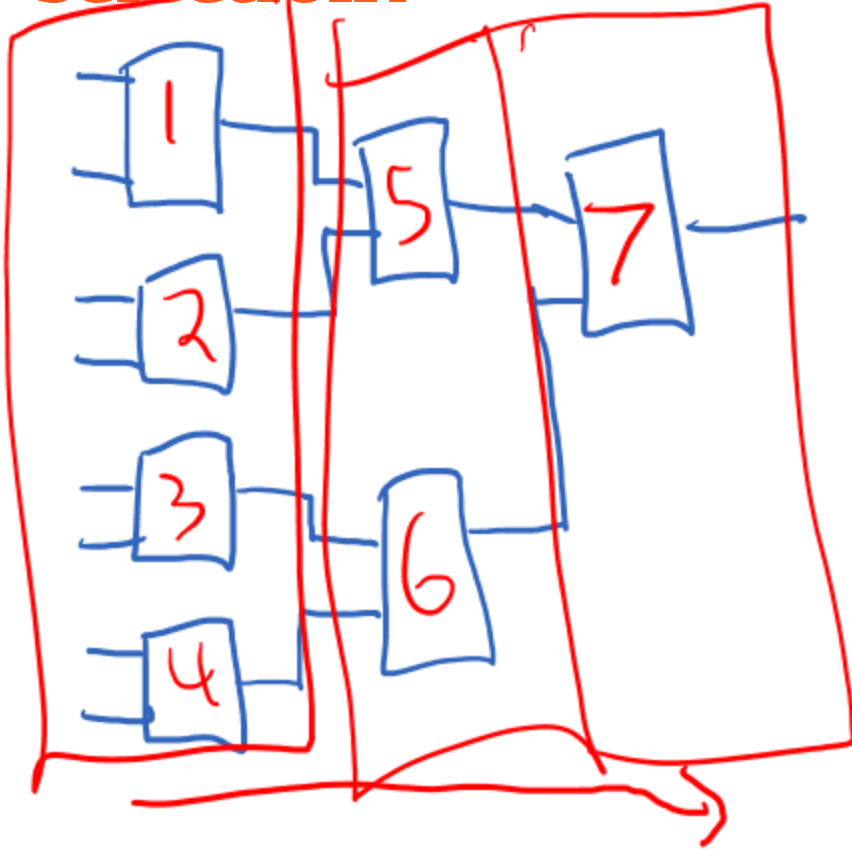


~~SA~~

~~SA~~

$S = 2 = 10_{10}$

How many 2-MUX for a 8 selection?



depth
= 3

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Q5

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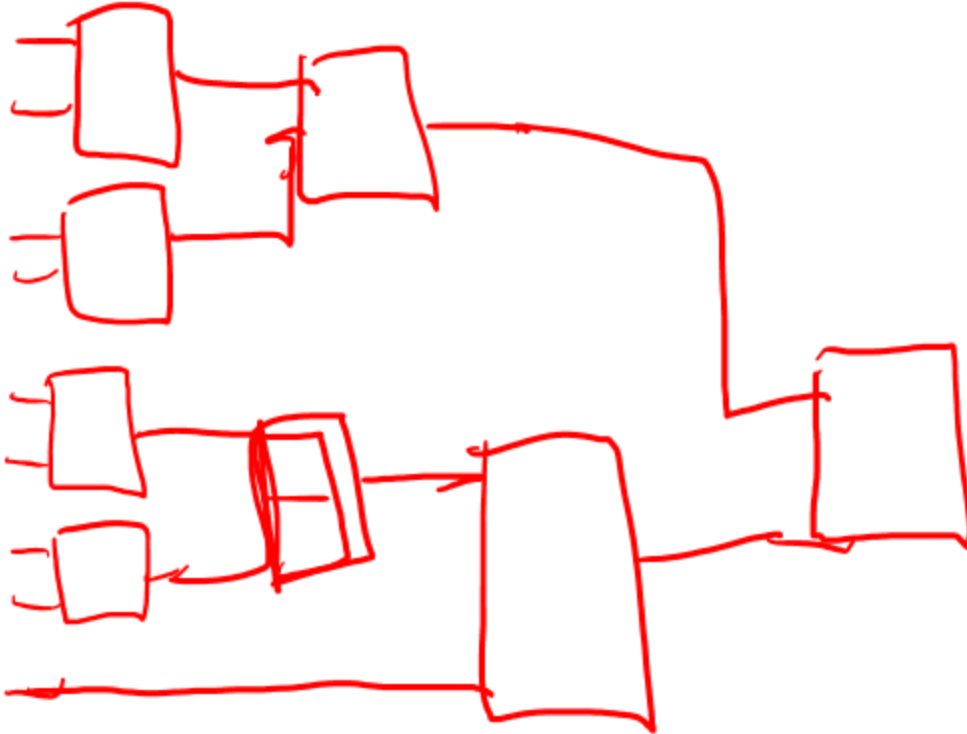
$$\log_2 16 = 4$$

Q6

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What depth of 2-MUX's for a 9 input selection?



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Q7

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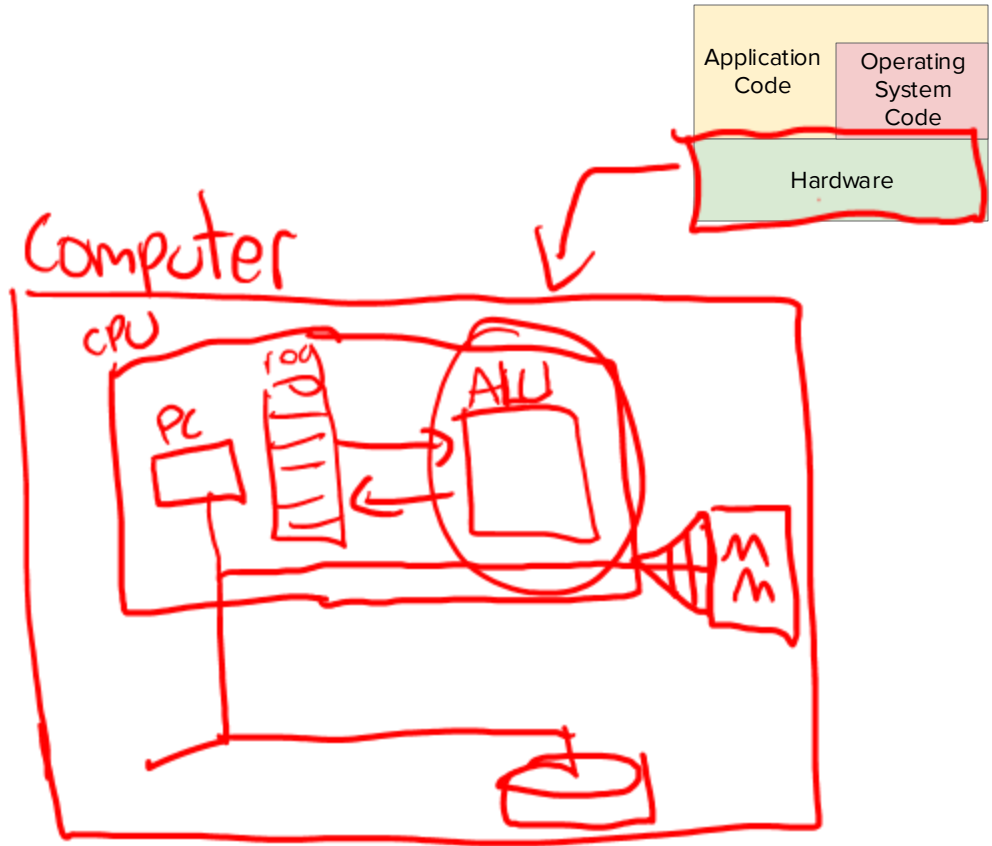
4

MUX Takeaways

selects 1 From many
more depth = bad
Slower

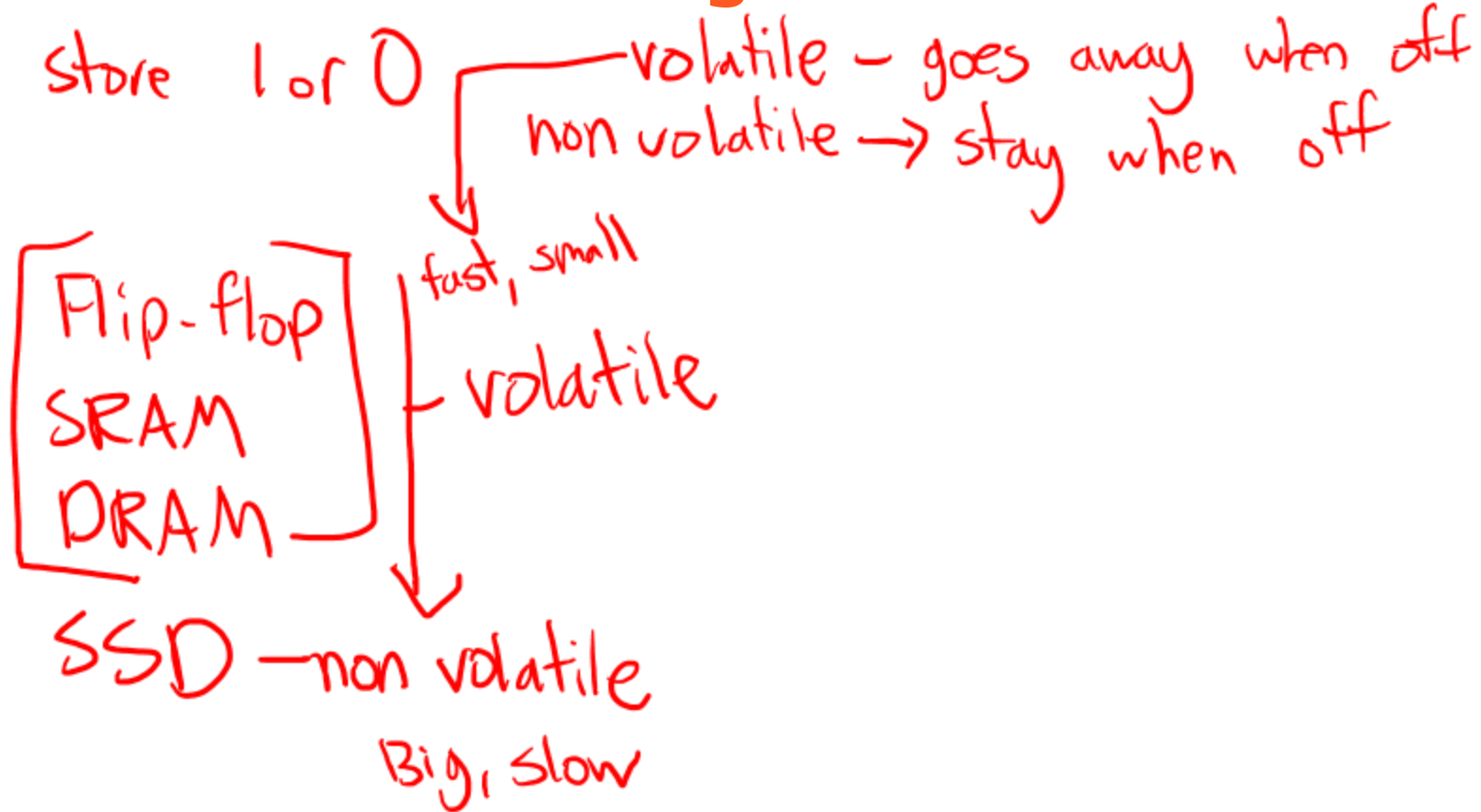
Summary Slide

1. Circuit Basics
2. Gates
3. Binary
4. Arithmetic Computations
5. Selection
- 6. Storage**



Storage

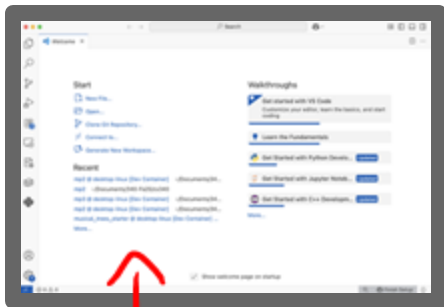
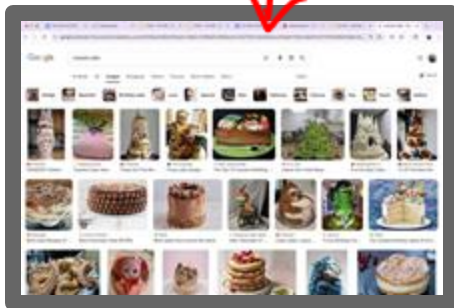
Hardware for Storing Information



Hardware for Storing Information



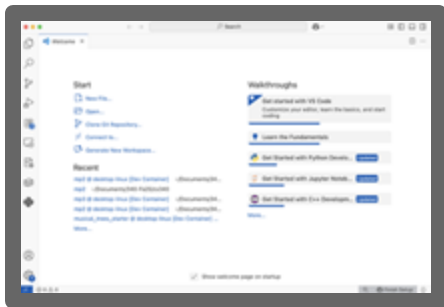
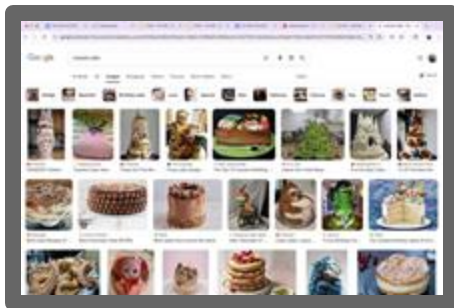
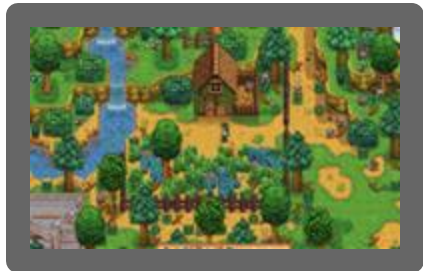
Caching RAM



slow
big



Caching RAM



what is most likely
reuse things

Locality

temporal

spatial

time

space

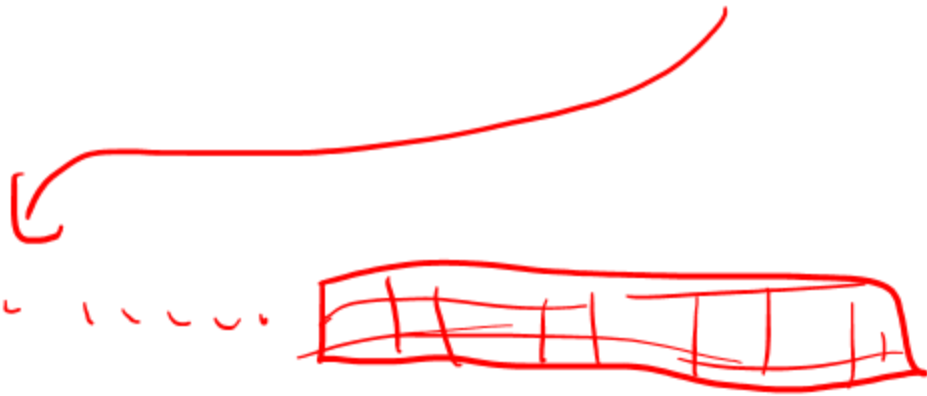
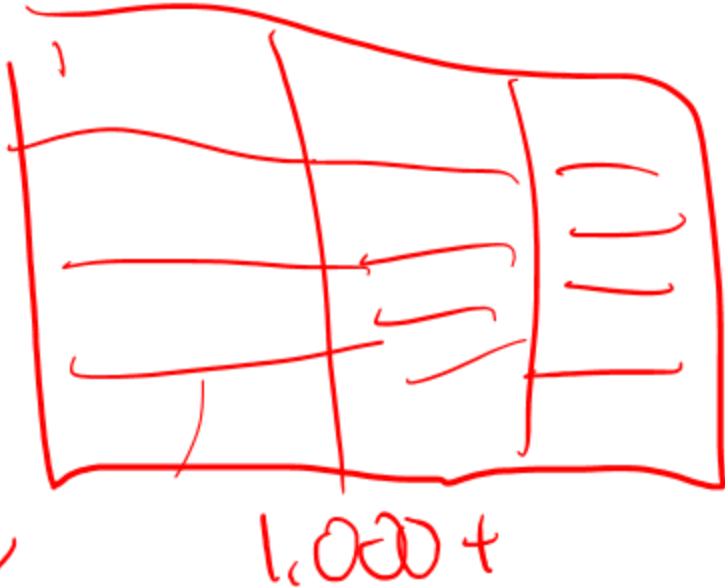
nearby
addresses



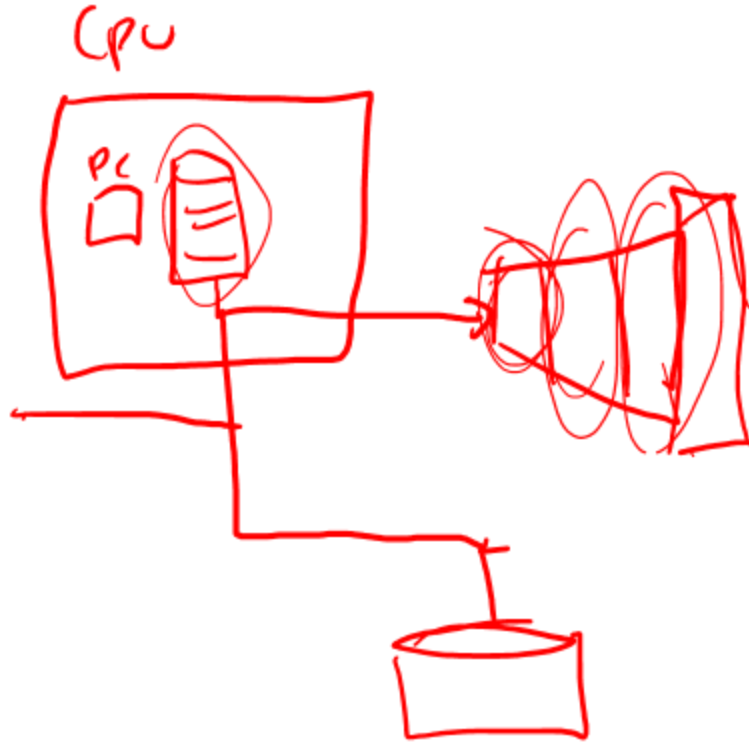
Caching - an algorithm for utilizing fast and small memory and ~~small~~^{slow} big memory. We keep copies in higher levels for quick access

Locality - the idea that computers often use nearby and similar information sequentially.
Local and temporal locality.

Library Example



Computer Information Storage



Can you change this code for better locality?

```
6  → int arr1[500];  
7  → int arr2[500];  
8  //add stuff to arrays  
9  int count = 0;  
10 → for(int i = 0 ; i < 500; i++){  
11   → if(arr1[i]%2 == 0) count++;  
12   → if(arr2[i]%2 == 0) count++;  
13 }
```



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for arr2[0] arr2[499]
*(arr2+0) *(arr2+499)
↓
arr2[0] arr2[499]

Can you change this code for better locality?

500 + 450

```

8   int doub[500][450];
9   //add stuff to doub
10  for(int col = 0; col < 450; col++){
11      for(int row = 0; row < 500; row++){
12          doub[row][col]++;
13      }
14  }

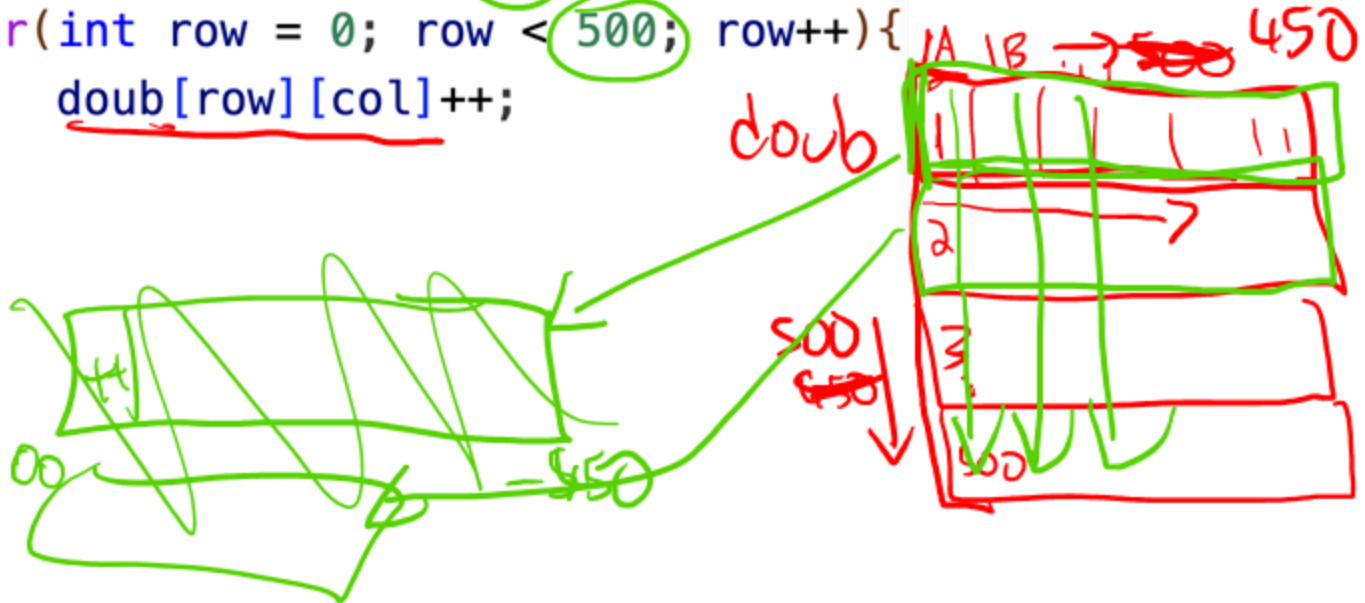
```

doub

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09

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Building Blocks

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