Clustering and network analysis of gene expression data

Chapter 11 in
Jonathan Pevsner,
Bioinformatics and Functional Genomics,

3rd edition

(Chapter 9 in 2nd edition)

Clustering in Matlab

Choices of distance metrics in clustergram(... 'RowPDistValue' ..., 'ColumnPDistValue' ...,)

Metric	Description
'euclidean'	Euclidean distance (default).
'seuclidean'	Standardized Euclidean distance. Each coordinate difference between rows in X is scaled by dividing by the corresponding element of the standard deviation S=nanstd(X). To specify another value for S, use D=pdist(X, 'seuclidean', S).
'cityblock'	City block metric.
'minkowski'	Minkowski distance. The default exponent is 2. To specify a different exponent, use $D = pdist(X, 'minkowski', P)$, where P is a scalar positive value of the exponent.
'chebychev'	Chebychev distance (maximum coordinate difference).
'mahalanobis'	Mahalanobis distance, using the sample covariance of X as computed by nancov. To compute the distance with a different covariance, use D = pdist(X, 'mahalanobis', C), where the matrix C is symmetric and positive definite.
'cosine'	One minus the cosine of the included angle between points (treated as vectors).
'correlation'	One minus the sample correlation between points (treated as sequences of values).
'spearman'	One minus the sample Spearman's rank correlation between observations (treated as sequences of values).
'hamming'	Hamming distance, which is the percentage of coordinates that differ.
'jaccard'	One minus the Jaccard coefficient, which is the percentage of nonzero coordinates that differ.
custom distance function	A distance function specified using @: D = pdist(X,@distfun) A distance function must be of form
	d2 = distfun(XI,XJ)
	taking as arguments a 1-by- n vector XI, corresponding to a single row of X, and an $m2$ -by- n matrix XJ, corresponding to multiple rows of X. distfun must accept a matrix XJ with an arbitrary number of rows. distfun must return an $m2$ -by-1 vector of distances d2, whose k th element is the distance between XI and XJ (k ,:).

Choices of hierarchical clustering algorithm in clustergram(...'linkage',...)

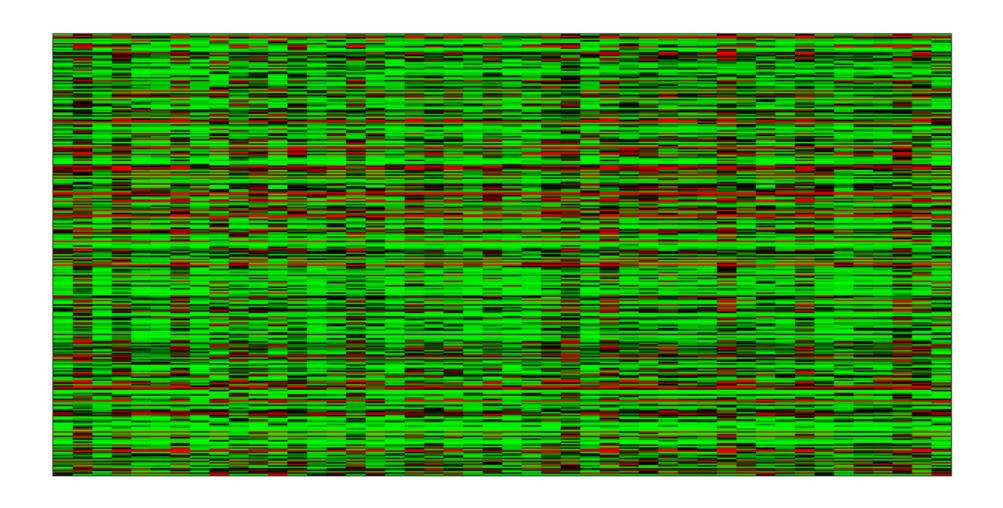
Х		Matrix with two or more rows. The rows represent observations, the columns represent categories or dimensions.				
method	Algorithm for con	Algorithm for computing distance between clusters.				
	Method	Description				
	'average'	Unweighted average distance (UPGMA)				
	'centroid'	Centroid distance (UPGMC), appropriate for Euclidean distances only				
	'complete'	Furthest distance				
	'median'	Weighted center of mass distance (WPGMC), appropriate for Euclidean distances only				
	'single'	Shortest distance				
	'ward'	Inner squared distance (minimum variance algorithm), appropriate for Euclidean distances only				
	'weighted'	'weighted' Weighted average distance (WPGMA)				
	Default: 'single	Default: 'single'				

Clustering group exercise

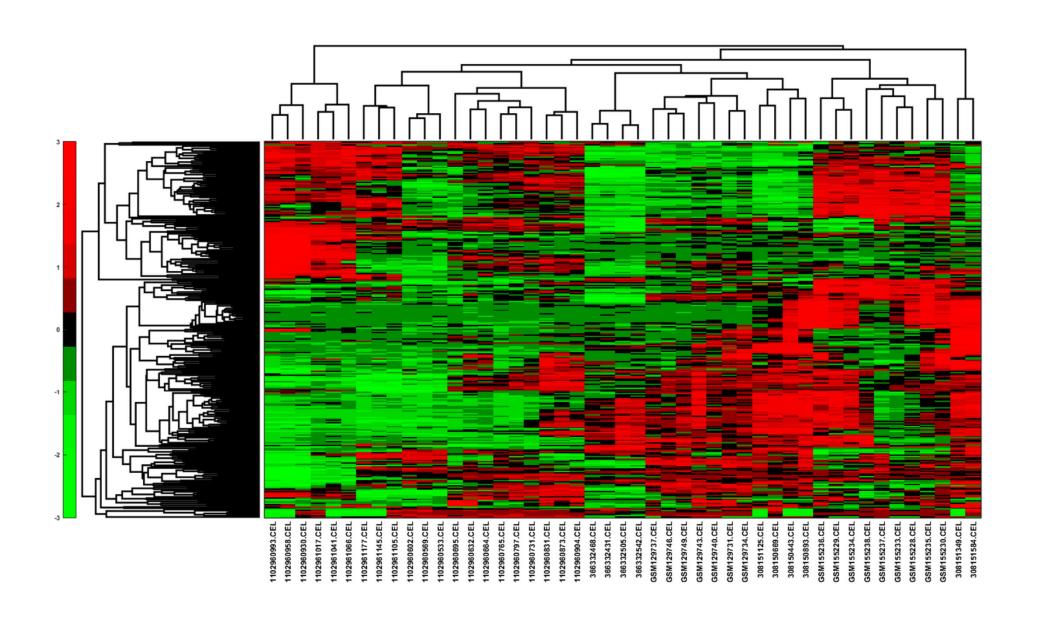
- Each group will analyze a cluster of genes identified in the T cell expression table
- Analyze the table of top 100 genes by variance in 47 samples
- Cluster them using:
 - Group 1: 'linkage', 'average', 'RowPDistValue', 'euclidean',
 - Group 2: 'linkage', 'average', 'RowPDistValue', 'cityblock',
 - Group 3: 'linkage', 'average', 'RowPDistValue', 'correlation',
 - Group 4: 'linkage', 'single', 'RowPDistValue', 'euclidean',
 - Group 5: 'linkage', 'single', 'RowPDistValue', 'cityblock',
 - Group 6: 'linkage', 'single', 'RowPDistValue', 'correlation',
- Use clustergram(..., 'Standardize','Row',
 (linkage', <u>as specified for your group,</u>
 (RowPDistValue' <u>as specified for your group,</u>
 (RowLabels',gene_names1,'ColumnLabels', array_names)

```
load expression_table.mat
gene_variation=std(exp_t')';
[a,b]=sort(gene variation,'descend');
ngenes=100;
exp_t1=exp_t(b(1:ngenes),:);
gene_names1=gene_names(b(1:ngenes));
%%% for group 1
CGobj1 = clustergram(exp t1,
'Standardize','Row',...
'RowLabels',
gene_names1,'ColumnLabels',array_names)
set(CGobj1,'RowLabels',gene_names1,'ColumnLab
els', array names, 'linkage',
'average','RowPDist','euclidean');
set(CGobj1,'RowLabels',gene_names1,'ColumnLab
els', array names, 'linkage',
'average', 'RowPDist', 'correlation');
```

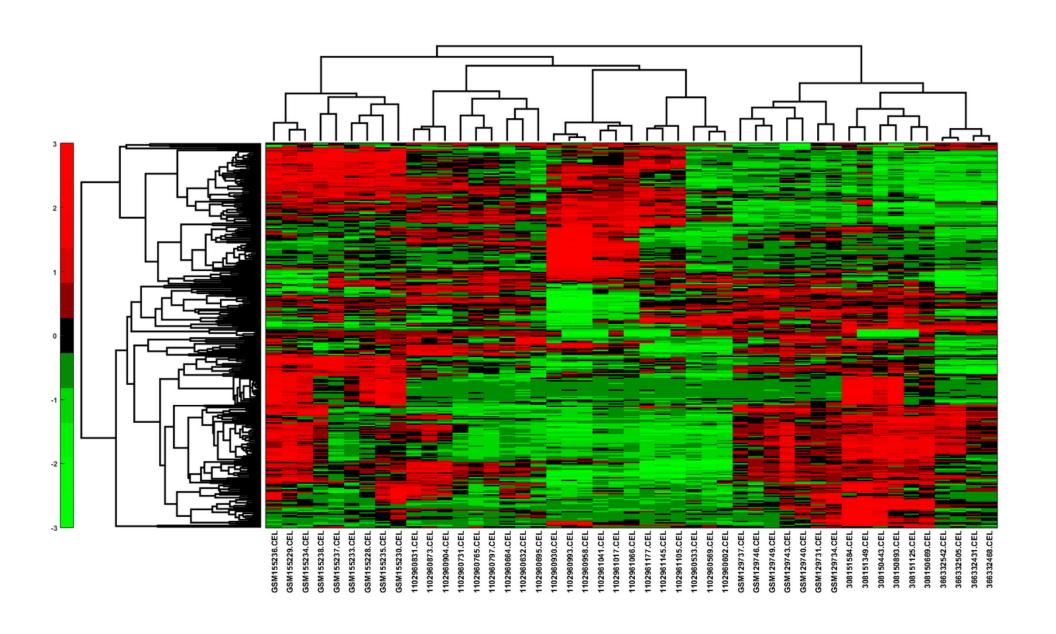
Before clustering



UPGMA hierarchical clustering, Euclidian distance



UPGMA hierarchical clustering, correlation distance



Search for shared biological functions

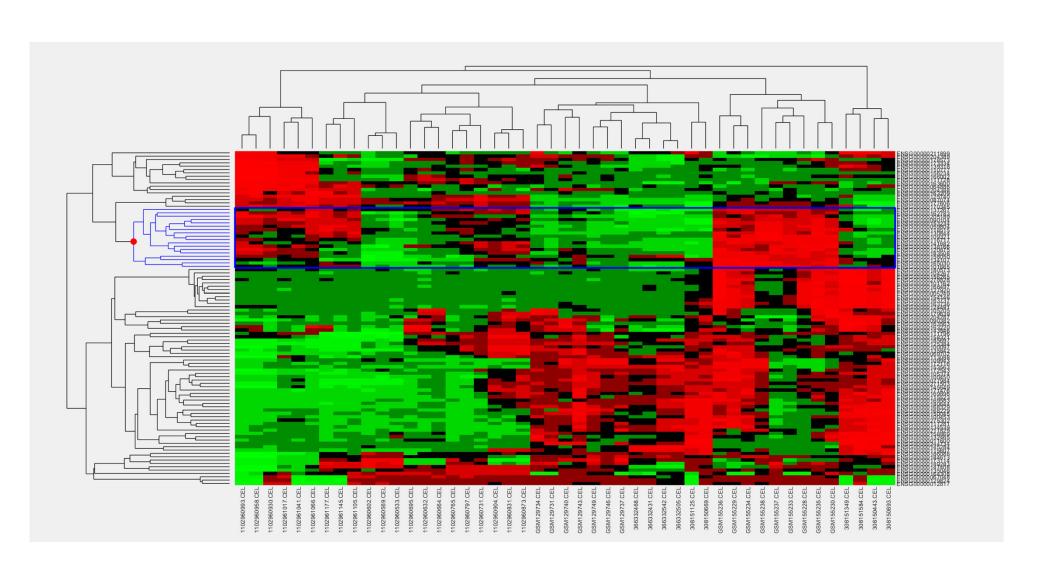
- copy the list of displayed genes
- go to "Start Analysis" on https://david.ncifcrf.gov/tools.jsp
- Paste genes from gene list displayed by Matlab into the box in the left panel of the website
- select ENSEMBL_GENE_ID and "gene list" radio button
- Click "Functional Annotation Clustering"
- Select groups in "Annotation Summary Results" which have many genes from your list. Definitely select "PUBMED_ID" and interaction databases like "Biogrid"
- First look at "Functional Annotation Chart" rectangular button below to display all overrepresented terms. Sort by "Benjamini" correction for multiple hypotheses testing
- Select "Functional Annotation Clustering" rectangular button below to display annotation results for gene list broken into multiple groups (clusters) each with related biological functions
- Write down the # of genes in the cluster and the top functions in two most interesting clusters

```
%%%
%Which biological functions are
overrepresented in different clusters?
%1) Pick a cluster:
%2) Select a node on the tree of rows,
%3) Right click
%4) Choose "export group info" into
the workspace
%5) Name it gene list
%Run the following two Matlab
commands to display genes
g1=gene_list.RowNodeNames;
for m=1:length(g1);
disp(g1{m});
end;
```

- % select ENSEMBL_GENE_ID and "gene list" radio button
- % Click "Functional Annotation Clustering"
- % Select groups in "Annotation Summary Results"
- % which have many genes from your list.
- % Definitely select "PUBMED_ID" and
- % interaction databases like "Biogrid"
- % First look at "Functional Annotation Chart" rectangular button below
- % to display all overrepresented terms.
- % Sort by "Benjamini" correction for multiple hypotheses testing
- % Select "Functional Annotation Clustering" rectangular button below
- % to display annotation results for gene list broken into multiple groups
- % (clusters) each with related biological functions
- % Write down the # of genes in the cluster and the top functions
- % in two most interesting clusters

Using options:

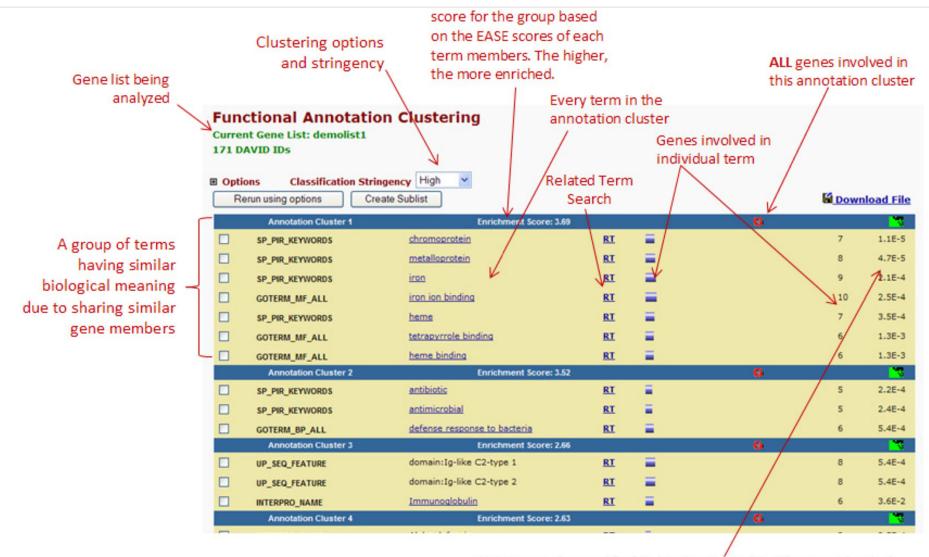
'linkage', 'average', 'RowPDistValue', 'euclidean',



54 chart records

Sublist	<u>Category</u>	<u>Term</u>	‡ RT	Genes	Count	<u>%</u>	<u>Benjamini</u>
	GOTERM_CC_DIRECT	nucleus	<u>RT</u>		16	88.9 8.1E-7	3.7E-5
	PIR_SUPERFAMILY	<u>dual specificity protein phosphatase (MAP kinase phosphatase)</u>	<u>RT</u>	_	3	16.7 4.0E-5	8.0E-5
	GOTERM_MF_DIRECT	protein tyrosine/threonine phosphatase activity	<u>RT</u>		3	16.7 3.4E-5	1.3E-3
	GOTERM_MF_DIRECT	MAP kinase tyrosine phosphatase activity	<u>RT</u>		3	16.7 3.4E-5	1.3E-3
	GOTERM_MF_DIRECT	MAP kinase tyrosine/serine/threonine phosphatase activity	<u>RT</u>		3	16.7 5.9E-5	1.5E-3
	INTERPRO	Mitogen-activated protein (MAP) kinase phosphatase	<u>RT</u>		3	16.7 3.3E-5	1.9E-3
	SMART	RHOD	<u>RT</u>		3	16.7 2.5E-4	4.8E-3
	INTERPRO	Rhodanese-like domain	<u>RT</u>	_	3	16.7 2.2E-4	6.2E-3
	SMART	<u>DSPc</u>	<u>RT</u>		3	16.7 8.4E-4	8.0E-3
	INTERPRO	<u>Dual specificity phosphatase, catalytic domain</u>	<u>RT</u>		3	16.7 6.0E-4	9.2E-3
	INTERPRO	<u>Dual specificity phosphatase, subgroup, catalytic domain</u>	<u>RT</u>		3	16.7 6.6E-4	9.2E-3
	GOTERM_BP_DIRECT	endoderm formation	<u>RT</u>	_	3	16.7 5.6E - 5	1.1E - 2
	UP_KW_CELLULAR_COMPONENT	<u>Nucleus</u>	<u>RT</u>		13	72.2 1.5E-3	1.3E-2
	SMART	PTPc motif	<u>RT</u>	_	3	16.7 2.3E-3	1.5E-2
	GOTERM_MF_DIRECT	phosphoprotein phosphatase activity	<u>RT</u>		3	16.7 8.0E-4	1.5E-2
	INTERPRO	Protein-tyrosine phosphatase, catalytic	<u>RT</u>		3	16.7 1.4E-3	1.6E-2
	UP_KW_PTM	<u>Ubl conjugation</u>	<u>RT</u>		7	38.9 4.5E-3	1.9E-2
	UP_KW_PTM	<u>Isopeptide bond</u>	<u>RT</u>		6	33.3 5.4E-3	1.9E-2
	INTERPRO	Protein-tyrosine phosphatase, active site	<u>RT</u>		3	16.7 2.1E-3	2.0E-2
	INTERPRO	Protein-tyrosine/Dual specificity phosphatase	<u>RT</u>	_	3	16.7 2.8E-3	2.3E-2
	UP_SEQ_FEATURE	DOMAIN:Rhodanese	<u>RT</u>		3	16.7 1.9E-4	2.4E-2
	KEGG_PATHWAY	MAPK signaling pathway	<u>RT</u>		5	27.8 5.9E-4	2.8E-2
	GOTERM_MF_DIRECT	myosin phosphatase activity	<u>RT</u>		3	16.7 2.4E-3	3.6E-2
	GOTERM_MF_DIRECT	protein tyrosine phosphatase activity	<u>RT</u>		3	16.7 4.2E-3	5.3E-2
	GOTERM_CC_DIRECT	nucleoplasm	<u>RT</u>		10	55.6 2.3E-3	5.4E-2
	GOTERM_BP_DIRECT	negative regulation of MAPK cascade	<u>RT</u>		3	16.7 7.0E-4	6.8E-2

Mark Download File



EASE Score, the modified Fisher Exact P-Value. They are identical to that in the Chart Report. The smaller, the more enriched.

Help and Manual

Current Gene List: List_3

Current Background: Homo sapiens

18 DAVID IDs

■ Options Classification Stringency Medium ∨

Rerun using options

Create Sublist

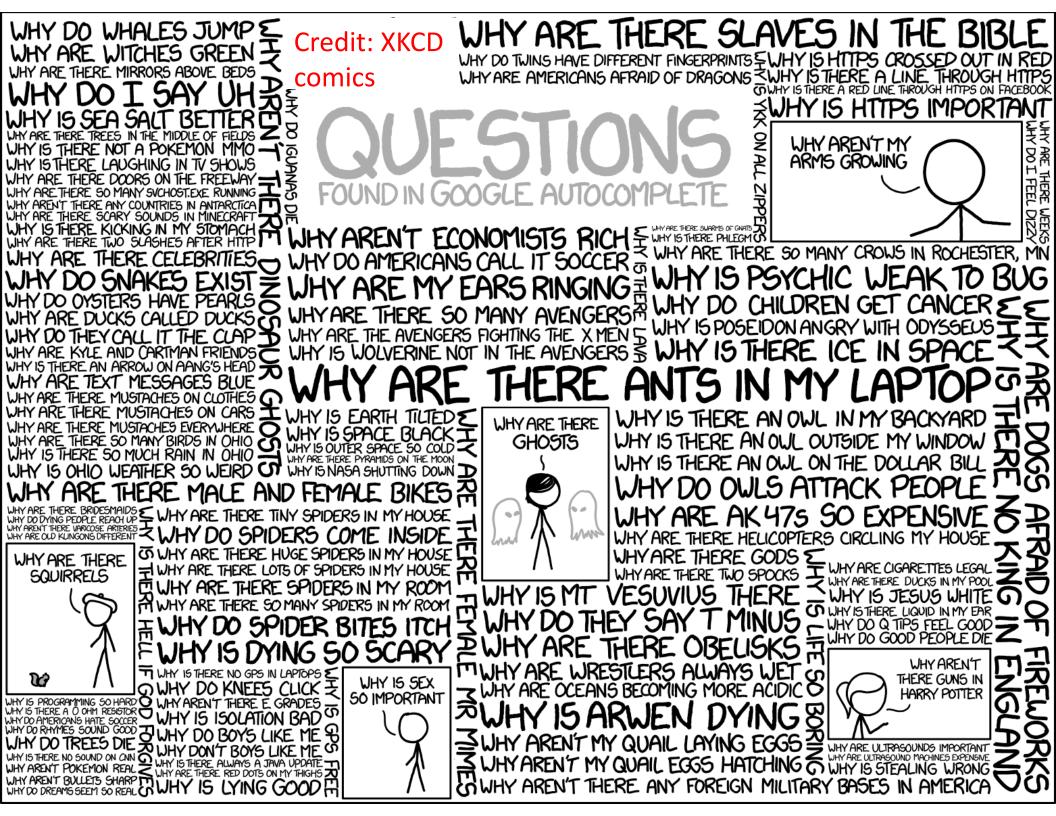
25 Cluster(s)

	Down	load	File
--	------	------	------

Annotatio	n Cluster 1	Enrichment Score: 5.2	G	To the second se	Count	P_Value	Benjamini
	DISGENET	Juvenile arthritis	<u>RT</u>		7	1.5E-8	4.7E-7
	DISGENET	Juvenile psoriatic arthritis	<u>RT</u>		7	1.5E-8	4.7E-7
	DISGENET	Polyarthritis, Juvenile, Rheumatoid Factor Negative	<u>RT</u>		7	1.5E-8	4.7E-7
	DISGENET	Polyarthritis, Juvenile, Rheumatoid Factor Positive	<u>RT</u>		7	1.5E-8	4.7E-7
	DISGENET	Juvenile-Onset Still Disease	<u>RT</u>		7	1.8E-8	4.7E-7
	KEGG_PATHWAY	MAPK signaling pathway	<u>RT</u>		5	5.9E-4	2.8E-2
	BIOGRID_INTERACTION	mitogen-activated protein kinase 1(MAPK1)	<u>RT</u>		4	3.8E-3	1.0E0
	WIKIPATHWAYS	MAPK signaling pathway	<u>RT</u>		3	5.8E-2	6.9E-1
	GAD_DISEASE_CLASS	UNKNOWN	<u>RT</u>		5	1.5E-1	9.9E-1
Annotatio	n Cluster 2	Enrichment Score: 2.83		- III	Count	P_Value	Benjamini
	INTERPRO	Mitogen-activated protein (MAP) kinase phosphatase	<u>RT</u>		3	3.3E-5	1.9E-3
	GOTERM_MF_DIRECT	protein tyrosine/threonine phosphatase activity	<u>RT</u>	_	3	3.4E-5	1.3E-3
	GOTERM_MF_DIRECT	MAP kinase tyrosine phosphatase activity	<u>RT</u>	_	3	3.4E-5	1.3E-3
	PIR_SUPERFAMILY	<u>dual specificity protein phosphatase (MAP kinase phosphatase)</u>	<u>RT</u>	=	3	4.0E-5	8.0E-5
	GOTERM_BP_DIRECT	endoderm formation	<u>RT</u>		3	5.6E-5	1.1E-2
	GOTERM_MF_DIRECT	MAP kinase tyrosine/serine/threonine phosphatase activity	<u>RT</u>	=	3	5.9E-5	1.5E-3
	PUBMED_ID	27880917	<u>RT</u>	_	4	1.7E-4	2.5E-2
	UP_SEQ_FEATURE	DOMAIN: Rhodanese	<u>RT</u>		3	1.9E-4	2.4E-2
	INTERPRO	Rhodanese-like domain	<u>RT</u>	_	3	2.2E-4	6.2E-3
	SMART	RHOD	RT		3	2.5E-4	4.8E-3

					:		
Annotatio	on Cluster 3	Enrichment Score: 2.43	G	<u> </u>	Count	P_Value	Benjamini
	DISGENET	Arsenic Poisoning, Inorganic	<u>RT</u>		3	3.5E-3	4.6E-2
	DISGENET	Nervous System, Organic Arsenic Poisoning	<u>RT</u>	_	3	3.5E-3	4.6E-2
	DISGENET	Arsenic Poisoning	<u>RT</u>	_	3	3.5E-3	4.6E-2
	DISGENET	Arsenic Encephalopathy	<u>RT</u>		3	3.5E-3	4.6E-2
	DISGENET	Arsenic Induced Polyneuropathy	<u>RT</u>	_	3	3.5E-3	4.6E-2
	DISGENET	Dermatologic disorders	<u>RT</u>	_	3	5.1E-3	5.6E-2
Annotatio	on Cluster 4	Enrichment Score: 2.26	G	in the second se	Count	P_Value	Benjamini
	PUBMED_ID	<u>19322201</u>	<u>RT</u>		7	1.3E-8	5.9E-6
	BIOGRID_INTERACTION	ELAV like RNA binding protein 1(ELAVL1)	<u>RT</u>		7	4.4E-3	1.0E0
	UCSC_TFBS	СЕВРА	<u>RT</u>		7	1.8E-1	1.0E0
	UCSC_TFBS	CDPCR3HD	<u>RT</u>		7	6.5E-1	1.0E0
	UCSC_TFBS	FOXD3	<u>RT</u>		5	7.4E-1	1.0E0
Annotatio	on Cluster 5	Enrichment Score: 2.14	G	The state of the s	Count	P_Value	Benjamini
	GOTERM_BP_DIRECT	negative regulation of transcription from RNA polymerase II promoter	<u>RT</u>		6	1.4E-3	9.1E-2
	BIOGRID_INTERACTION	retinoid X receptor alpha(RXRA)	<u>RT</u>		3	6.1E-3	1.0E0
	GOTERM_MF_DIRECT	protein heterodimerization activity	<u>RT</u>		3	4.5E-2	3.7E-1
Annotatio	on Cluster 6	Enrichment Score: 1.95		in the second se	Count	P_Value	Benjamini
	REACTOME_PATHWAY	Generic Transcription Pathway	<u>RT</u>		7	2.8E-3	1.7E-1
	REACTOME_PATHWAY	RNA Polymerase II Transcription	<u>RT</u>		7	4.6E-3	1.7E-1
	REACTOME_PATHWAY	Gene expression (Transcription)	<u>RT</u>		7	8.2E-3	2.0E-1
	GAD_DISEASE_CLASS	UNKNOWN	<u>RT</u>		5	1.5E-1	9.9E-1
Annotatio	on Cluster 7	Enrichment Score: 1.76			Count	P_Value	Benjamini
	PUBMED_ID	<u>18029348</u>	<u>RT</u>		6	1.8E-5	3.4E-3
	UP_KW_PTM	<u>Isopeptide bond</u>	<u>RT</u>		6	5.4E-3	1.9E-2
	PUBMED_ID	<u>15342556</u>	<u>RT</u>		3	7.9E-3	4.8E-1
	PUBMED_ID	<u>26496610</u>	<u>RT</u>		3	1.0E-1	1.0E0
	GOTERM_MF_DIRECT	metal ion binding	<u>RT</u>		4	4.5E-1	1.0E0
	UCSC_TFBS	TAL1ALPHAE47	RT	_	3	7.9E-1	1.0E0

					:		
Annotatio	on Cluster 3	Enrichment Score: 2.43	G	<u> </u>	Count	P_Value	Benjamini
	DISGENET	Arsenic Poisoning, Inorganic	<u>RT</u>		3	3.5E-3	4.6E-2
	DISGENET	Nervous System, Organic Arsenic Poisoning	<u>RT</u>	_	3	3.5E-3	4.6E-2
	DISGENET	Arsenic Poisoning	<u>RT</u>	_	3	3.5E-3	4.6E-2
	DISGENET	Arsenic Encephalopathy	<u>RT</u>		3	3.5E-3	4.6E-2
	DISGENET	Arsenic Induced Polyneuropathy	<u>RT</u>	_	3	3.5E-3	4.6E-2
	DISGENET	Dermatologic disorders	<u>RT</u>	_	3	5.1E-3	5.6E-2
Annotatio	on Cluster 4	Enrichment Score: 2.26	G	in the second se	Count	P_Value	Benjamini
	PUBMED_ID	<u>19322201</u>	<u>RT</u>		7	1.3E-8	5.9E-6
	BIOGRID_INTERACTION	ELAV like RNA binding protein 1(ELAVL1)	<u>RT</u>		7	4.4E-3	1.0E0
	UCSC_TFBS	СЕВРА	<u>RT</u>		7	1.8E-1	1.0E0
	UCSC_TFBS	CDPCR3HD	<u>RT</u>		7	6.5E-1	1.0E0
	UCSC_TFBS	FOXD3	<u>RT</u>		5	7.4E-1	1.0E0
Annotatio	on Cluster 5	Enrichment Score: 2.14	G	The state of the s	Count	P_Value	Benjamini
	GOTERM_BP_DIRECT	negative regulation of transcription from RNA polymerase II promoter	<u>RT</u>		6	1.4E-3	9.1E-2
	BIOGRID_INTERACTION	retinoid X receptor alpha(RXRA)	<u>RT</u>		3	6.1E-3	1.0E0
	GOTERM_MF_DIRECT	protein heterodimerization activity	<u>RT</u>		3	4.5E-2	3.7E-1
Annotatio	on Cluster 6	Enrichment Score: 1.95		in the second se	Count	P_Value	Benjamini
	REACTOME_PATHWAY	Generic Transcription Pathway	<u>RT</u>		7	2.8E-3	1.7E-1
	REACTOME_PATHWAY	RNA Polymerase II Transcription	<u>RT</u>		7	4.6E-3	1.7E-1
	REACTOME_PATHWAY	Gene expression (Transcription)	<u>RT</u>		7	8.2E-3	2.0E-1
	GAD_DISEASE_CLASS	UNKNOWN	<u>RT</u>		5	1.5E-1	9.9E-1
Annotatio	on Cluster 7	Enrichment Score: 1.76			Count	P_Value	Benjamini
	PUBMED_ID	<u>18029348</u>	<u>RT</u>		6	1.8E-5	3.4E-3
	UP_KW_PTM	<u>Isopeptide bond</u>	<u>RT</u>		6	5.4E-3	1.9E-2
	PUBMED_ID	<u>15342556</u>	<u>RT</u>		3	7.9E-3	4.8E-1
	PUBMED_ID	<u>26496610</u>	<u>RT</u>		3	1.0E-1	1.0E0
	GOTERM_MF_DIRECT	metal ion binding	<u>RT</u>		4	4.5E-1	1.0E0
	UCSC_TFBS	TAL1ALPHAE47	RT	_	3	7.9E-1	1.0E0

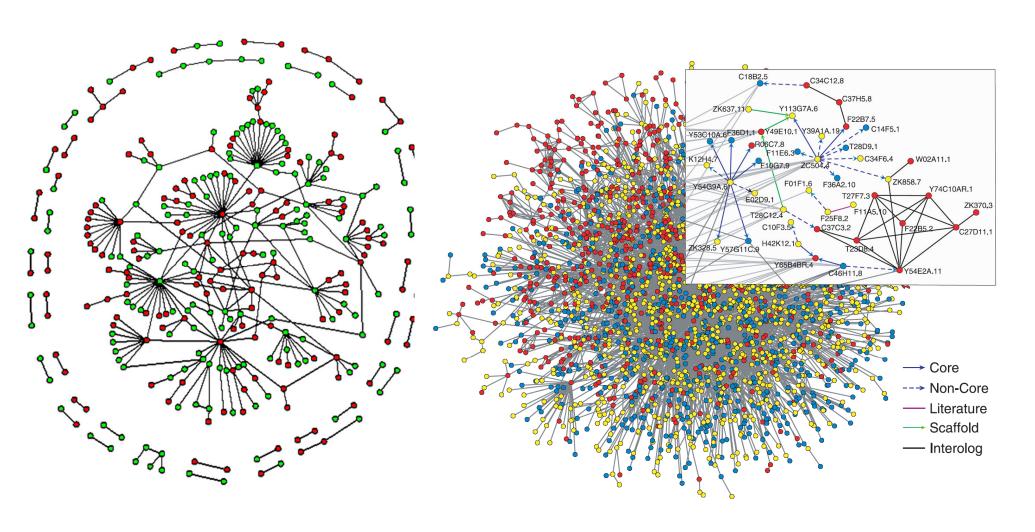


Basic concepts of network analysis

Reminder from the first lecture

Protein-Protein binding IntAct Database (Dec 2015)

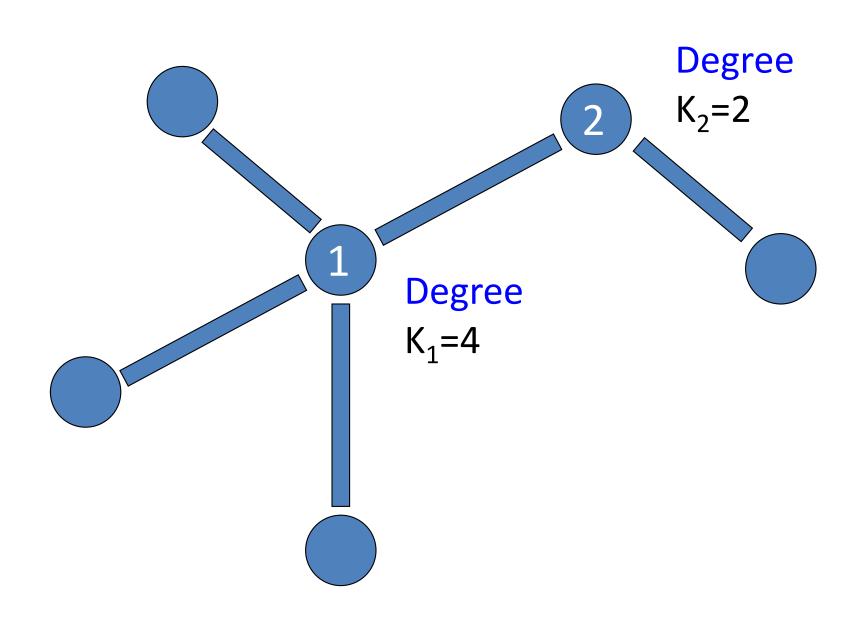
Interactions: 577,297 Proteins: 89,716



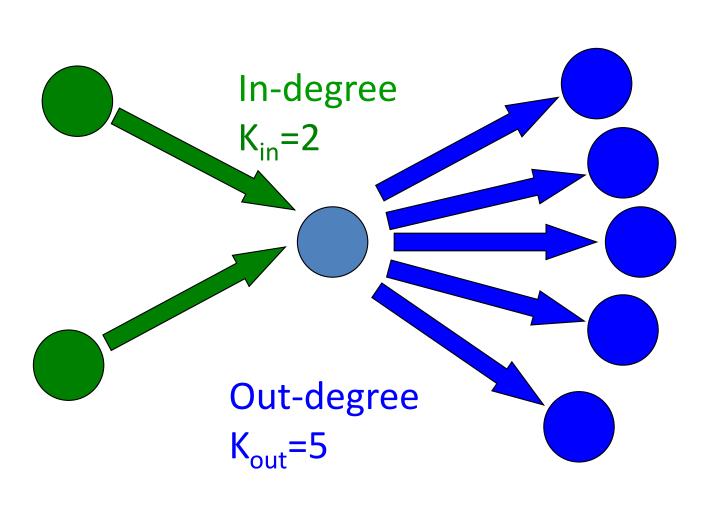
Baker's yeast *S. cerevisiae* (only nuclear proteins shown) From S. Maslov, K. Sneppen, Science 2002

Worm *C. elegans* From S. Lee et al , Science 2004

Degree of a node – its # of neighbors

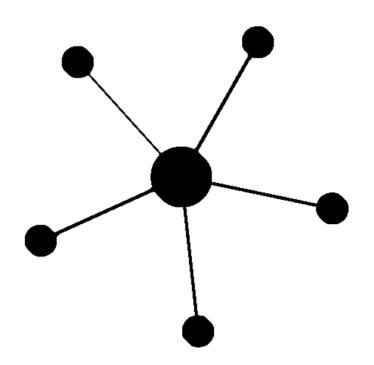


Directed networks have in- and out- degrees



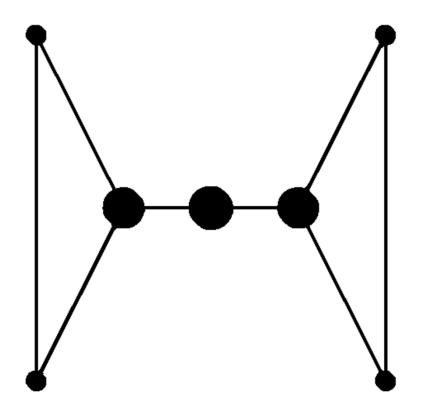
How to find "important" nodes?

- By their degree
- Hubs = important
- Example: Google's PageRank



How to find "important" nodes?

- By their connectivity
- Connectors = important
- Betweenness-centrality

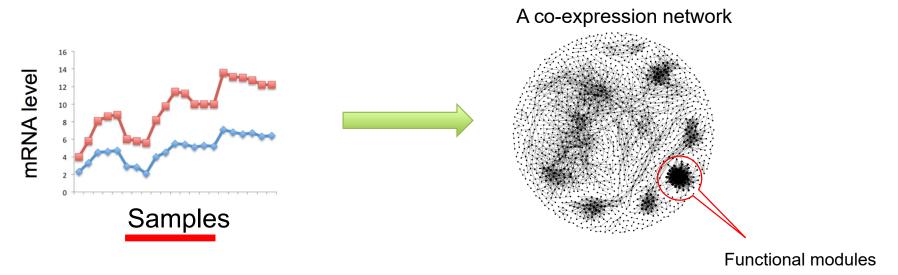


Betweenness centrality: definition

- Take a node i
- There are (N-1)*(N-2)/2 pairs of other nodes
- For each pair find the shortest path on the network
- If more than one shortest path, sample them equally
- Betweenness-centrality C(i) ~ the number of shortest paths going through node i

To analyze correlations in expression for all pairs of genes: Co-expression networks

How to construct a co-expression network?



- Start with a matrix of log2 of expression levels of N genes in K samples (conditions): for our T-cell data N=3000, K=47
- For each of N(N-1)/2 pairs of genes i and j calculate the correlation coefficient $\rho_{ii} = \sigma_{ii}/\sigma_i \sigma_i$ of gene levels across K samples
- Put a threshold, e.g. ρ_{ij} >0.85, or otherwise select the most correlated pairs of genes (~4500 in our case). Now you have a weighted network.
- Identify densely interconnected functional modules in this network.
- Modules can be used to infer unknown functions of genes via "Guilt by Association" principle.

How to install Gephi software for network analysis?

- Install Gephi from: https://gephi.org/users/download/
- One of the common problems with installation is the version of Java on your computer. One possible solution is here: https://github.com/gephi/gephi/issues/1787.

Sometimes after installation Gephi may complain that it cannot find java version 1.8 or higher. In this case you need to go to C:\Program Files\Gephi-0.9.2\etc

Open file gephi.conf using notepad.exe (MS Word does not work!).

Add a line jdkhome="C:\Program Files (x86)\Java\jre1.8.0_231"

(the numbers in ...jre1.8.0_231 may be changed to reflect the actual directory where Java is installed on your computer). If JDK is not installed on your computer, you need to install itfirst from https://www.java.com/en/download/win10.jsp"

Co-expression network analysis exercise

- Start Gephi and open coexpression_network_random_start.gephi
- Run "Layout" → Fruchterman Reingold → Speed 10.0
- Run "Average degree", "Network diameter", "Modularity" in the Statistics tab in the right panel.
- Color nodes by "modularity class":
 Appearance → Nodes → Partition → Palette Icon → Modularity class
- Size nodes first by "degree".
 Appearance → Nodes → Ranking → Multiple Circles Icon → Degree
 - If the nodes are too small, select "Min size": 10 and "Max size":80
 - Nodes in large tightly connected clusters have large degree
- Then size nodes by "betweenness-centrality"
 Appearance → Nodes → Ranking → Multiple Circles Icon → Betweenness-centrality
 - Large circles are "coordinator" genes connecting different co-expressed clusters to each other. Potentially biologically interesting

Disease-disease similarity network

- Based on the table summarizing all current medical knowledge of genes implicated in diseases:
 - Rows: 516 common human diseases
 - Columns: 25,000 human genes
 - Matrix element $D_{i\alpha}$ =1 if the gene α is known to be involved in the disease i . 0 otherwise
- Constructed disease-disease similarity network:
 - Weight of the edge # of shared genes between two diseases
 - Easy to construct: the adjacency matrix A of the network is simply A=D•D⁺

Disease network analysis exercise

- Start Gephi and open disease_disease_random_start.gephi
- Run "Layout" → Fruchterman Reingold → Speed 10.0
 Observe how clusters emerge.
- Run "Average degree", "Network diameter", "Modularity" analysis tools in the right panel.
- Color nodes with medical term: "disorder class"
 Appearance → Nodes → Partition → Palette Icon → Disorder class
- Then color nodes by "modularity class". See how well it agrees with the previous color.
 - Appearance \rightarrow Nodes \rightarrow Partition \rightarrow Palette Icon \rightarrow Modularity class
- Size nodes first by "degree".
 - Appearance → Nodes → Ranking → Multiple Circles Icon → Degree
 - Which disease has the largest degree?
- Size nodes by "betweenness centrality"
 - Appearance → Nodes → Ranking → Multiple Circles Icon → Degree
 - Which diseases have the largest betweenness-centrality?
 - These "connector" diseases linking different diseases clusters to each other. They highlight potentially interesting connections between diseases

